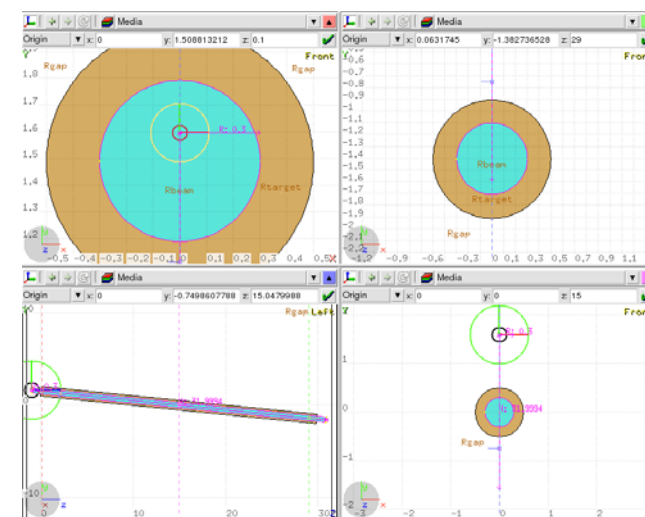
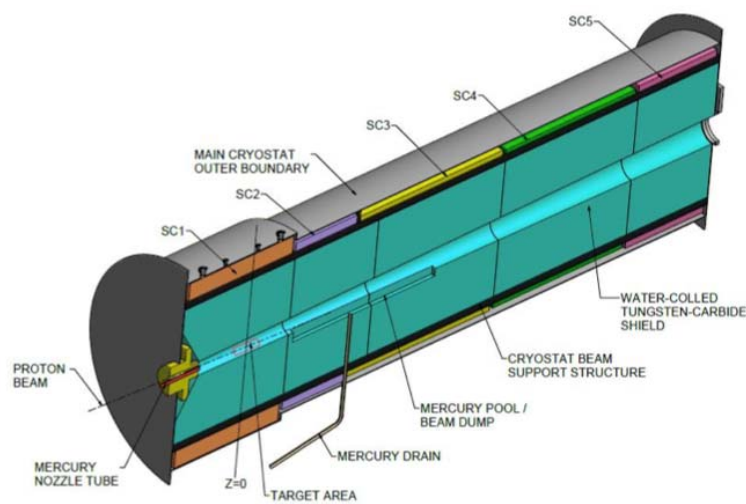
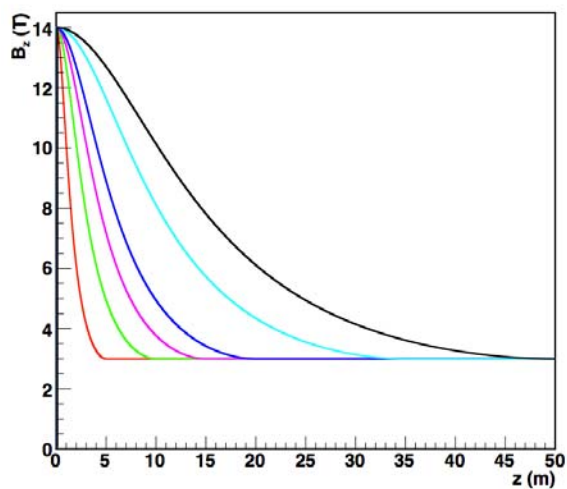




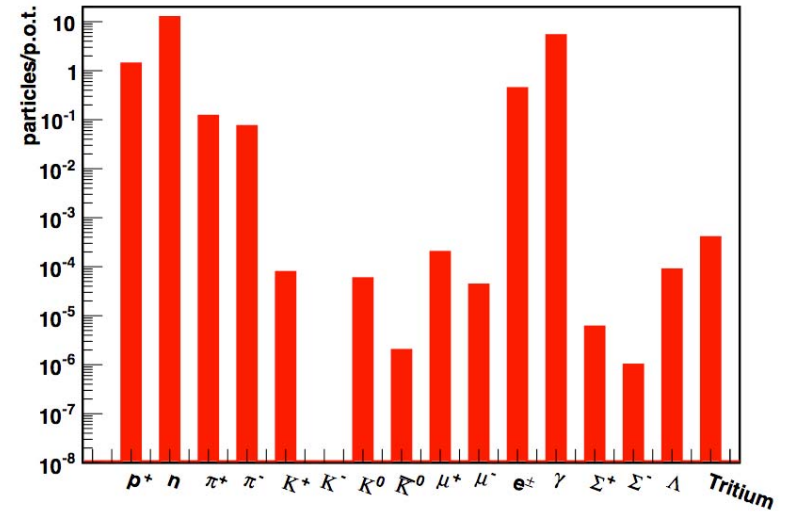
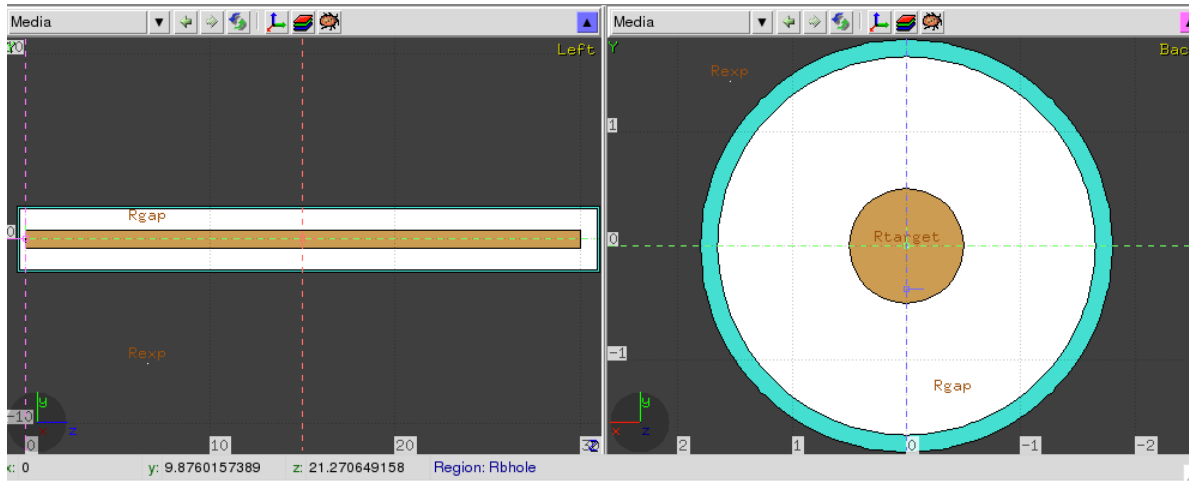
Institute of High Energy Physics
Chinese Academy of Sciences



Studies on pion/muon capture at MOMENT
Nikos Vassilopoulos
IHEP, CAS
August 11, 2015



particle production for Hg



MOMENT – Hg, L =30 cm, R = 0.5 cm: current parameters

σ_b (mm)	π^+	π^-	μ^+	μ^-	n	p^+
1	0.124	0.075	1.8×10^{-4}	5.3×10^{-5}	12.4	1.38

- $E_k = 1.5$ GeV
- no field, tilt
- 10^6 p.o.t. \rightarrow stat. error <1% for π, n, p and 6, 15% for μ^+, μ^-
- FLUKA 2015

π^+ production and P_T acceptance for adiabatic solenoids

for adiabatic taper solenoid

- $B_1 = 14$ T, $r_1 = 20$ cm
- $P_{T1} = 420$ MeV/c

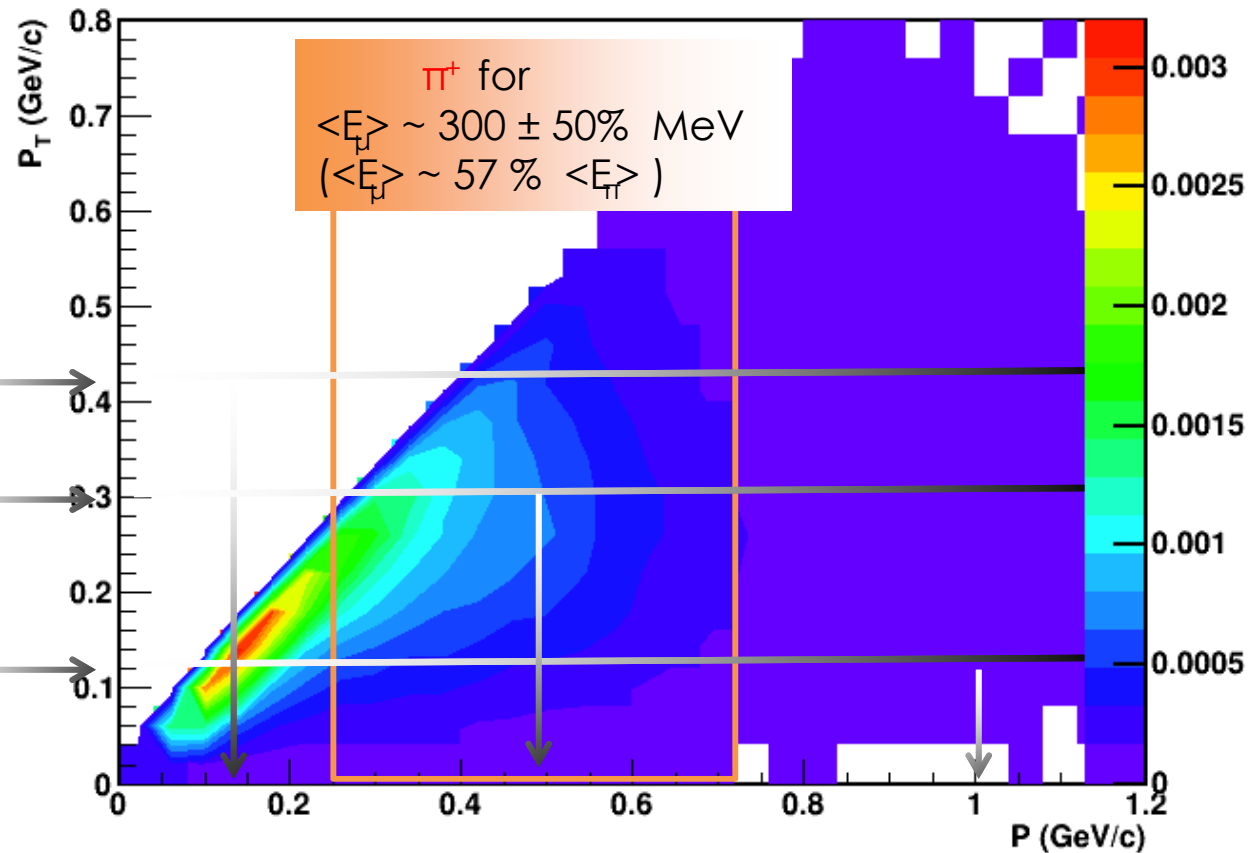


- $B_2 = 3$ T, $r_2 = 43$ cm
- $P_{T2} = 193$ MeV/c

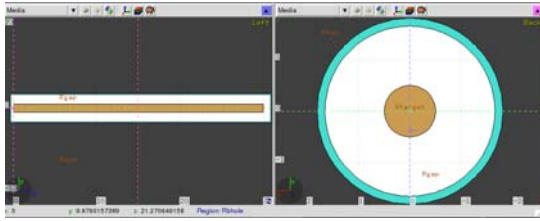
P_T accepted
 $r_1 = 20$ cm, $r_2 = 43$ cm

P_T accepted
 $r_1 = 14$ cm, $r_2 = 30$ cm

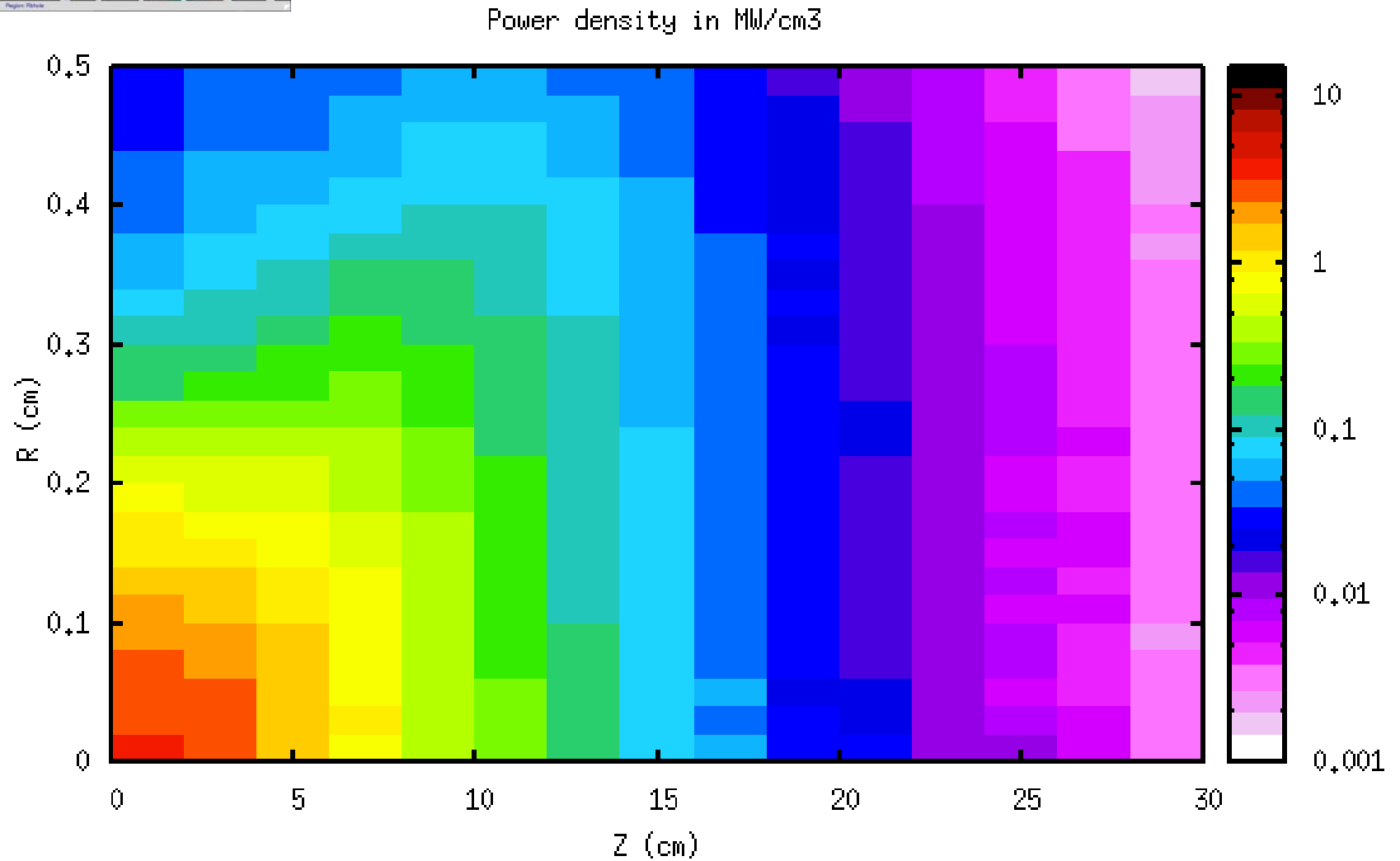
P_T accepted
 $r_1 = 7$ cm, $r_2 = 15$ cm



FLUKA 2015 (1e6 p.o.t.)



