

MUTAC Review
March 16, 2006, FNAL, Batavia, IL

Target Simulations

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Neutrino Factory / Muon Collider Collaboration Meeting
March 13, 2006, FNAL, Batavia, IL

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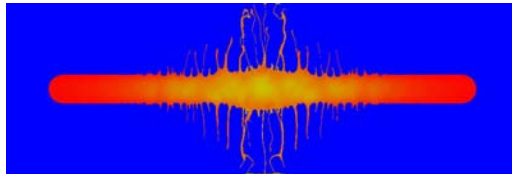
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Talk Outline

- Brief summary of previous results
- New development of FronTier MHD code
- Studies of the distortion of the mercury jet entering a 15 T magnetic solenoid. Comparison with HIMAG simulations (UCLA computational MHD group)
- Simulation of droplets in magnetic fields
- Simulation of the mercury jet – proton pulse interaction. Electrical conductivity models for multiphase systems (cavitating flow).
- Conclusions and future plans

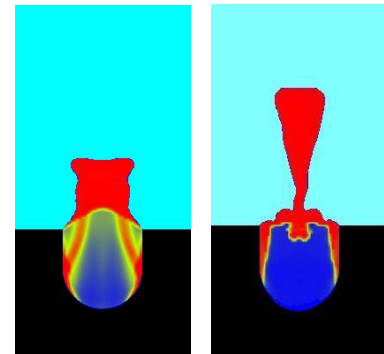
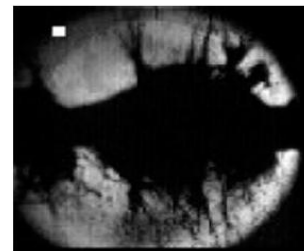
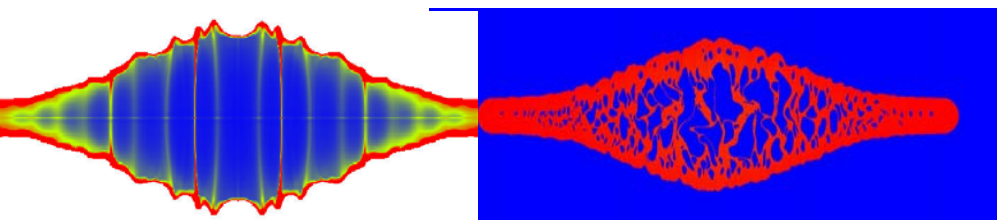
Brief summary of previous results

- Developed MHD code for compressible multiphase flows
- Developed EOS homogeneous and heterogeneous models for phase transition (cavitation) and the Riemann solver for the phase boundary
- Studied surface instabilities, jet breakup, and cavitation
- Found that MHD forces reduce both jet expansion, instabilities, and cavitation



Jet surface instabilities

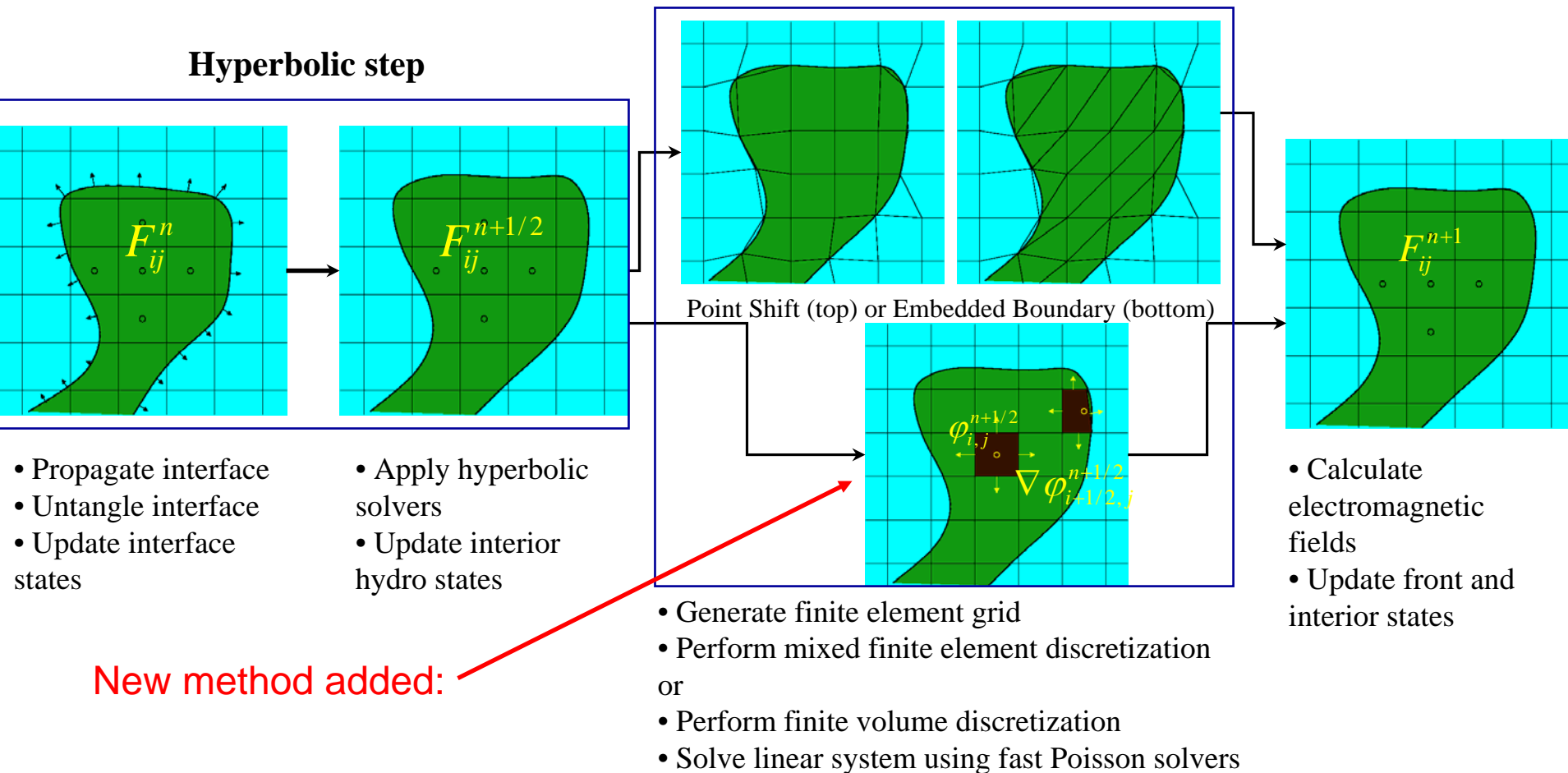
Cavitation in the mercury jet and thimble