Power on target



$$P_{\text{trg}} = 2.5 \text{ MW}$$

optimization studies

figure of merit:

π, μ, ρ yields, distributions downstream of:

- the Main Capture Solenoid (MSC)
- Adiabatic Transport Solenoid

Main Capture Solenoid

“idealized” field

$$B = 14 \text{ T}, L_{\text{MCS}} = 32 \text{ cm}, r_{\text{MCS}} = 20 \text{ cm}$$



study tilts, lengths, radii, beam-sizes



Gaussian field approximation at MCS

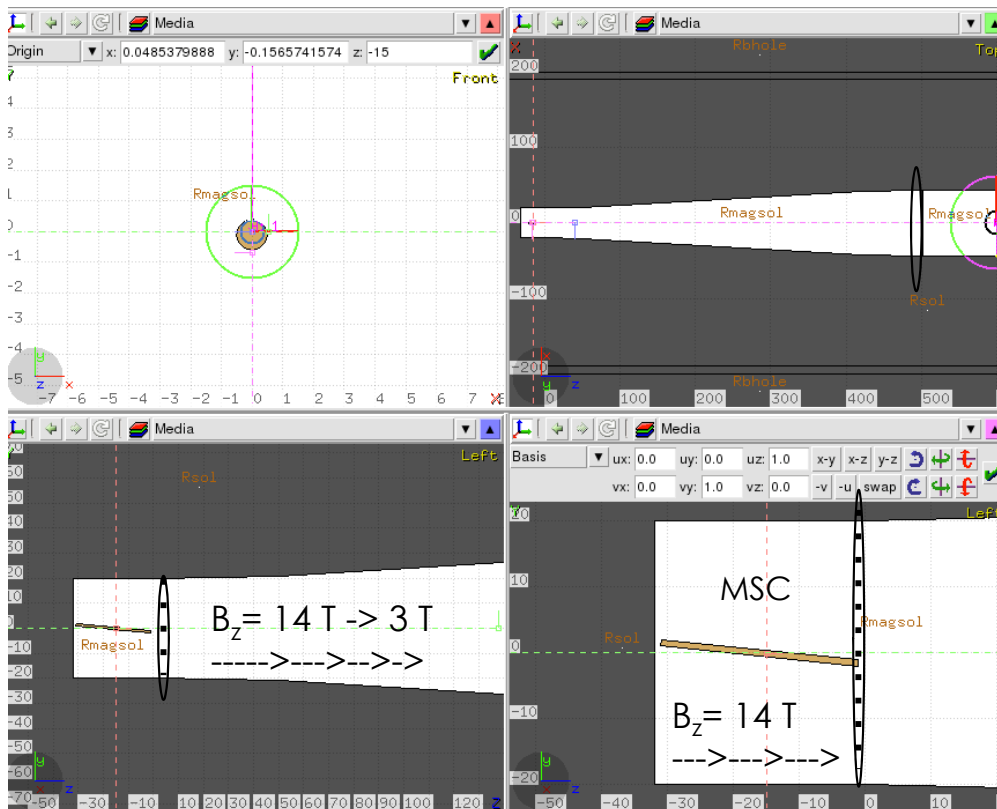


Adiabatic Transport Solenoid

$L = \underline{5}, 10, 15, 20, 35, \underline{50} \text{ m}$

$r = 20 \text{ cm} \rightarrow 43.2 \text{ cm}$

$B = 14 \text{ T} \rightarrow 3 \text{ T}$

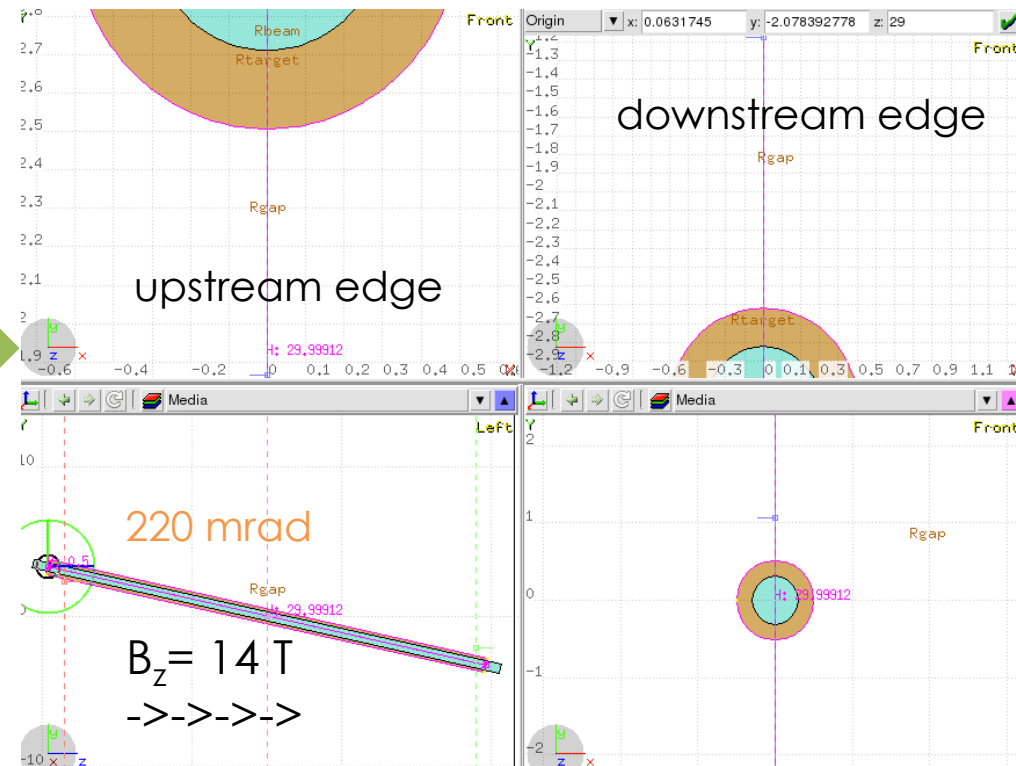
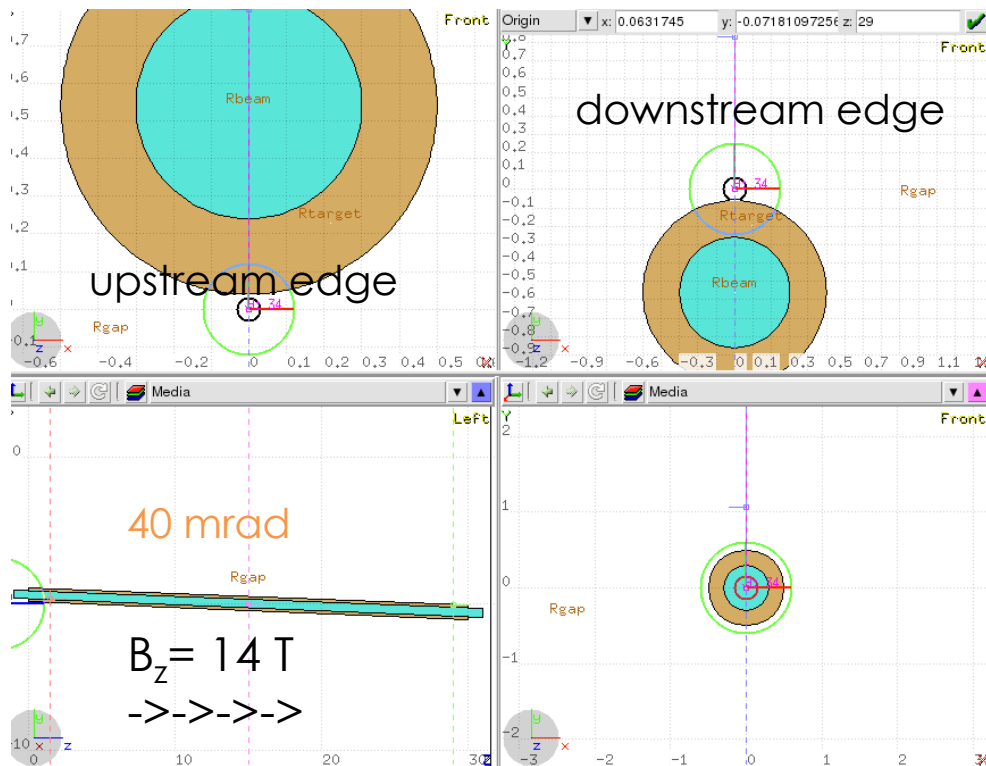


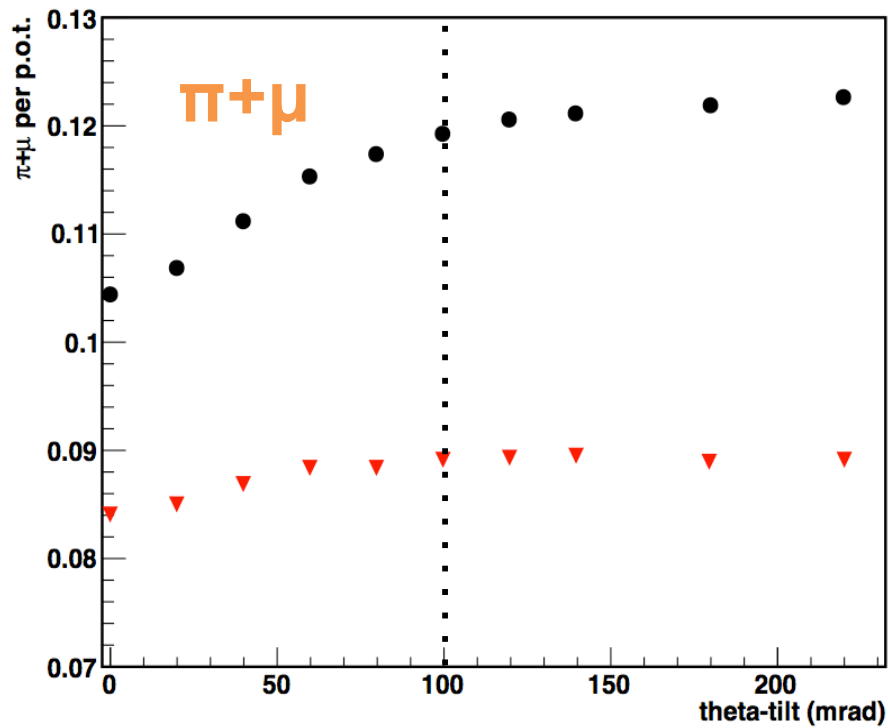
target tilt studies

$$L_{\text{trg}} = 30 \text{ cm}, r_{\text{trg}} = 5 \text{ mm}, \sigma_b = 1 \text{ mm}$$

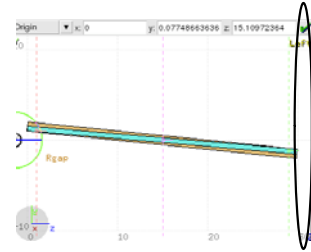
- π after one helix might hit the target, target tilt needed

$$\lambda_{\text{helix}} = \frac{2.1 * P_L (\text{MeV} / c)}{B_z (T)} \text{ cm}, \quad r_{\text{helix}} = \frac{P_T (\text{MeV} / c)}{3 * B_z (T)} \text{ cm}$$





particle yields at the edge of MCS for different tilts



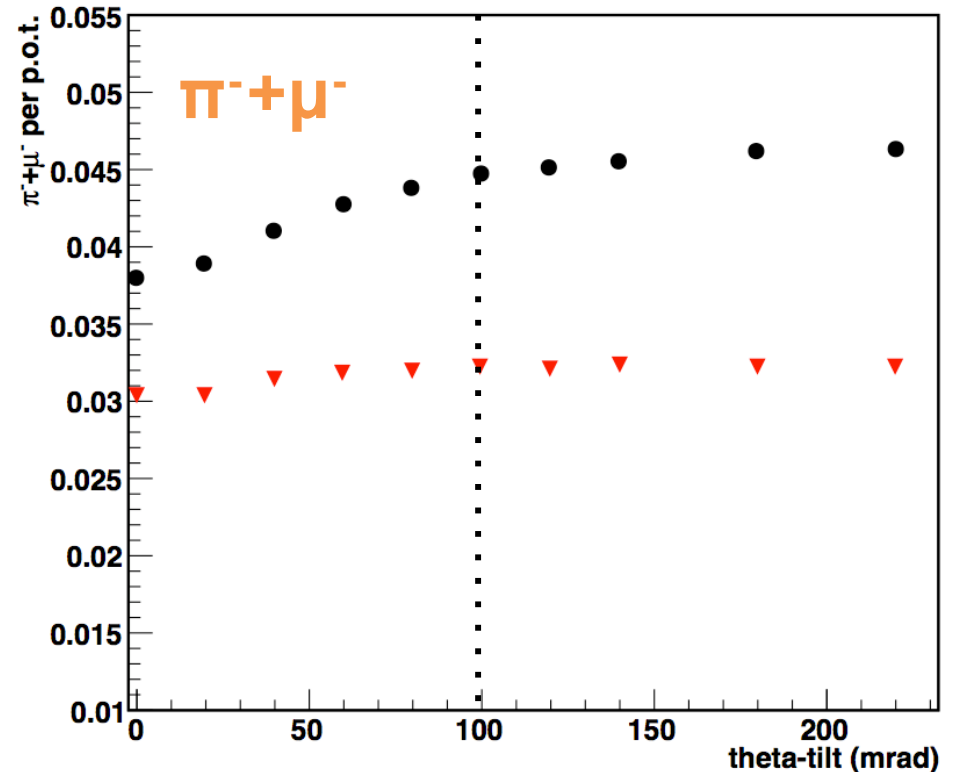
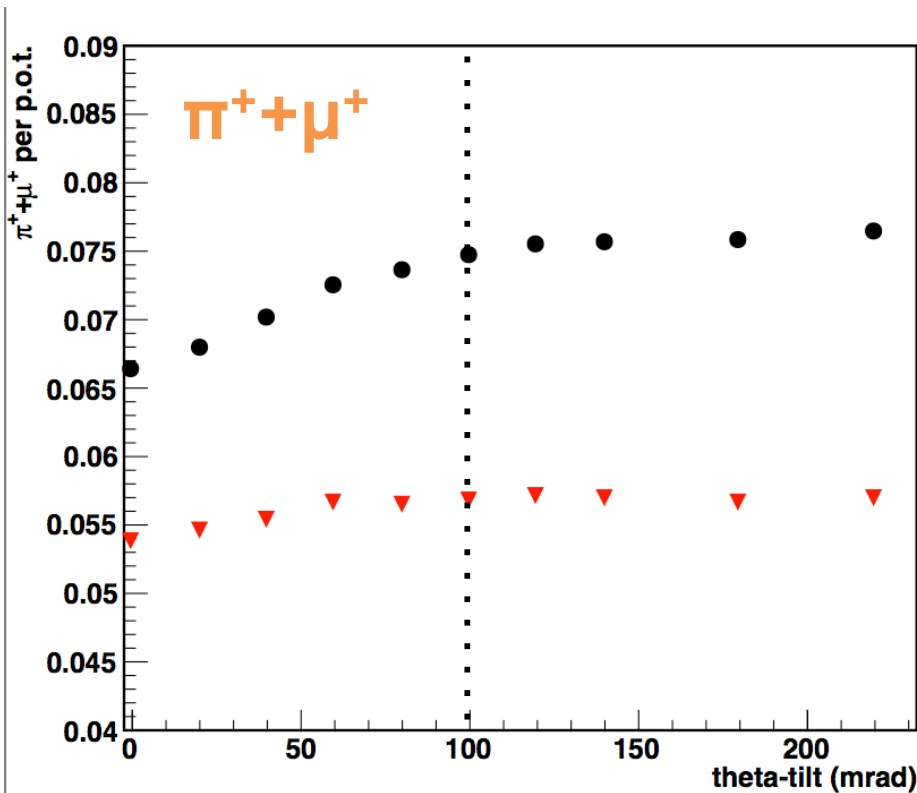
all momenta in black

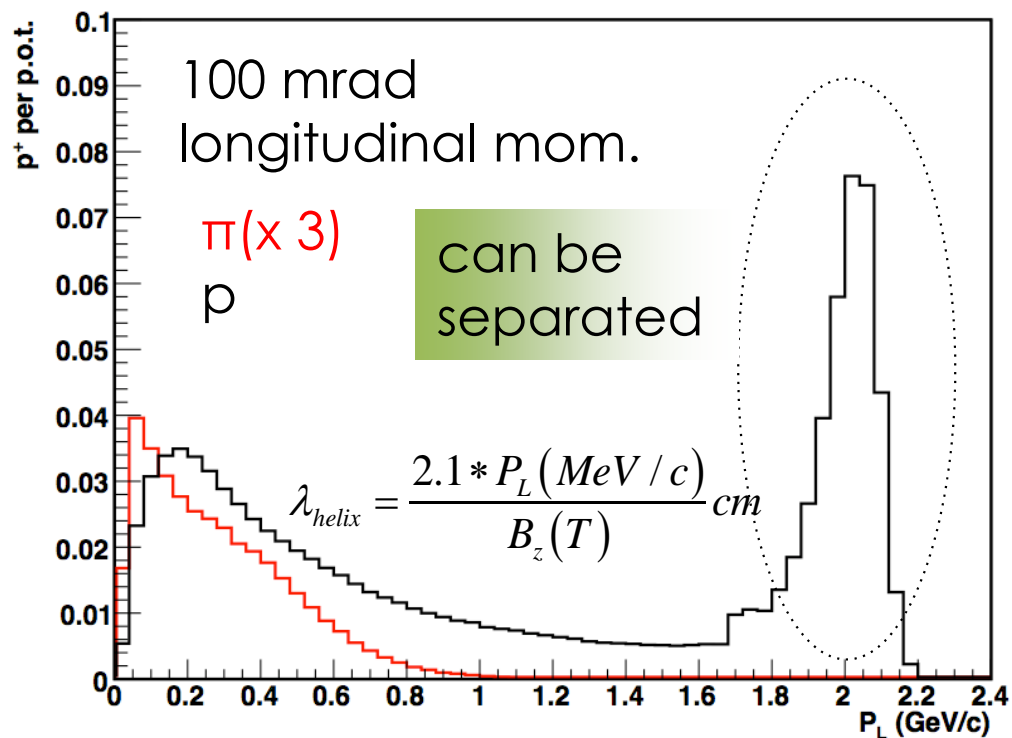
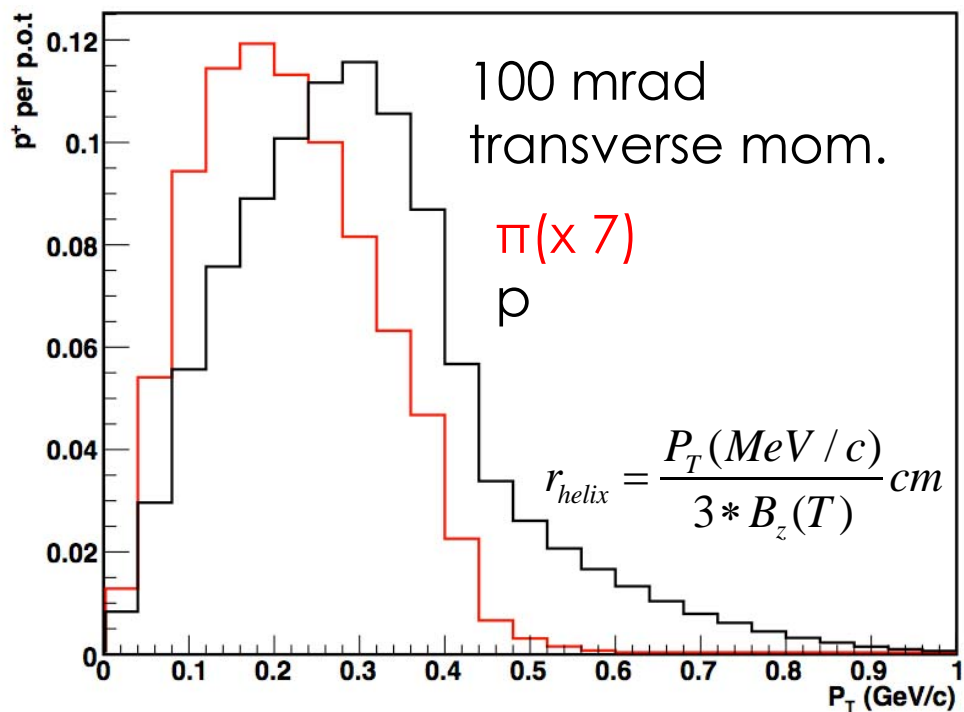
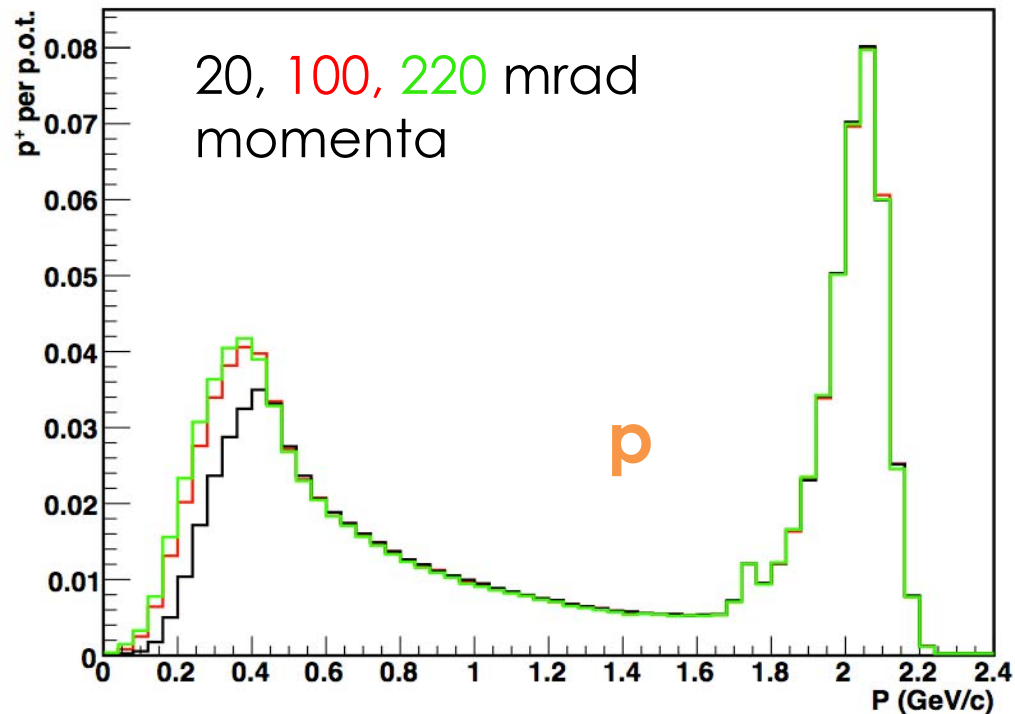
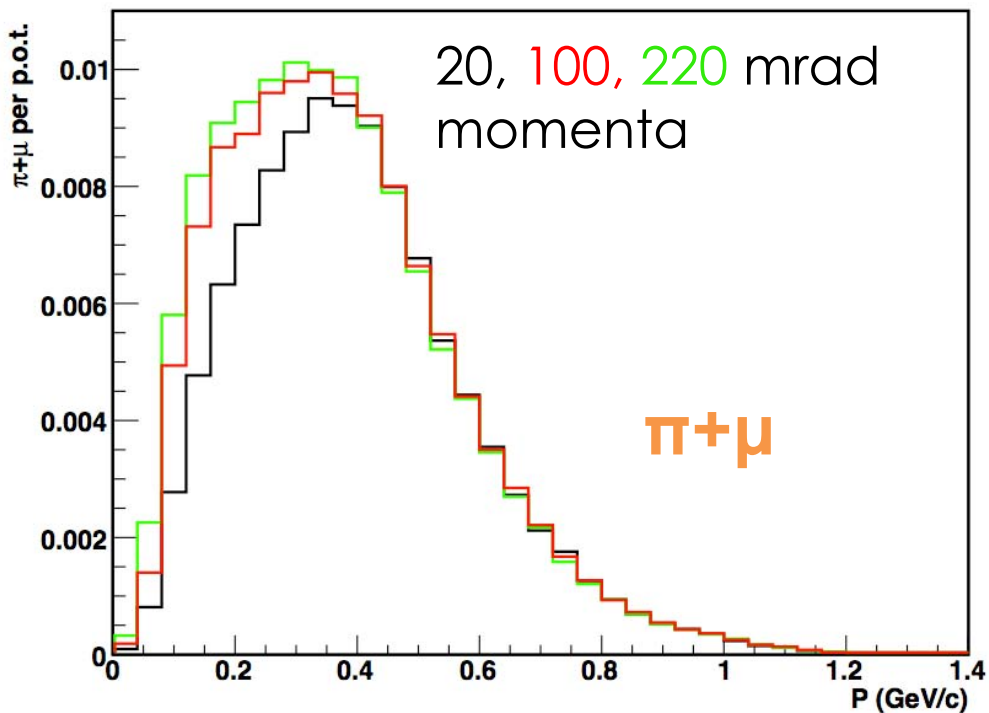
selection in red

- pions $0.222 < P \text{ (GeV/c)} < 0.776$
- muons $0.111 < P \text{ (GeV/c)} < 0.438$