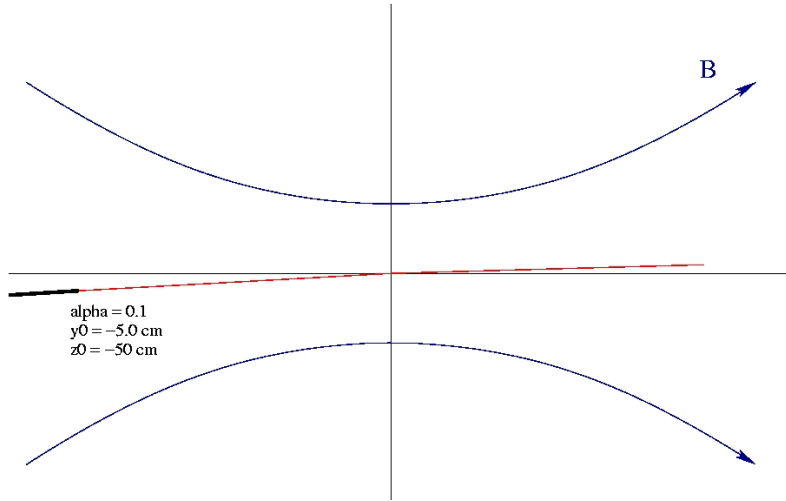
New elliptic solvers for MHD implemented in FronTier

- To improve robustness of the code with complex 3D interfaces, a new solver based on the Embedded Boundary method has been implemented and tested.
- The new code has been used for 3D jet and droplet simulations.

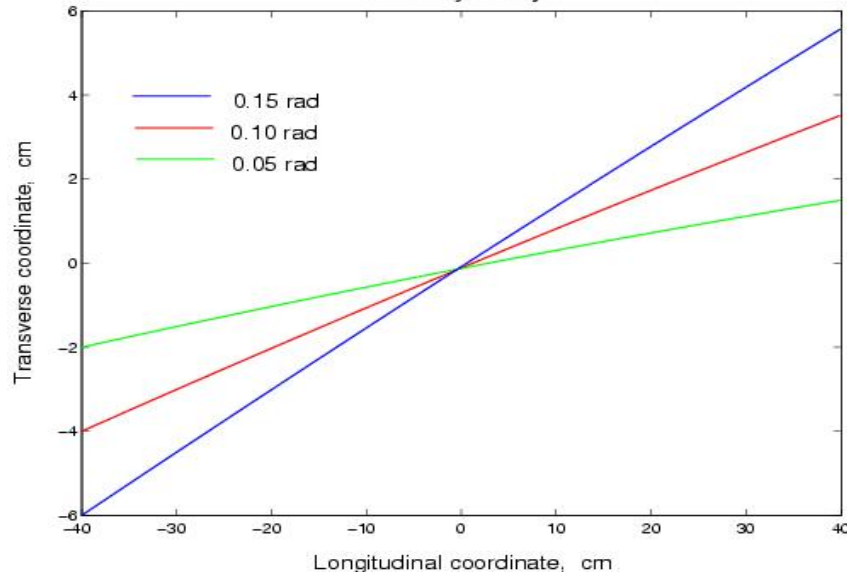
Schematic of FronTier-MHD



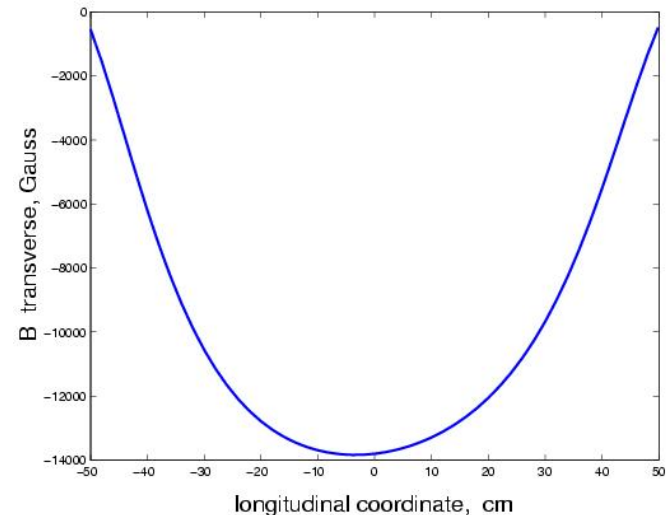
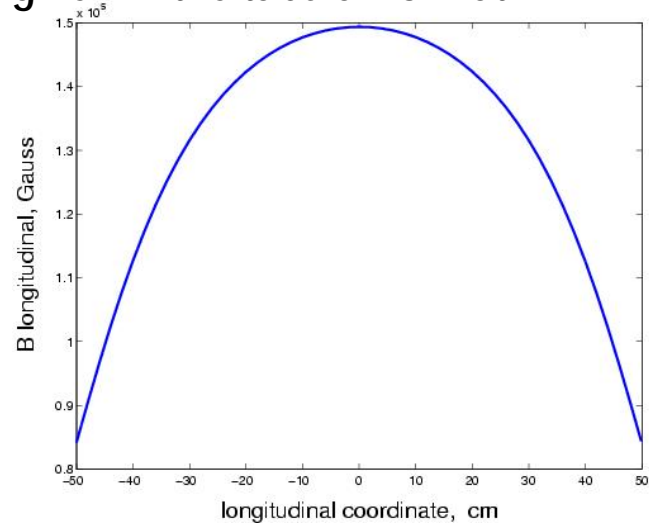
Mercury jet entering magnetic field. Schematic of the problem.



Jet trajectory



Magnetic field of the 15 T solenoid is given in the tabular format



Two research approaches

- Direct numerical simulations (FronTier and HIMAG)
- Perturbation series semi-analytical/semi-numerical studies.

$$\rho \mathbf{u} \cdot \nabla \mathbf{u} = -\nabla P + \frac{1}{c} (\mathbf{J} \times \mathbf{B})$$

$$\nabla \cdot \mathbf{u} = 0$$

$$\left. \begin{aligned} \mathbf{J} &= \sigma \left(-\nabla \phi + \frac{1}{c} \mathbf{u} \times \mathbf{B} \right) \\ \nabla \cdot \mathbf{J} &= 0 \end{aligned} \right\} \Rightarrow \Delta \phi = \frac{1}{c} \nabla \cdot (\mathbf{u} \times \mathbf{B})$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{B} = 0$$

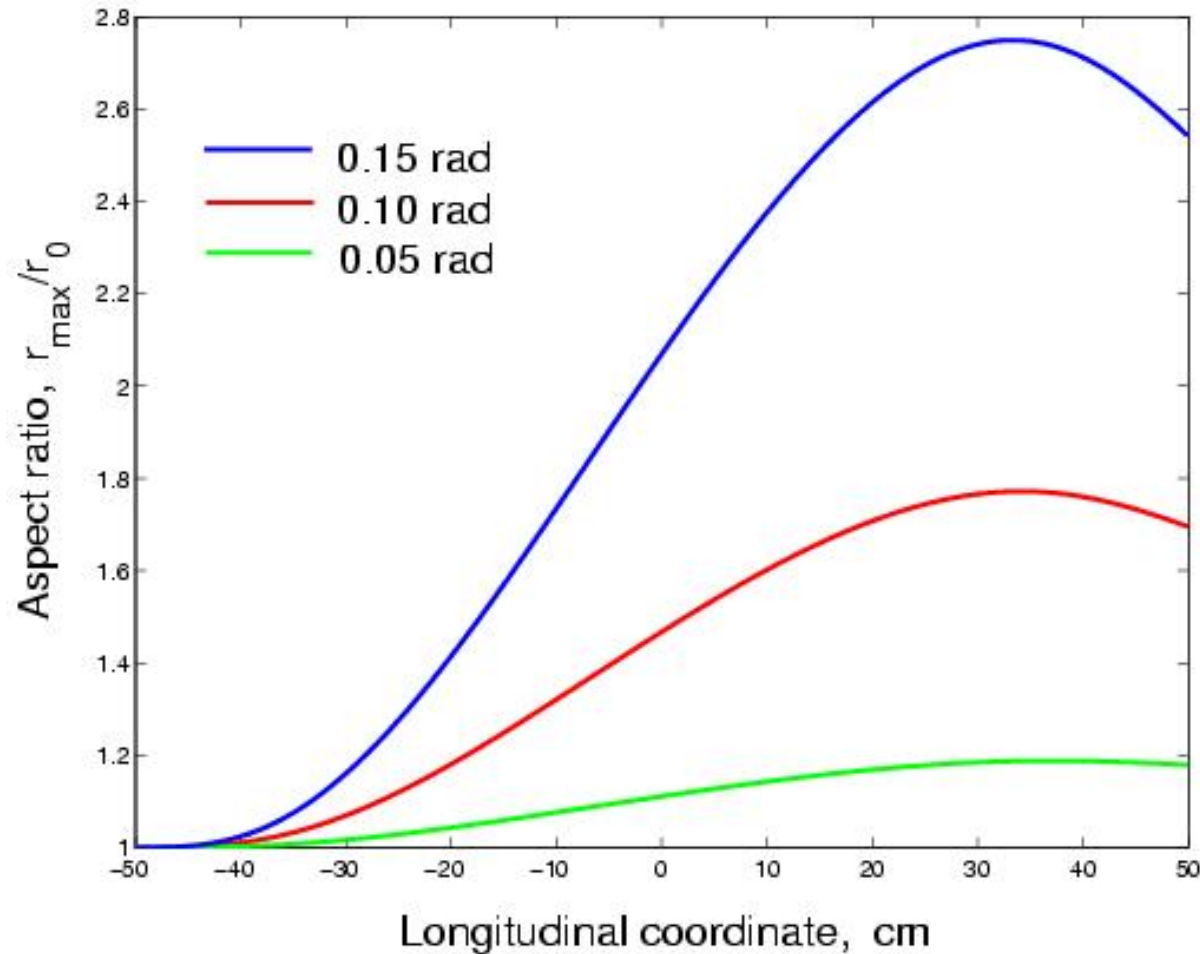
B.C.:

$$\left. \frac{\partial \phi}{\partial \mathbf{n}} \right|_{\Gamma} = \frac{1}{c} (\mathbf{u} \times \mathbf{B}) \cdot \mathbf{n}$$