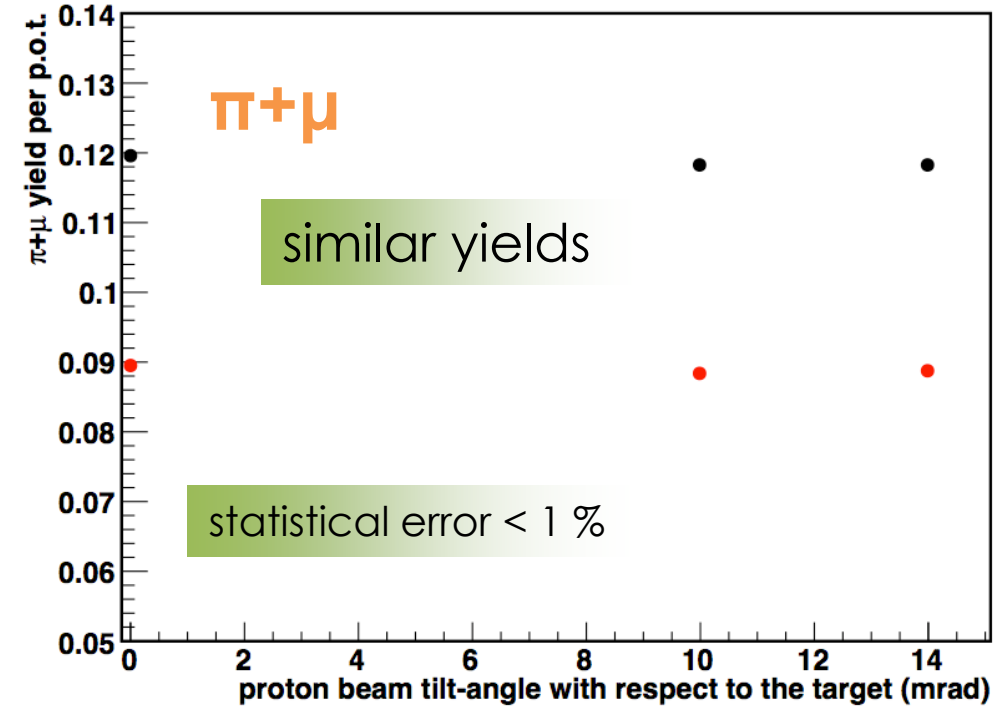
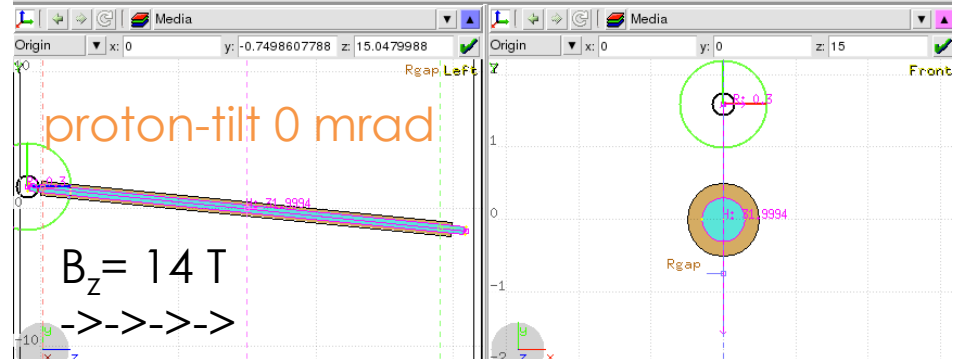
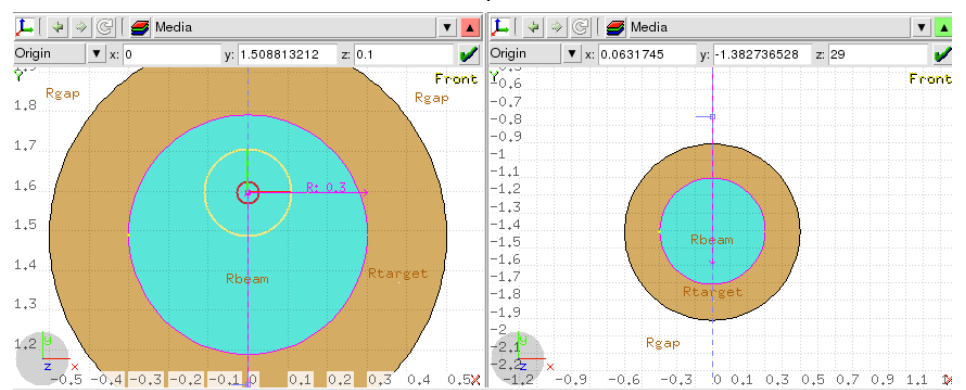
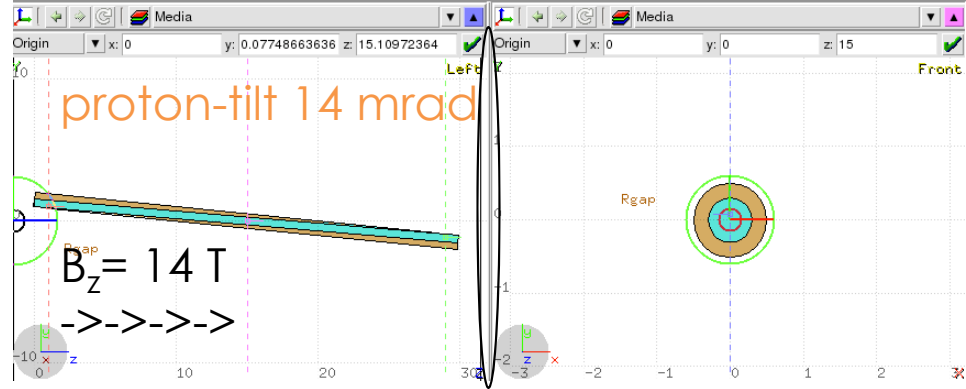
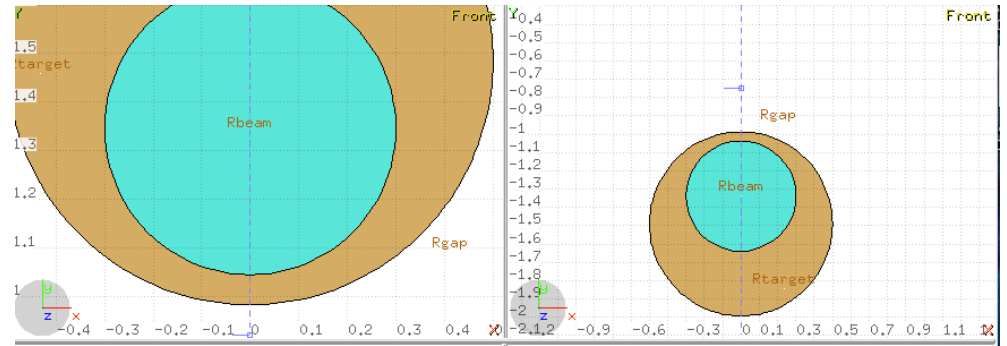
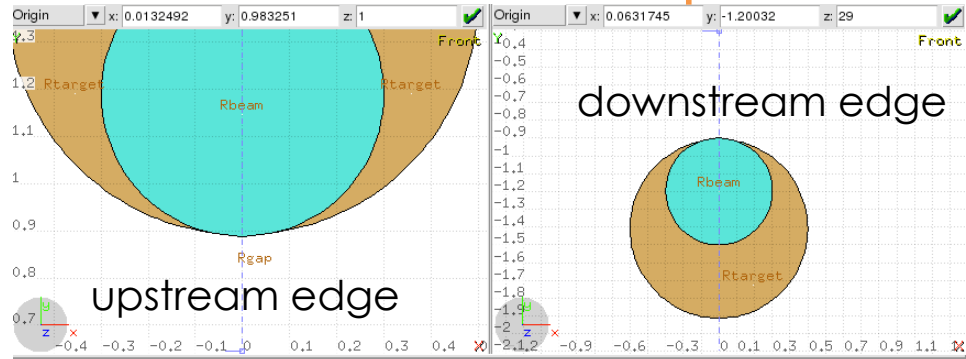
statistical error $< 1\%$

write the % of pi & mu



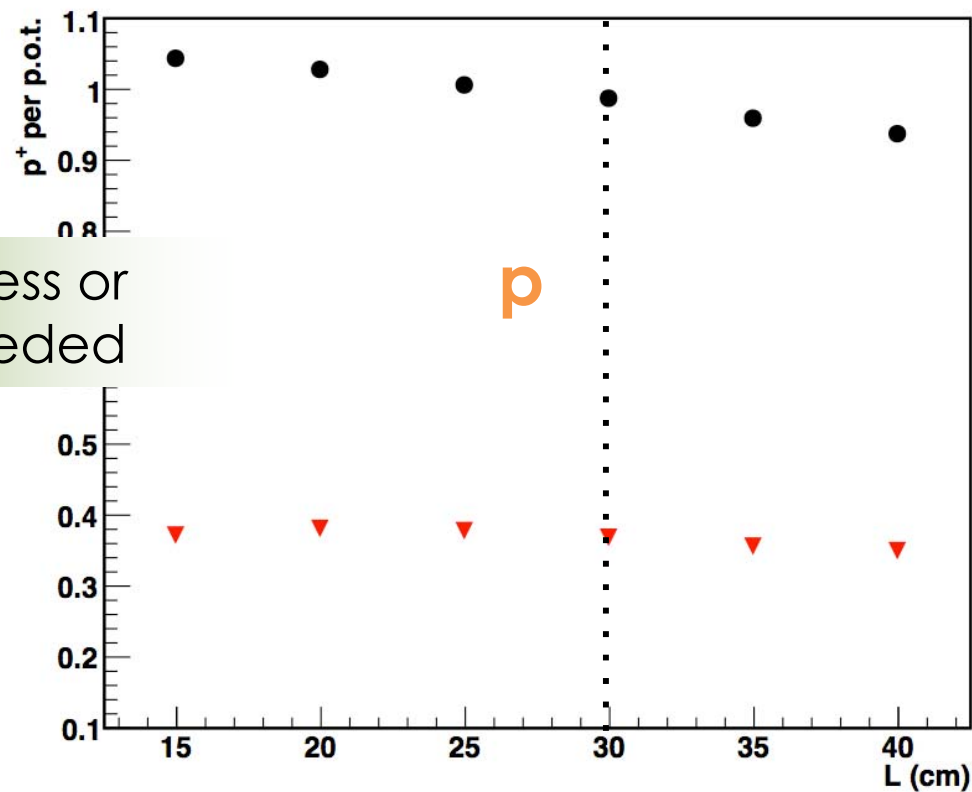
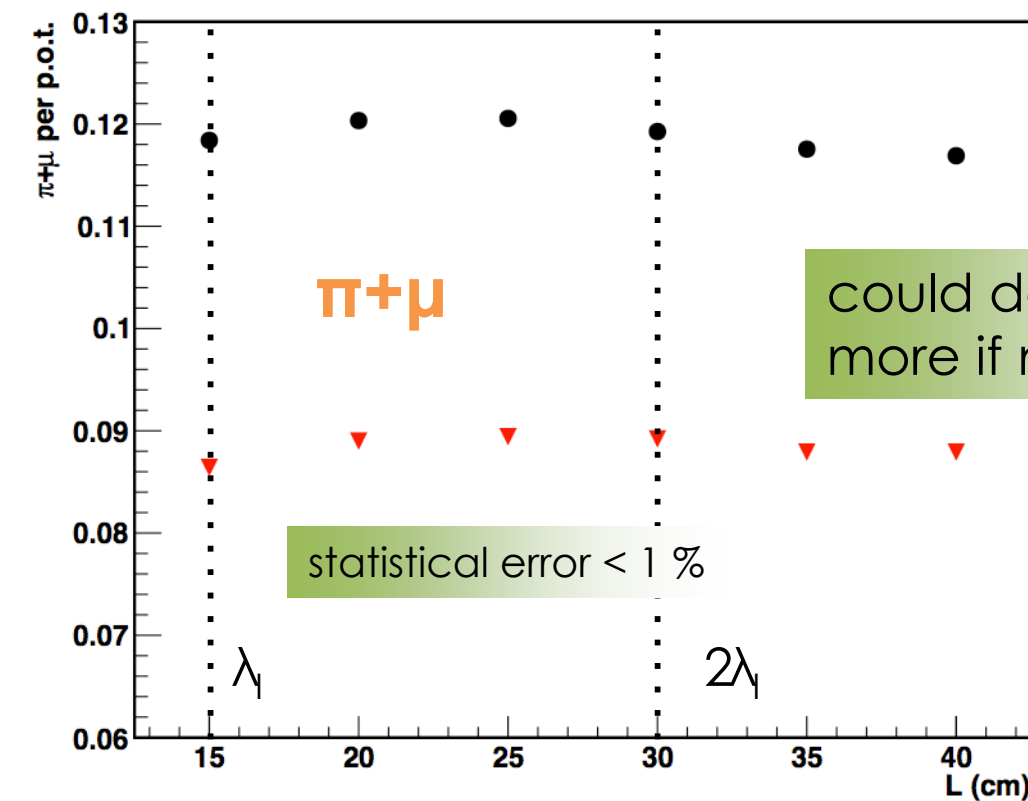
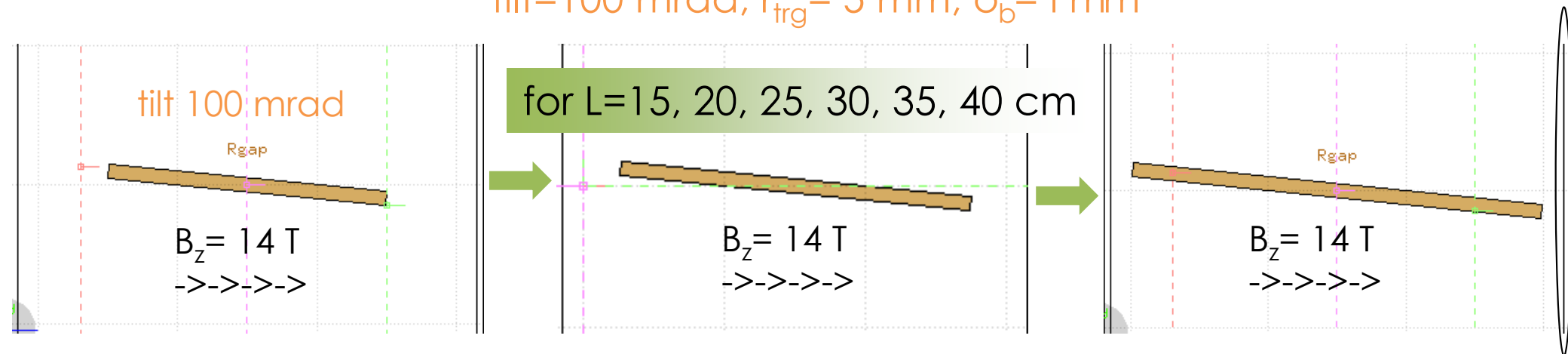