$$p_{\Gamma} - p_a = S \left(\frac{1}{r_1} + \frac{1}{r_2} \right)$$

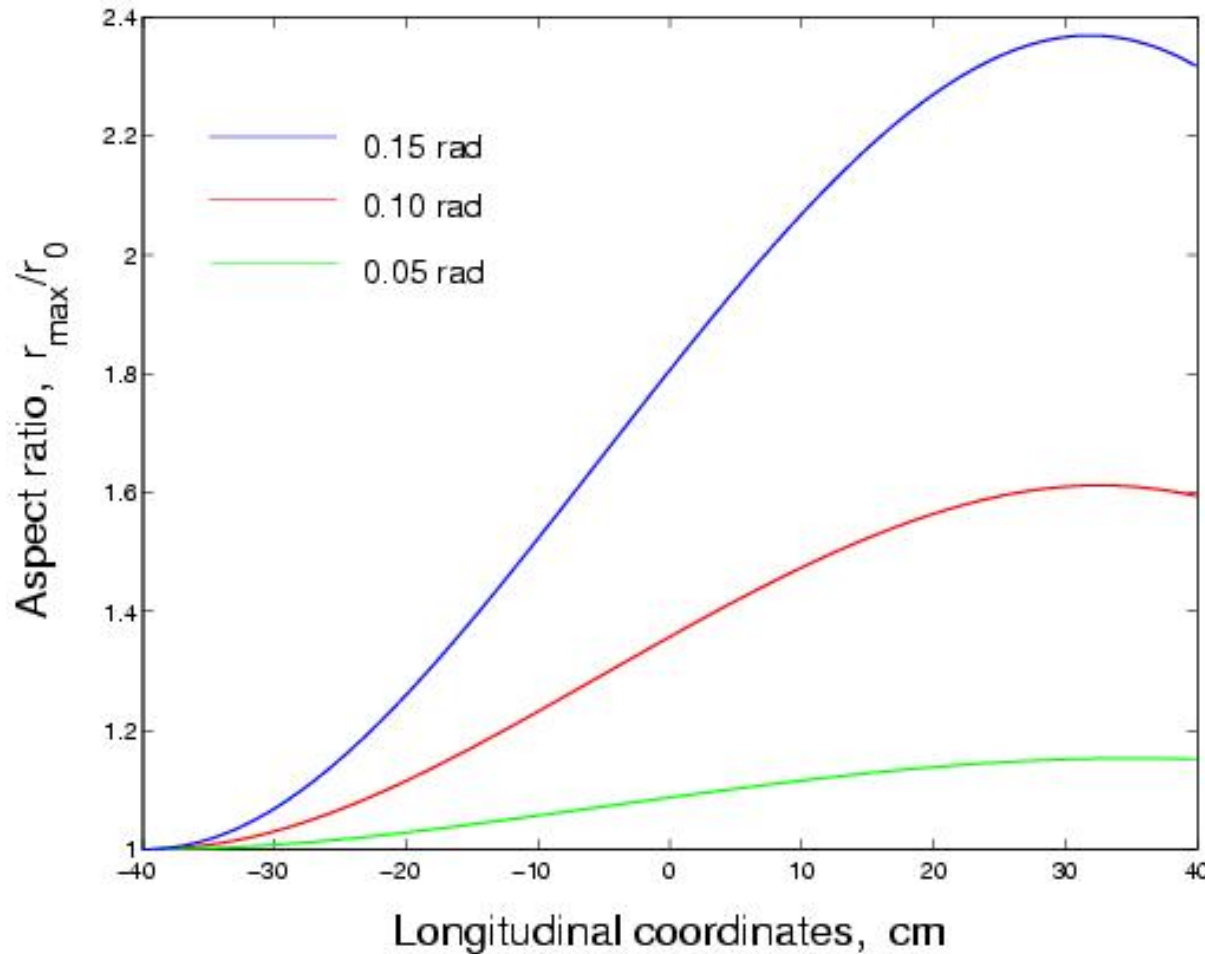
$$\mathbf{u}_{\Gamma} \cdot \mathbf{n} = 0$$

Results: Aspect ratio of the jet cross-section. I



$B = 15 \text{ T}$
 $V_0 = 25 \text{ m/s}$

Results: Aspect ratio of the jet cross-section. II



$B = 15 \text{ T}$
 $V_0 = 25 \text{ m/s}$

Summary of results

- Jet distortion (aspect ratio) strongly depends on the angle with the solenoid axes (it increases at larger angles)
- Jet aspect ratio increases at smaller jet velocities (at least if the change of velocity is small compared to the reference velocity of 25 m/s)
- Jet aspect ratio increases in nozzle is placed further from the solenoid center

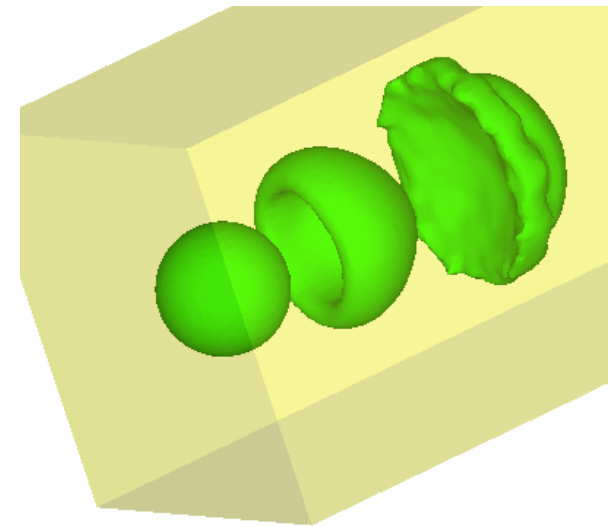
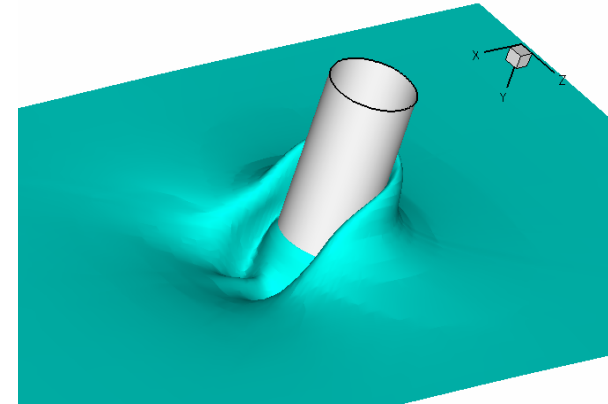
Typical values of the jet aspect ratio in the center of the solenoid:

$R_{\max}/R_0 = 1.35$ at $V = 25$ m/s, $\alpha = 100$ mrad, $B = 15$ T

$R_{\max}/R_0 = 1.09$ at $V = 25$ m/s, $\alpha = 50$ mrad, $B = 15$ T

UCLA code: HIMAG

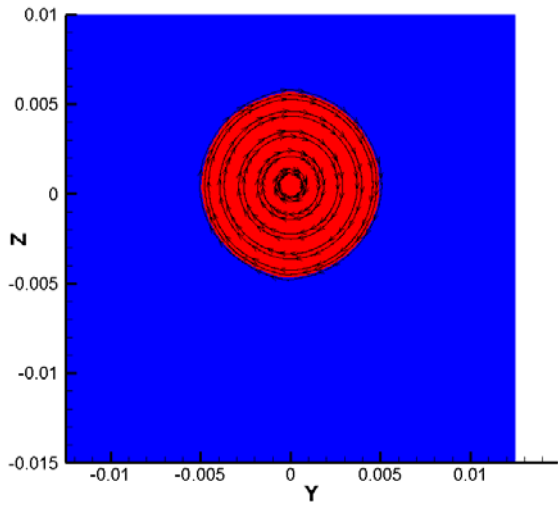
- HIMAG is a parallel, second order accurate, finite volume based code for incompressible MHD and Navier-Stokes equations.
- The code has been written for complex geometries using unstructured meshes. Flexibility in choosing a mesh: Hexahedral, Tetrahedral, Prismatic cells can be used.
- An arbitrary set of conducting walls maybe specified. Free surface flows are modeled using the Level Set method. **Multiple solid materials** can be simulated
- Graphical interfaces are available to assist users from problem setup to post-processing.
- A preliminary turbulence and heat transfer modeling capability now exists.



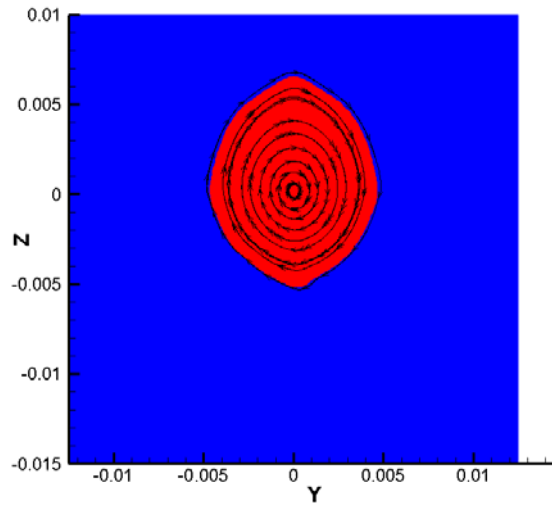
UCLA jet simulation setup

- The magnetic axis of the solenoid is horizontal. Magnetic field simulated as 24 x 78 windings with 7200 A spaced uniformly in ID 20 cm and OD 80 cm and axial length 1 m
- 100 mrad and 33 mrad tilt angle
- Inlet velocity 20 m/s
- Injection point of the jet is located at -5cm below the magnetic axis and -50cm from the solenoid center.
- The inlet electric potential condition is $\Phi = 0$, trying to simulate disturbances from a perfectly conducting nozzle
- MHD forces are turned off at the exit two diameter before the computational boundary
- Computational area 2.5 x 2.5 x 100 cm with 100 x 100 x 200 computational cells.