beam tilt with respect to the target



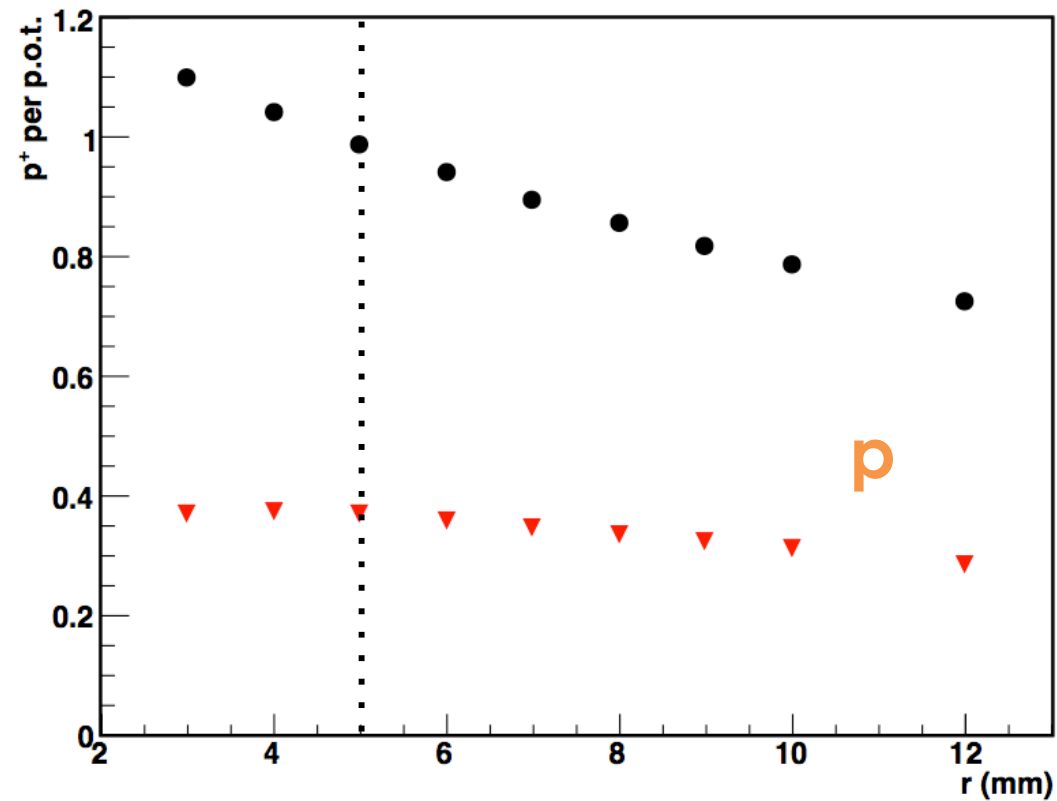
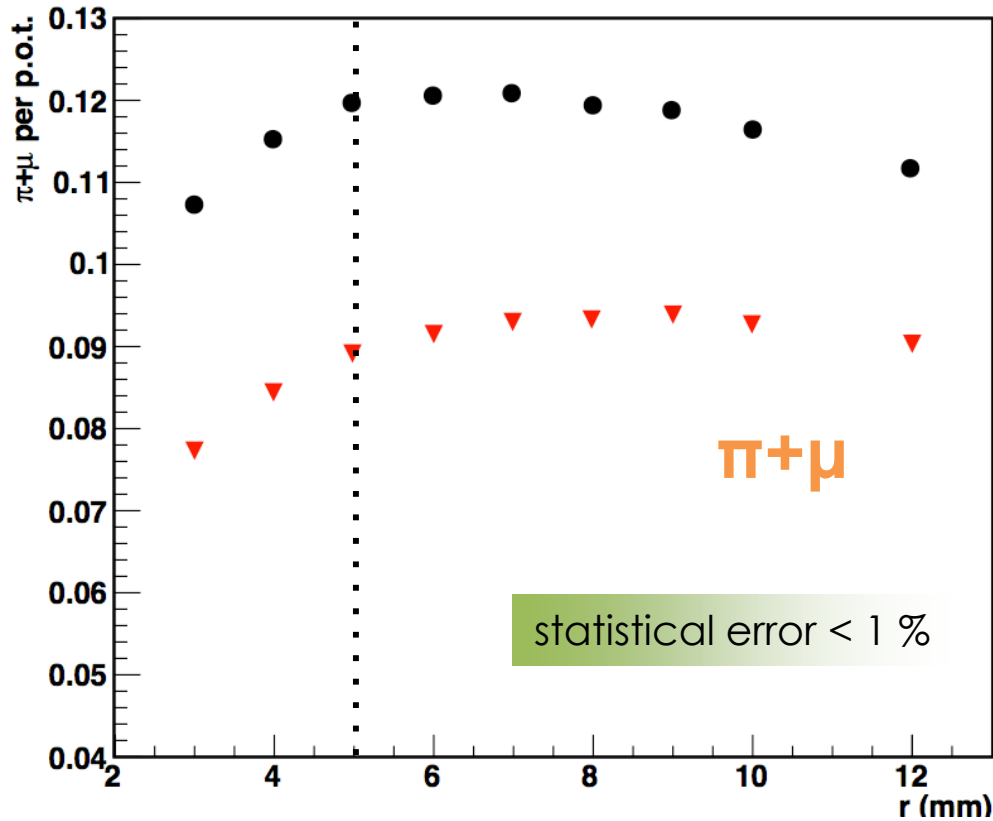
particle yields at the edge of MCS for different target lengths

tilt=100 mrad, $r_{trg} = 5$ mm, $\sigma_b = 1$ mm



particle yields at the edge of MCS for different radii

tilt=100 mrad, $L_{\text{trg}}=30$ cm, $\sigma_b=1$ mm

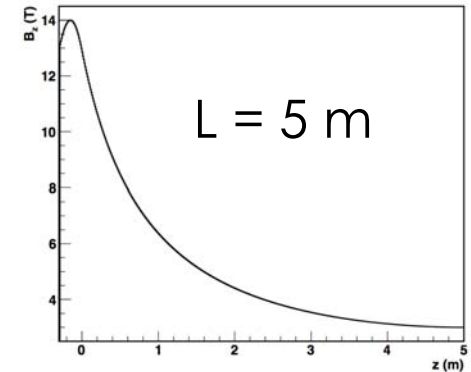
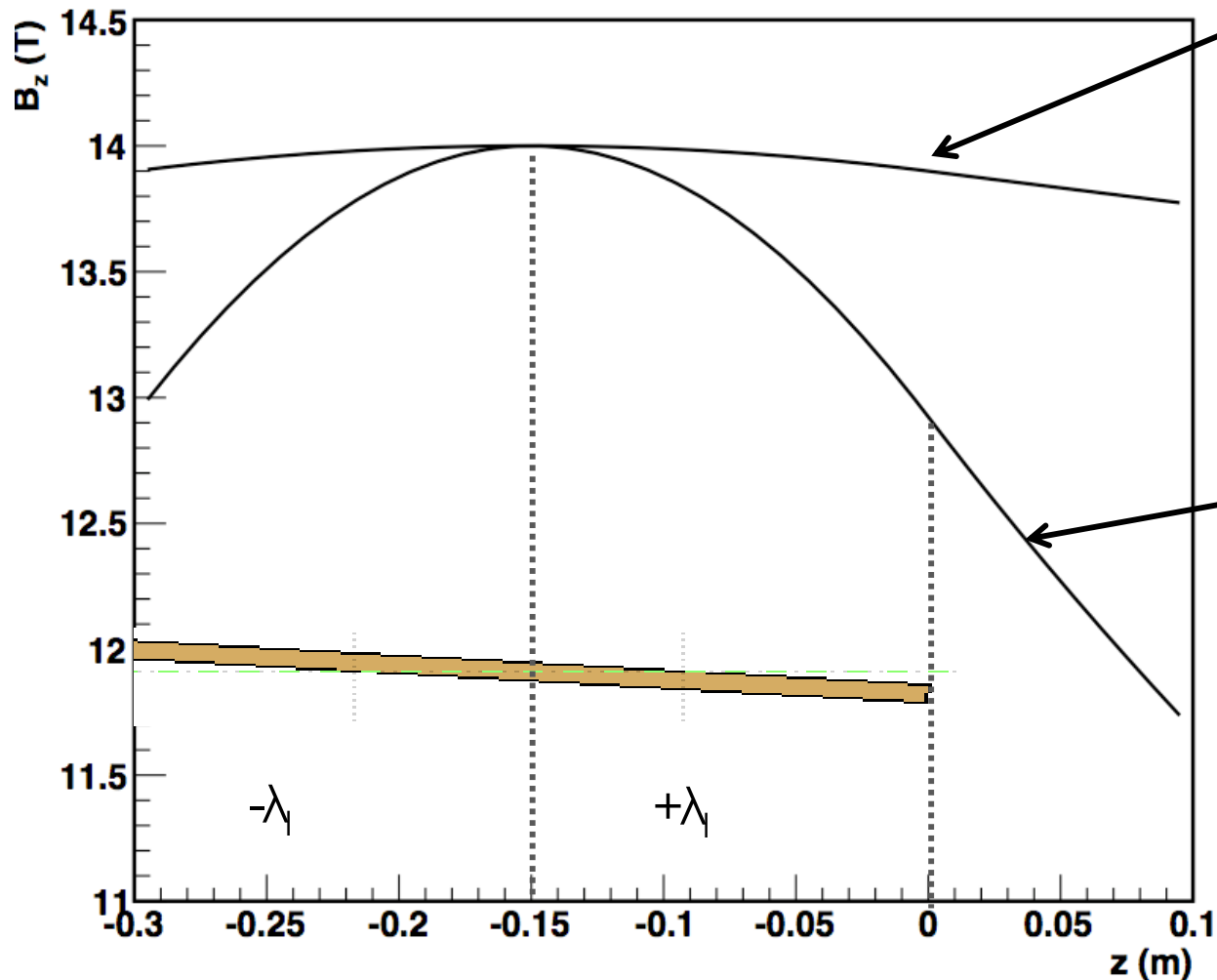


could do more in radius if needed

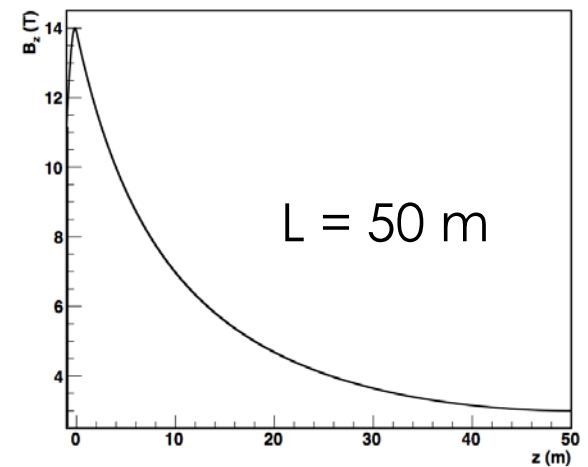


from ideal to Gaussian field for MCS

field as used in MOMENT studies,
0.8% reduction within $\pm\lambda_1$



gaussian $-0.3 \text{ m} < z < 0.3 \text{ m}$
7% reduction within $\pm\lambda_1$



$$B_z(0, z) = B_0 e^{-(z-z_0)^2/2\sigma^2}$$

$$B_0 = 14T, z_0 = -15cm$$

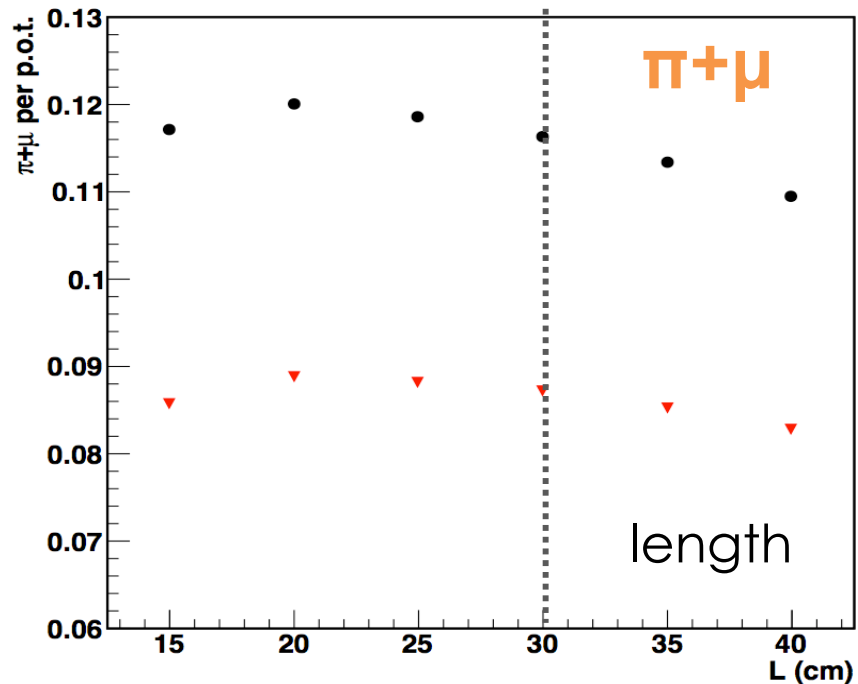
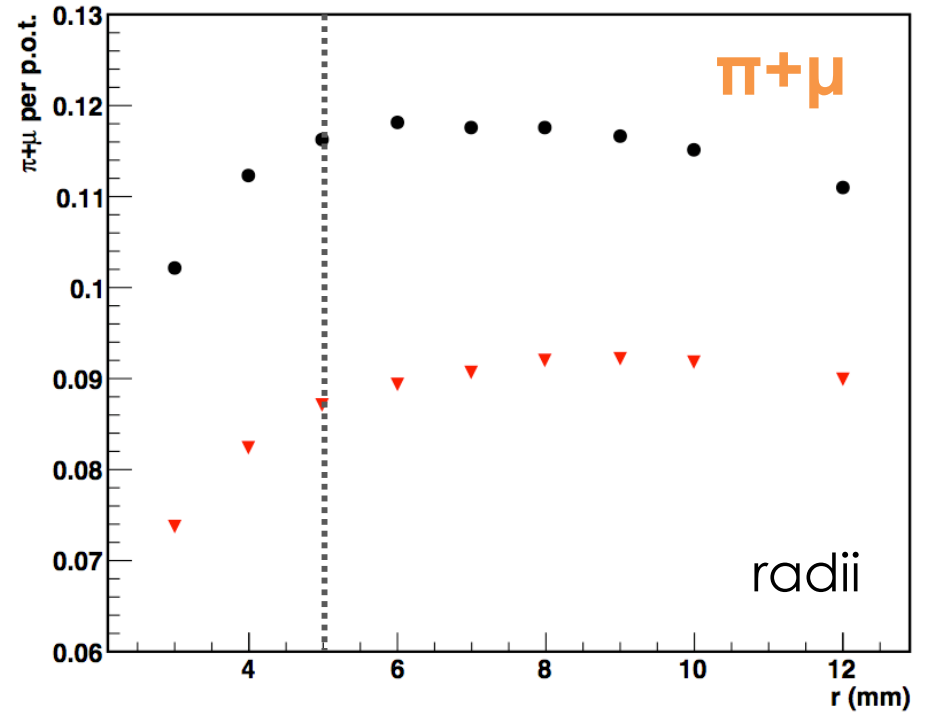
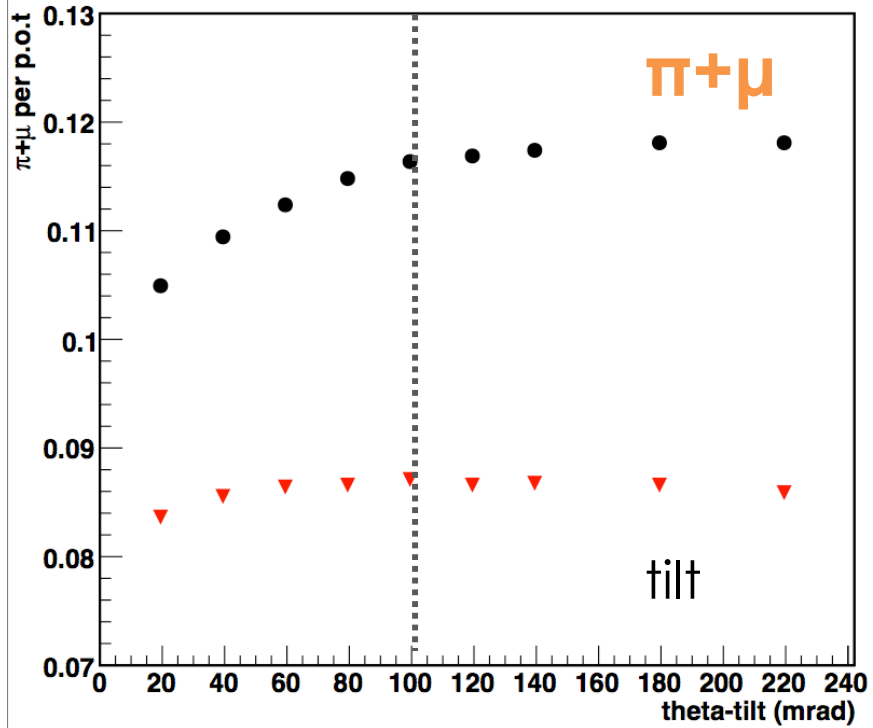
$$B_z(r, z) \approx B_z(0, z)$$

$$B_r(r, z) \approx -\frac{r}{2} * \frac{\partial B_z(0, z)}{\partial z}$$

particle yields at the edge of MCS
for different target parameters

fixed parameters : tilt=100 mrad or $L_{trg}=30 \text{ cm}$ or $r_{trg}=5mm$





all momenta in black

selection in red

• pions $0.222 < P \text{ (GeV/c)} < 0.776$

• muons $0.111 < P \text{ (GeV/c)} < 0.438$

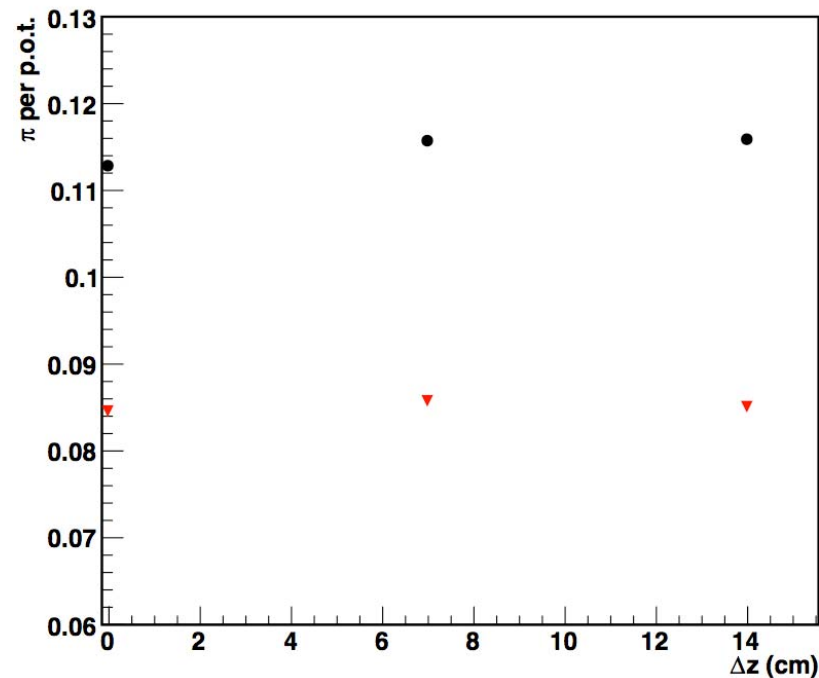
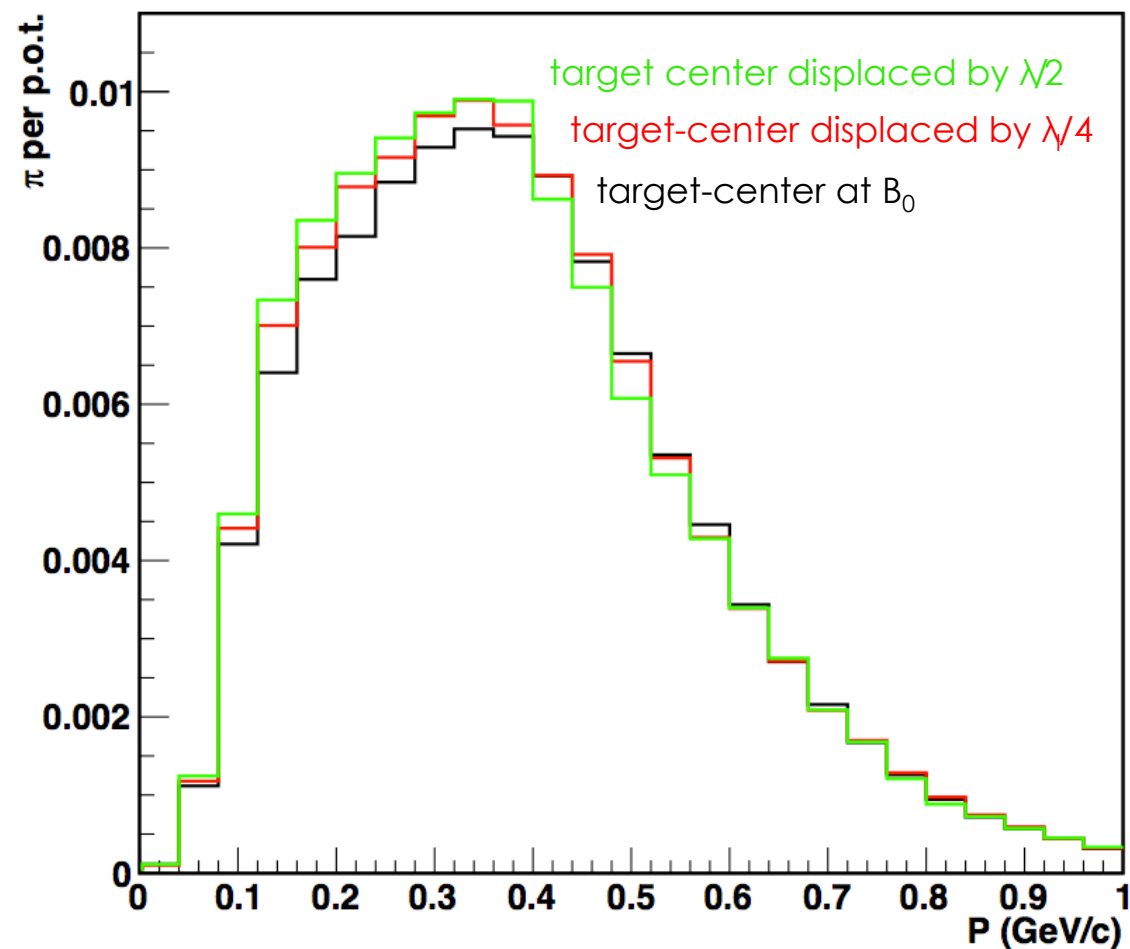
statistical error $< 1 \%$

similar results to the ideal field $B_0 = 14 \text{ T}$



target displacement at MCS

target-center displaced by $\lambda_1/2, \lambda_1$
with respect to B_0
 $r_{MCS} : 20 \text{ cm}$

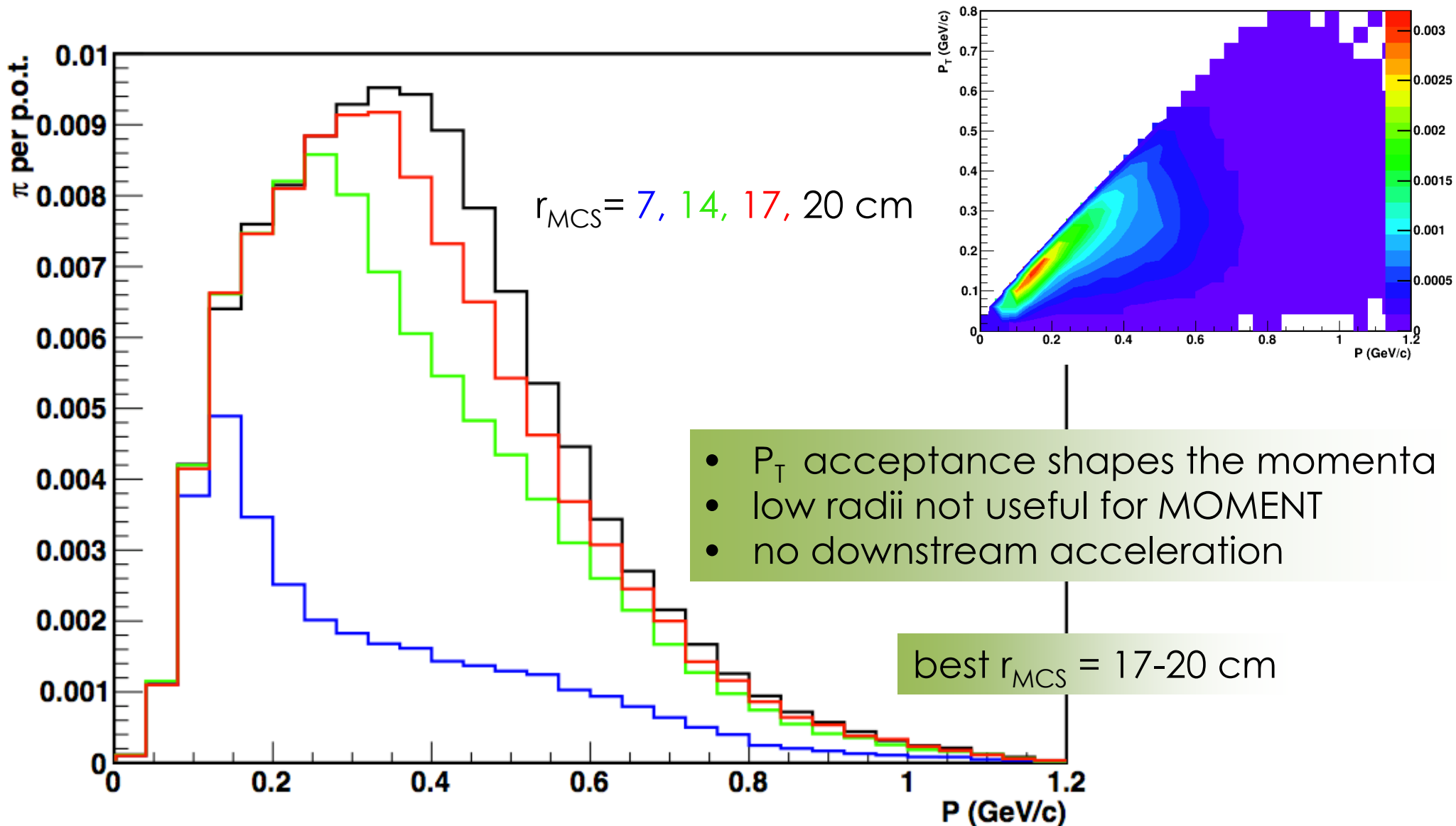


similar yields

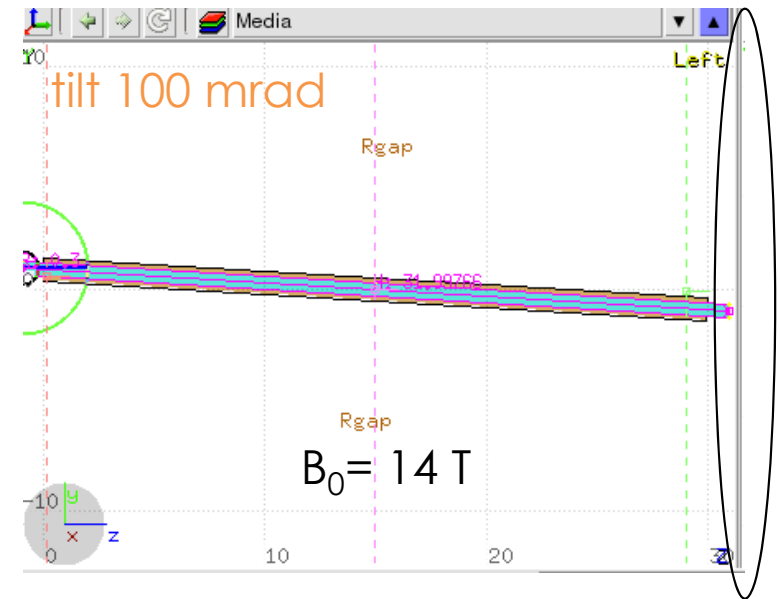


MCS radius

- $L_{hg}=30$ cm, $r_{hg}=0.5$ cm, $\text{tilt}_{hg}=100$ mrad
- $L_{MCS}=32$ cm, $r_{MCS}=7, 14, 30$ cm, $B_0=14$ T, gaussian $\sigma=45$ cm