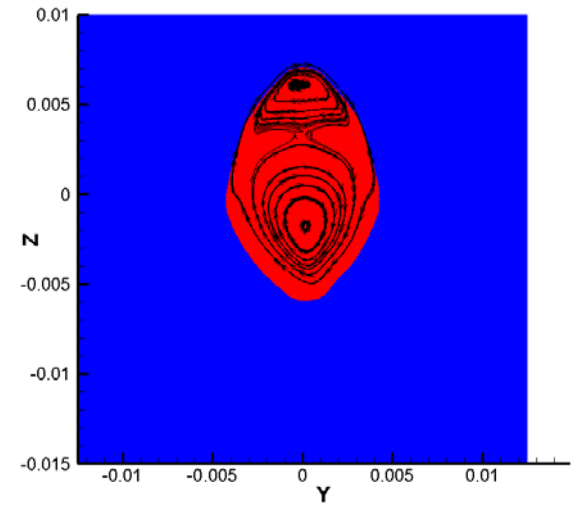
100 mrad tilt angle



$z = 0$ cm



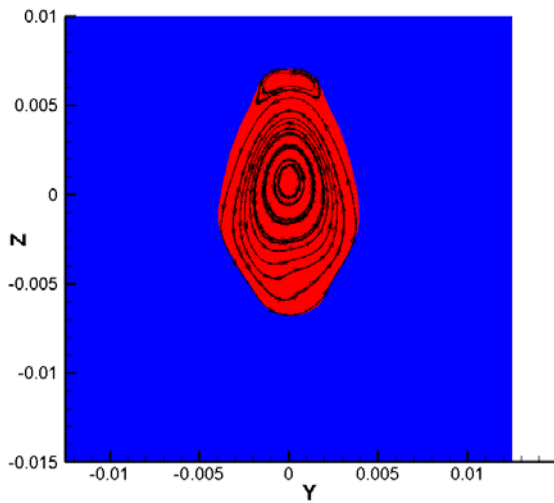
$z = 20$ cm



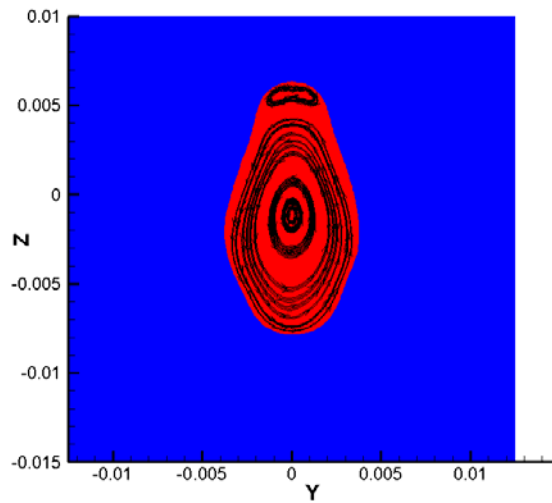
$z = 30$ cm

Aspect ratio = 1.4 in the solenoid center

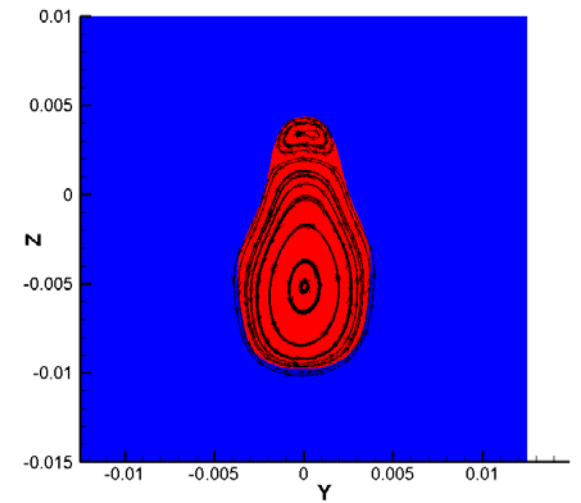
$z = 40$ cm



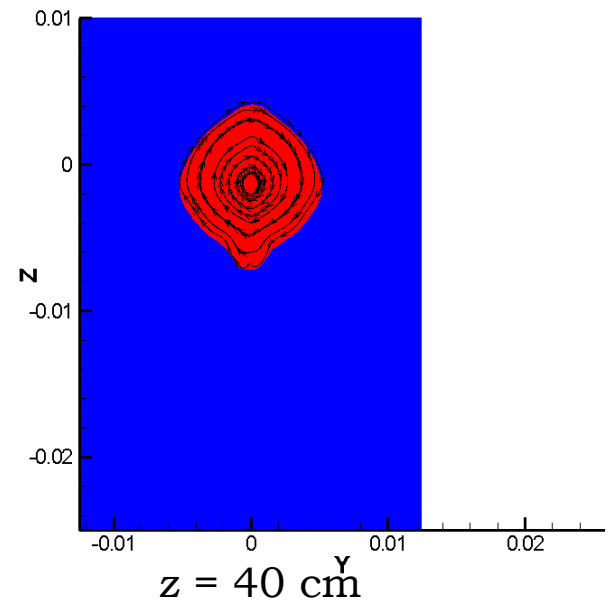
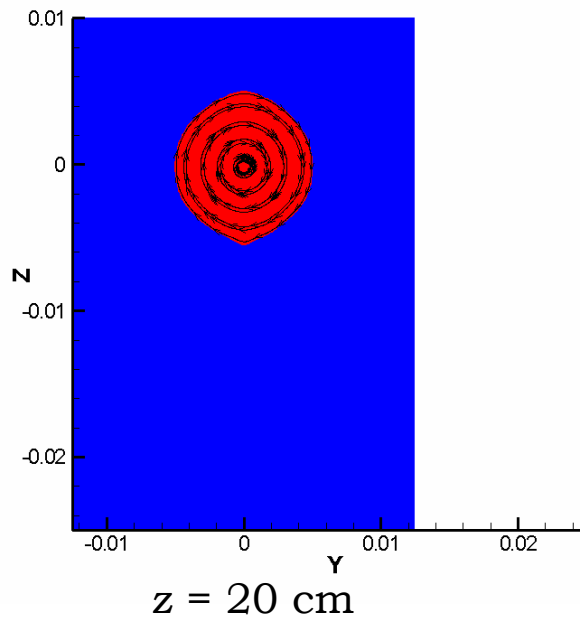
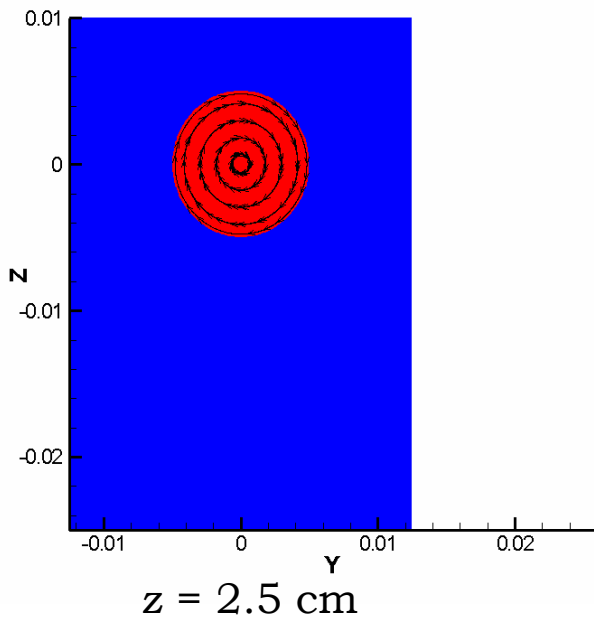
$z = 50$ cm