conclusions for the MCS



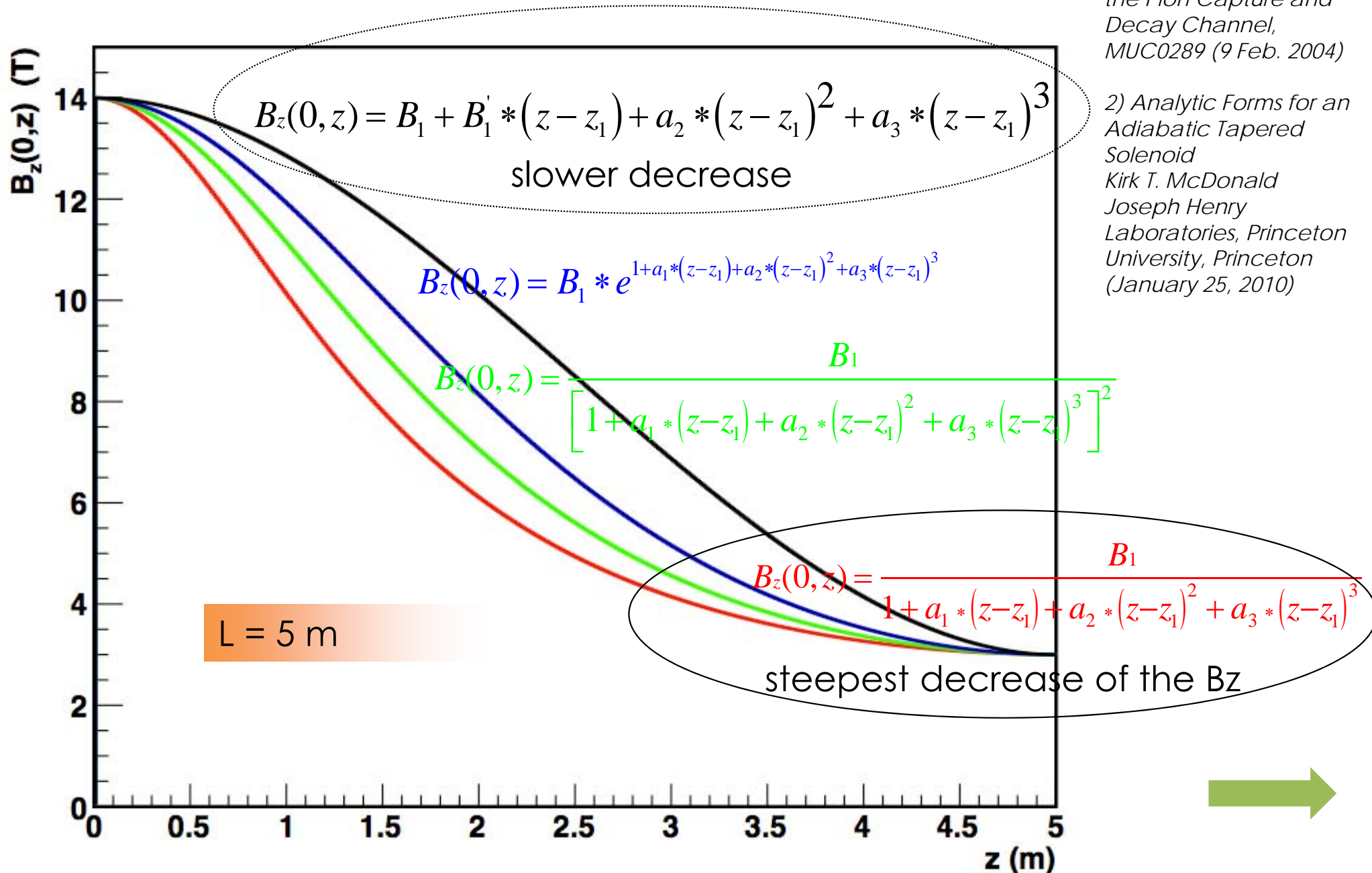
at MCS edge:

- target-tilt could be more than 100 mrad
- target-length, yield is maximal at 2 interaction lengths or slightly less
- target-radius could be increased more than 5 mm for $\sigma_b=0.1$ cm
- yield remains similar when proton beam-axis tilted with respect to the target-axis -> to be studied with higher angles between the two
- high energy protons could be separated (see Cai's talk)
- MCS radii should be ~ 17 -20 cm

adiabatic transport solenoids

1) K. Paul and C. Johnstone, *Optimizing the Pion Capture and Decay Channel*, MUC0289 (9 Feb. 2004)

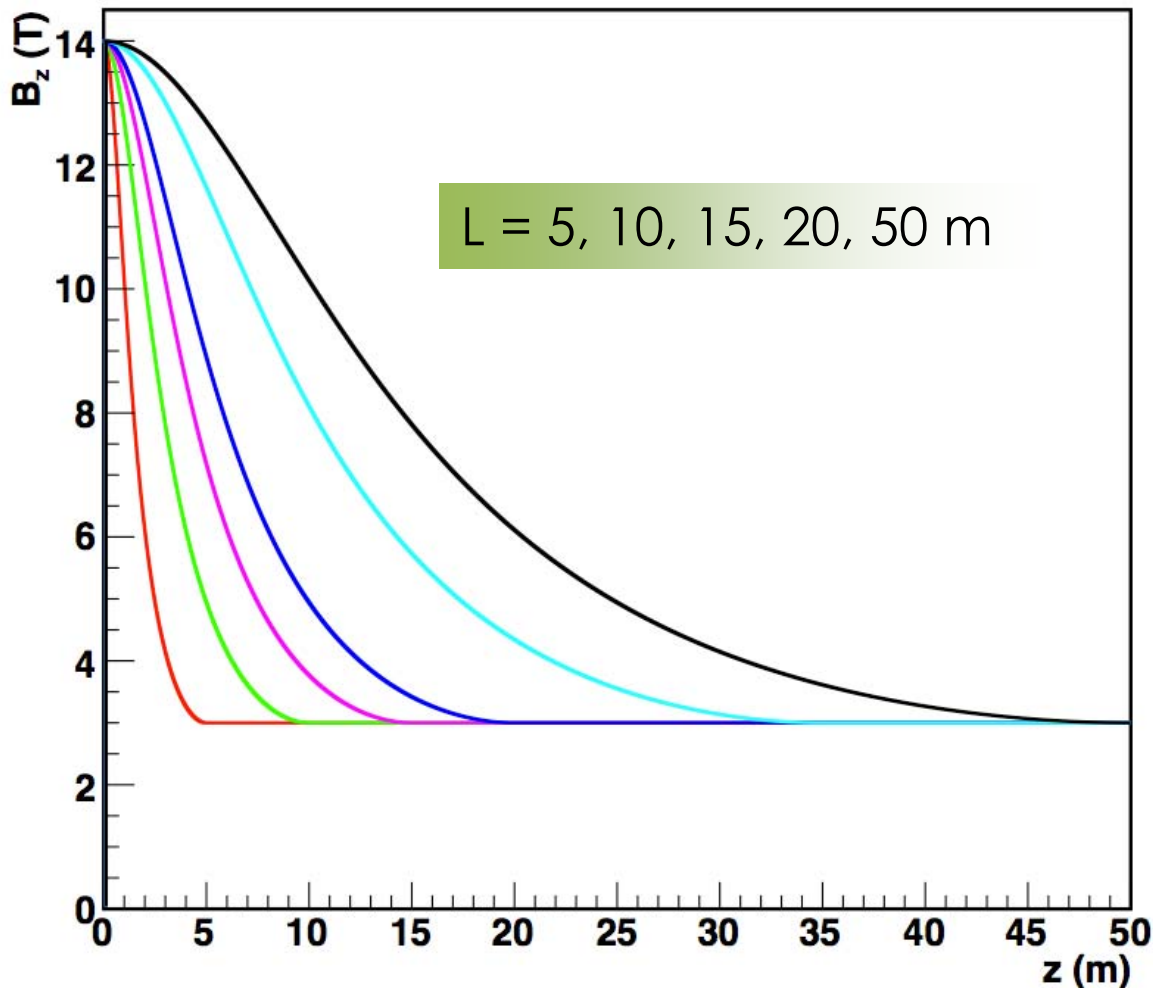
2) *Analytic Forms for an Adiabatic Tapered Solenoid*
Kirk T. McDonald
Joseph Henry
Laboratories, Princeton
University, Princeton
(January 25, 2010)



adiabatic inverse taper – 1st degree

(ideal field, steeper field-decrease response)

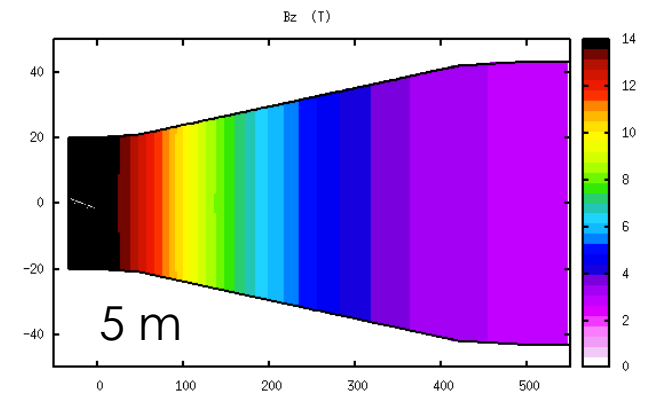
$$B_z(0, z) = \frac{B_1}{1 + a_1 * (z - z_1) + a_2 * (z - z_1)^2 + a_3 * (z - z_1)^3}$$



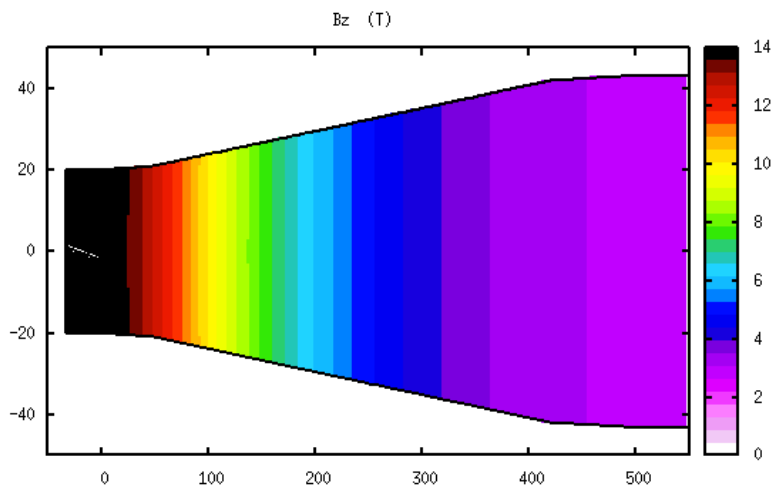
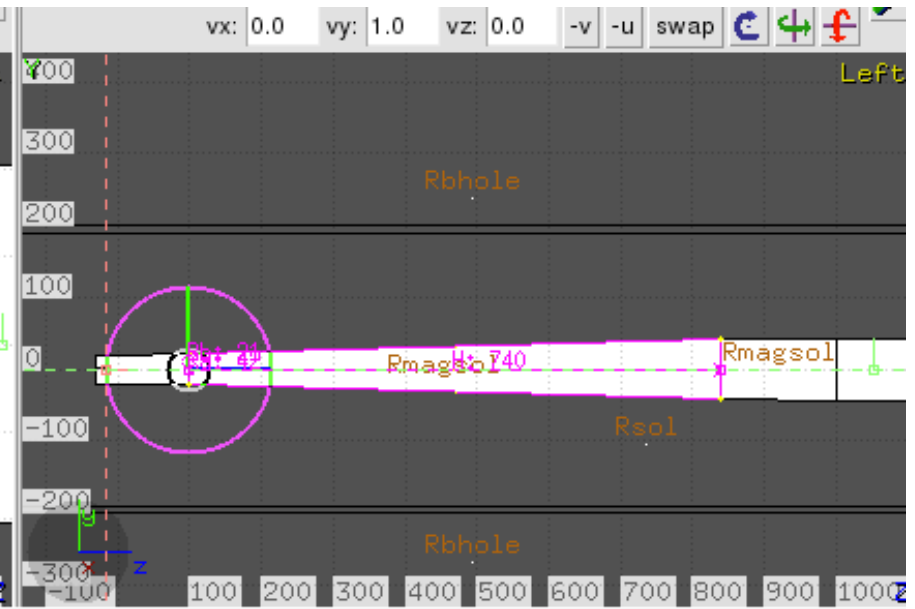
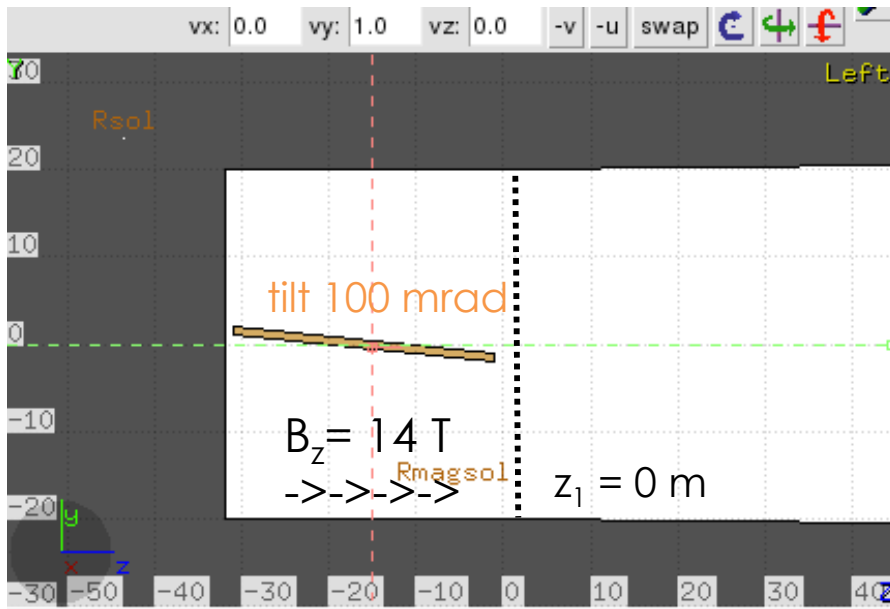
field approximation
implemented in FLUKA:

$$B_z(r, z) \approx B_z(0, z)$$

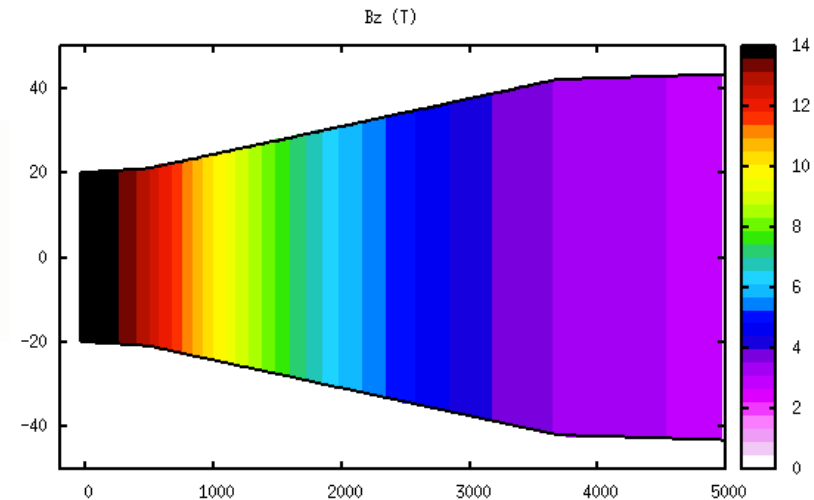
$$B_r(r, z) \approx -\frac{r}{2} * \frac{\partial B_z(0, z)}{\partial z}$$



ideal MCS + $B_z(0, z) = \frac{B_1}{1 + a_1 * (z - z_1) + a_2 * (z - z_1)^2 + a_3 * (z - z_1)^3}$