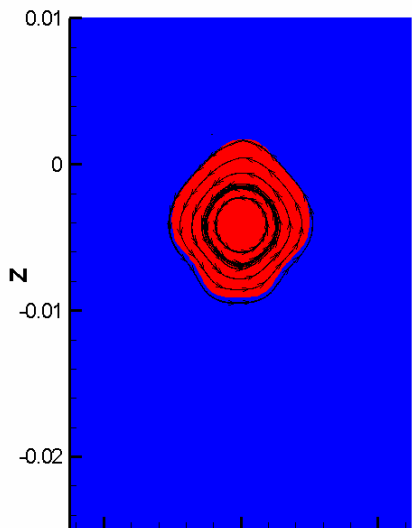
$z = 60$ cm



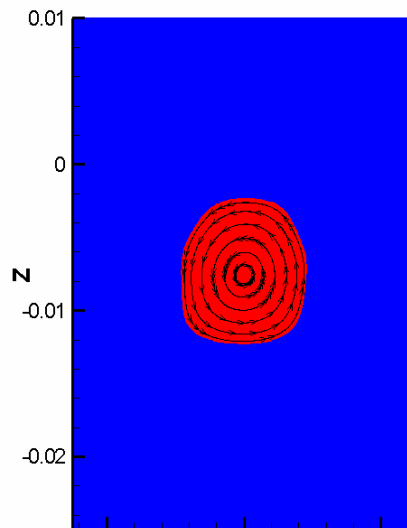
33 mrad tilt angle



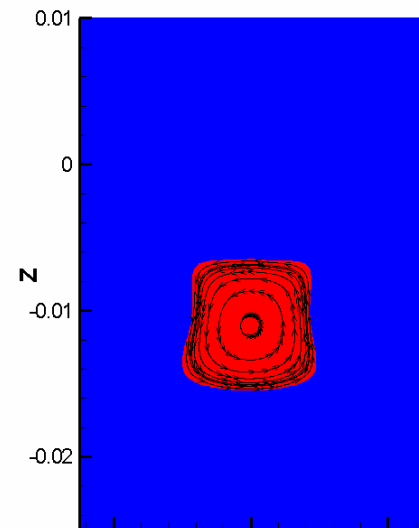
$z = 60$ cm



$z = 80$ cm



$z = 98$ cm

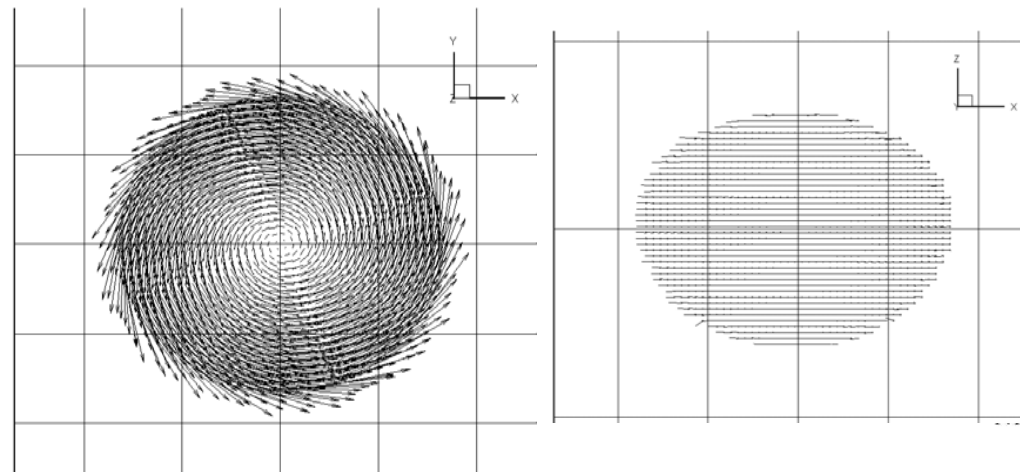
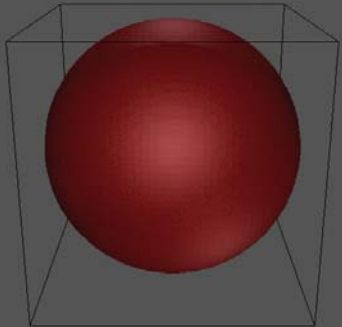


Consequences of the jet distortion

- Confirmed the distortion of the jet in the 15 T solenoid. Jet evolution exhibited the same features: reduction of the aspect ratio with the increase of the jet velocity, sensitivity to the nozzle placement, and the angle of the jet with the solenoid axis.
- Good quantitative agreement was achieved by independent studies.
- As a result of the jet distortion, the cross-section of the mercury jet interaction with the proton pulse is significantly reduced. This reduces particle production rate
- **In order to reduce the jet distortion, the angle between the magnetic field and the solenoid axes for future experiments has been reduced to 33 mrad.**

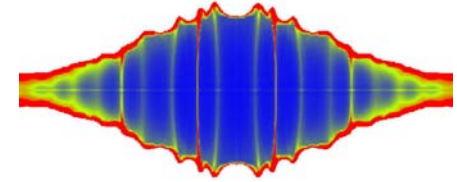
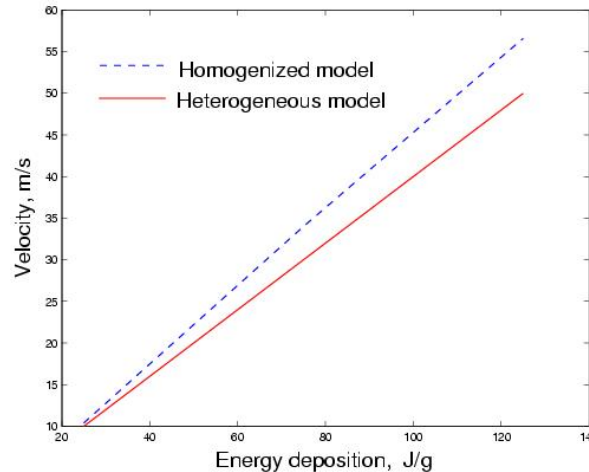
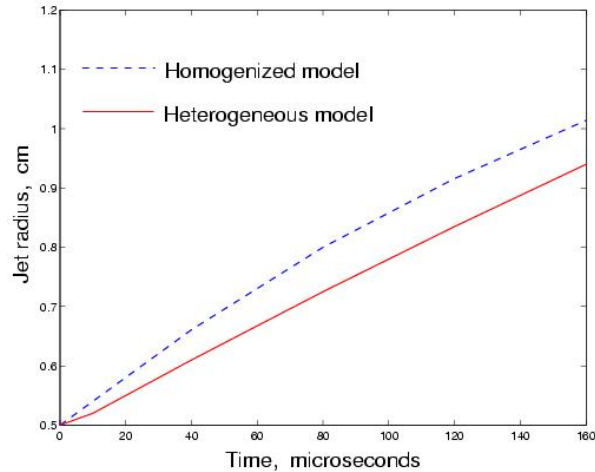
Droplet studies in magnetic fields

- Studied the evolution of droplets ($r \sim 1\text{-}3\text{ mm}$) moving longitudinally and transversely in the 15 T solenoid with velocities $\sim 10 - 100\text{ m/sec}$.
- Change of the velocity of droplets was **negligible**.
- Slight deformation of droplets traveling longitudinally in the high grad **B** region.

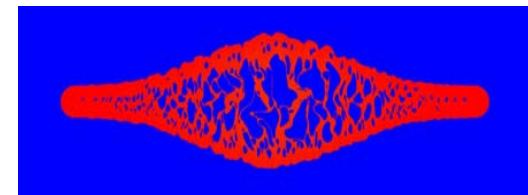


Mercury jet – proton pulse interaction using different EOS models

- We evaluated and compared homogeneous and heterogeneous cavitation models:



Homogeneous model



Heterogeneous model

- Two models agree reasonably well
- Since 3D direct numerical simulation of cavitation bubbles with the resolution of small scale effects still remain prohibitively expensive, the homogeneous model is currently used for 3D simulations
- Problem of electrical conductivity of multiphase domains within the homogeneous model.

Electrical conductivity models for multiphase mixtures (cavitating liquid)

- There are several models for the conductivity of multiphase mixtures (the original one proposed by Maxwell)
- Most of them predict phase transition (in the conductivity parameter at some critical volume fraction)
- Bruggeman's Symmetrical Effective Medium Theory

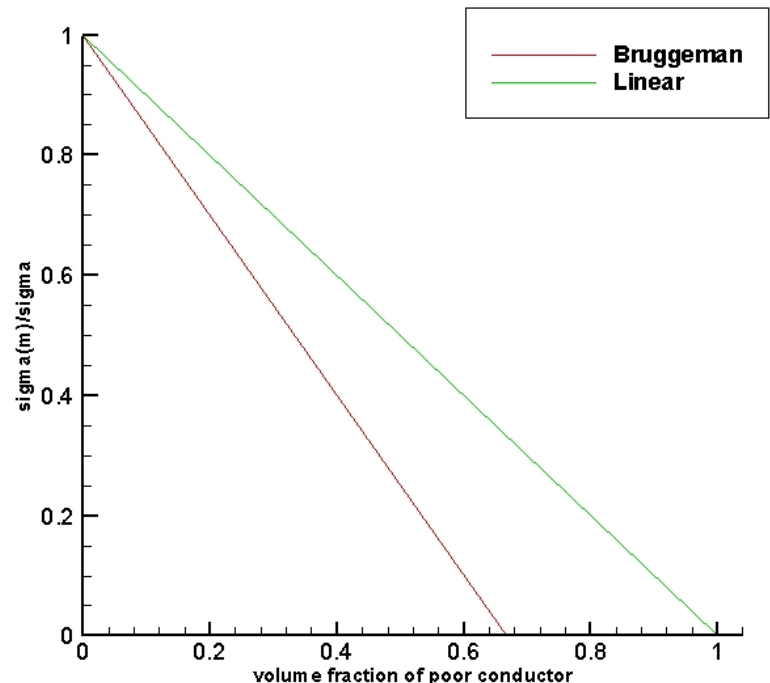
$$\delta_1 \frac{\sigma_1 - \sigma_m}{\sigma_1 + 2\sigma_m} + \delta_2 \frac{\sigma_2 - \sigma_m}{\sigma_2 + 2\sigma_m} = 0$$

$\delta_{(1,2)}$ -- volume fraction of components

$\sigma_{(1,2)}$ -- conductivity of components

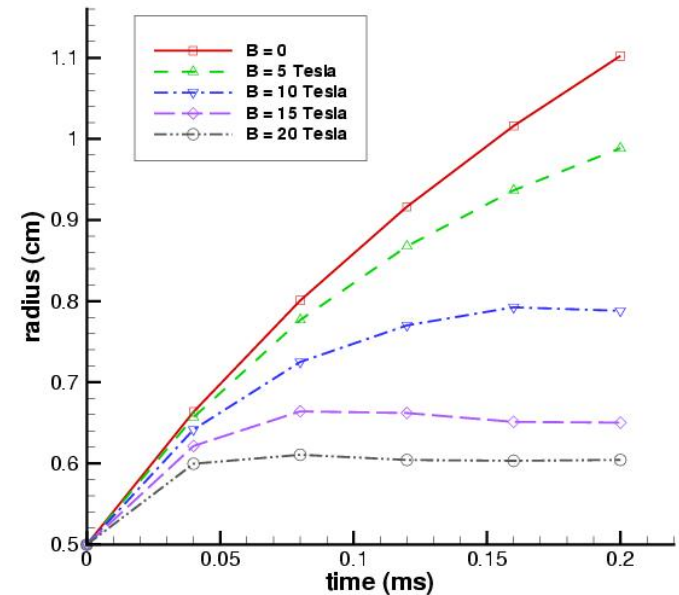
σ_m -- effective conductivity of mixture

$$\text{for } \sigma_1 \gg \sigma_2 \Rightarrow \sigma_m = \frac{\sigma_1}{2} (3\delta_1 - 1)$$



Numerical simulations

- The linear conductivity model predicts strong stabilizing effect of the magnetic field



- Stabilizing effect of the magnetic field is weaker if conductivity models with phase transitions are used (~ 20 % for Bruggeman's model)
- Influence of the droplet size on the conductivity is being studied now.

Conclusions and Future Plans

- Further development of mathematical models and software libraries for the FronTier-MHD code

- Deformation of the mercury jet entering 15 Tesla solenoid has been established. The design angle between the jet and solenoid axis has been changed to 33 mrad.

- Performed simulations of droplets. The calculated velocity change was negligible.

- Studies of the electrical conductivity for multiphase domains. Linear conductivity models predicts strong stabilizing effect of the magnetic field. Bruggeman's model predict 20% weaker effect.

- 3D numerical simulations of the mercury jet – proton pulse interaction.