@ $z_1 = 0$ m
 $r_1 = 20$ cm, $B_1 = 14$ T
 @ $z_2 = 5 \rightarrow 50$ m
 $r_2 = 43.2$ cm, $B_2 = 3$ T



yields at the end of the adiabatic section vs length

all momenta in black

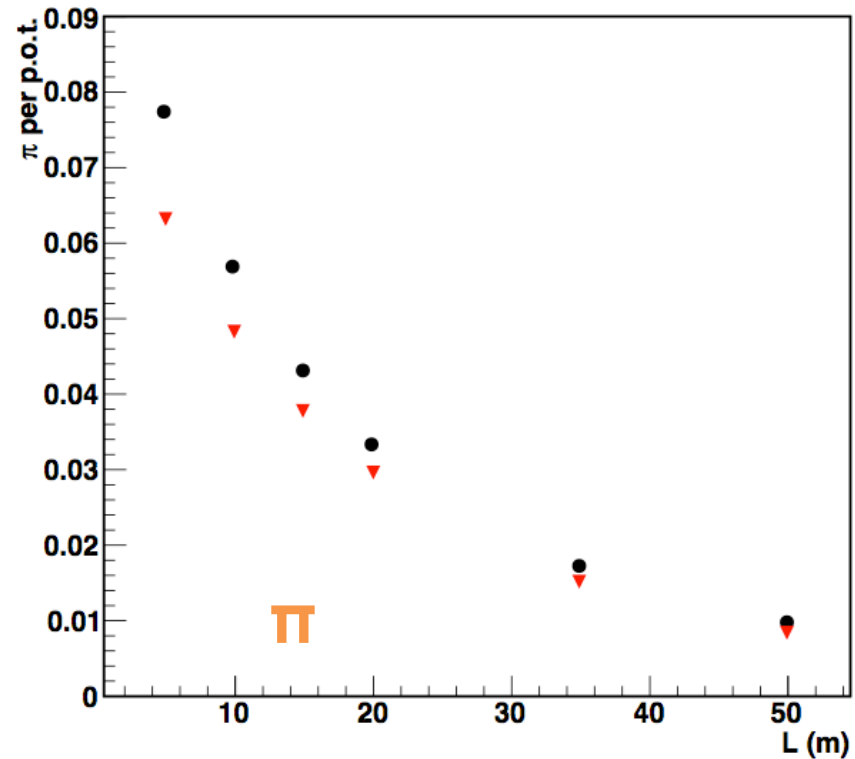
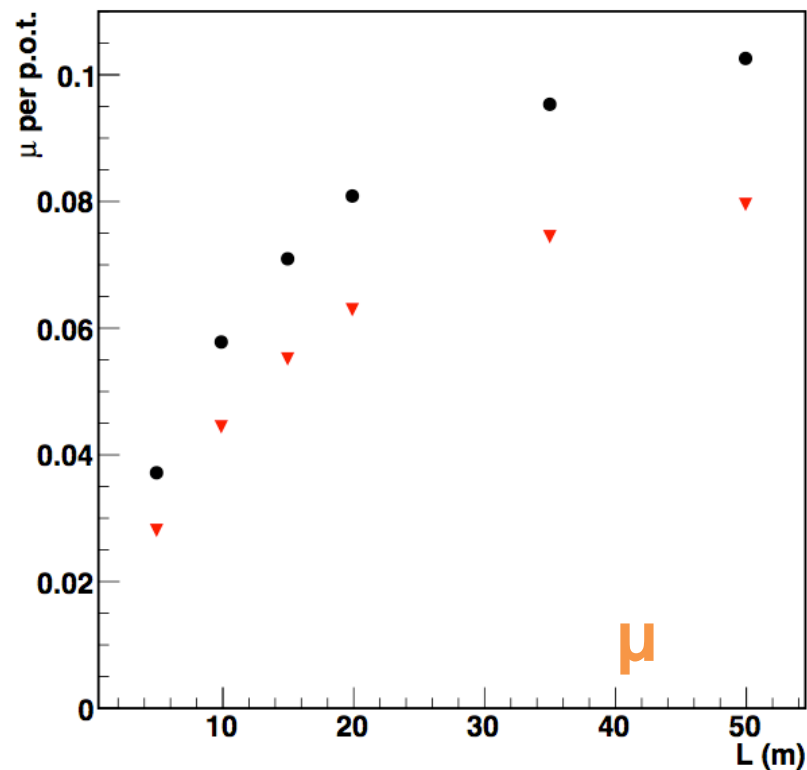
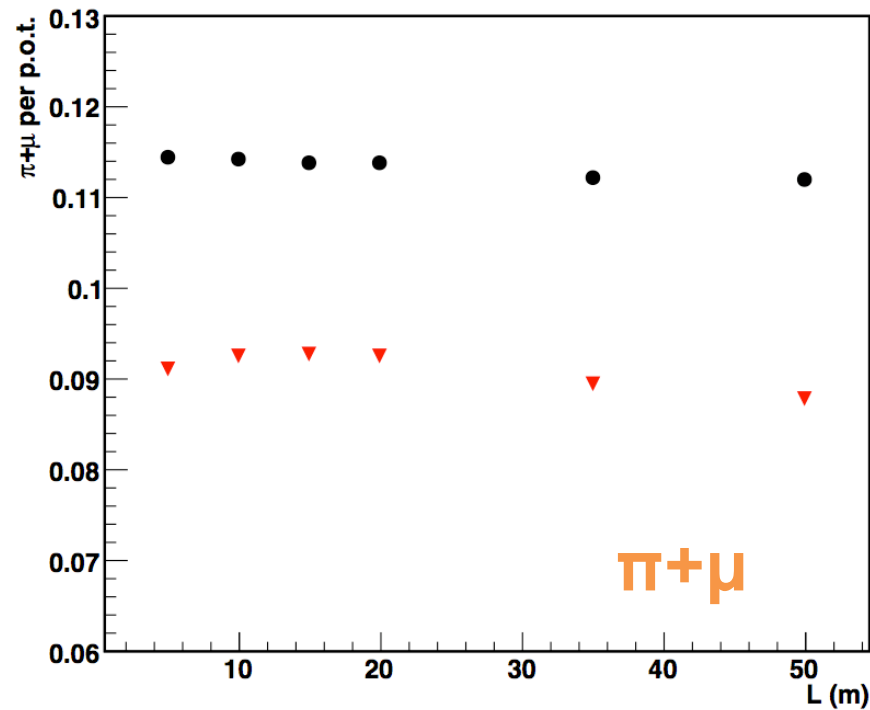
selection in red

• pions $0.222 < P \text{ (GeV/c)} < 0.776$

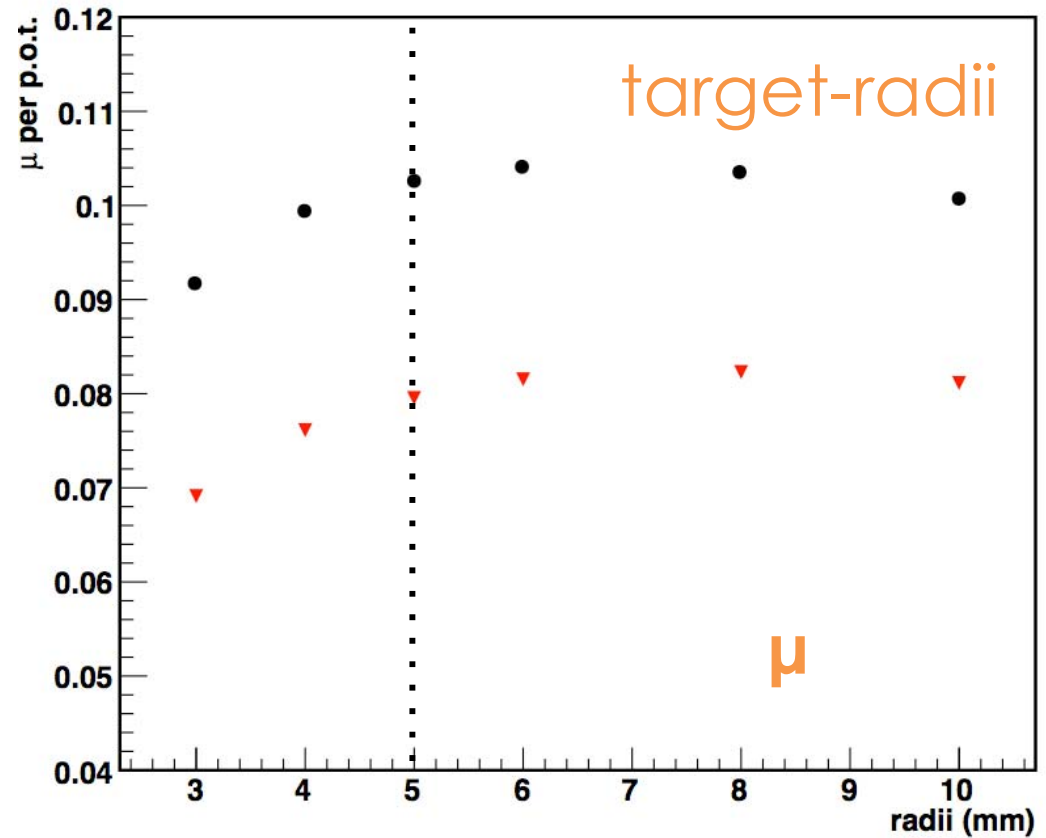
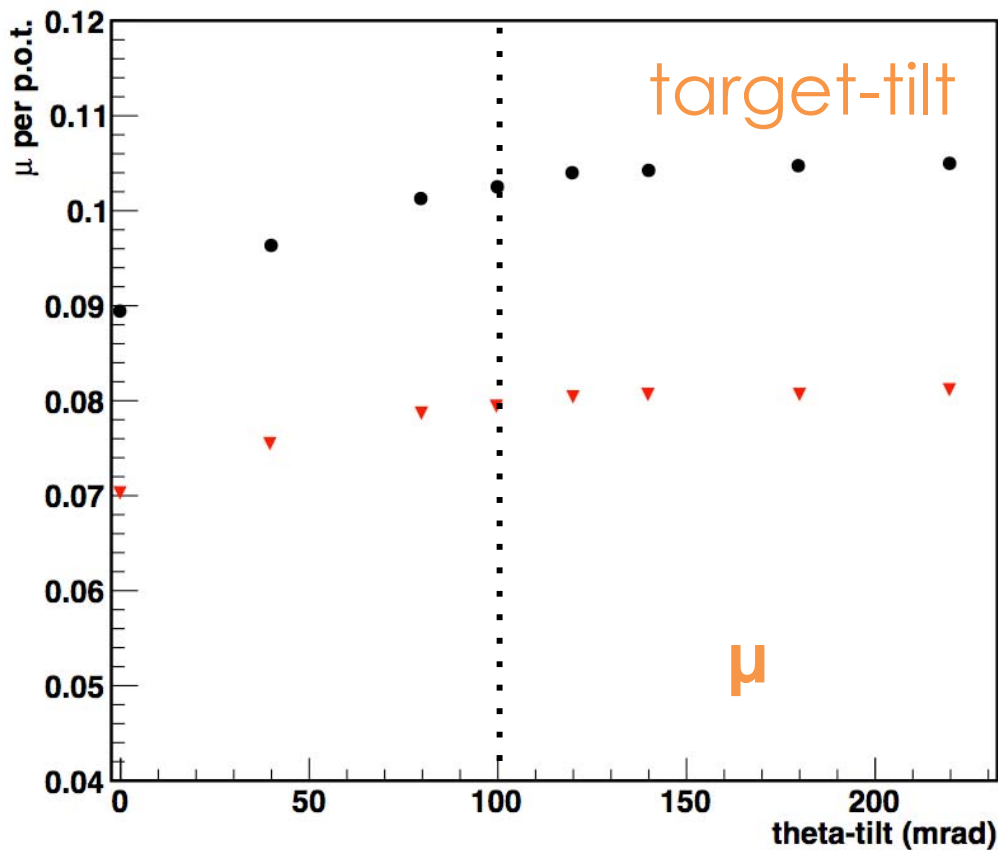
• muons $0.111 < P \text{ (GeV/c)} < 0.438$

statistical error $< 1 \%$

geometry approximation systematic error



muon yields for inverse taper L = 50 m vs different target-tilts, radii



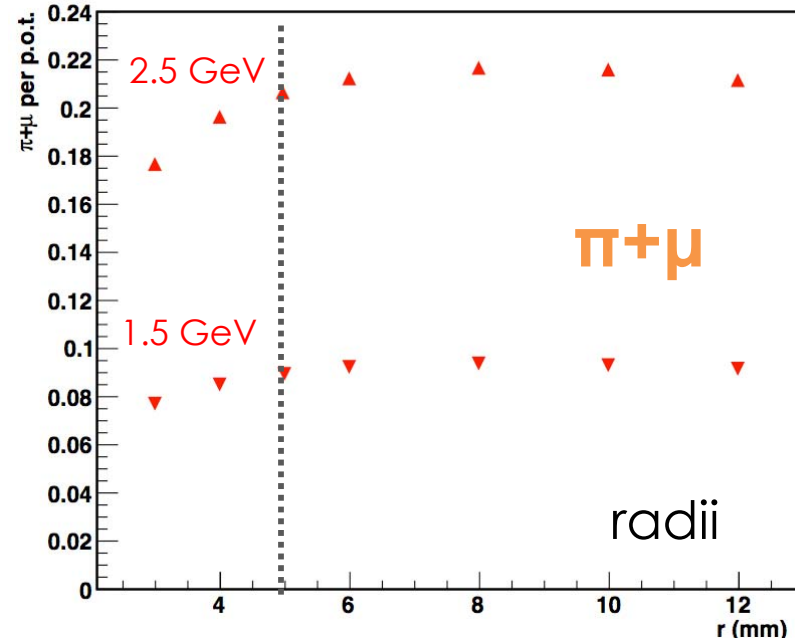
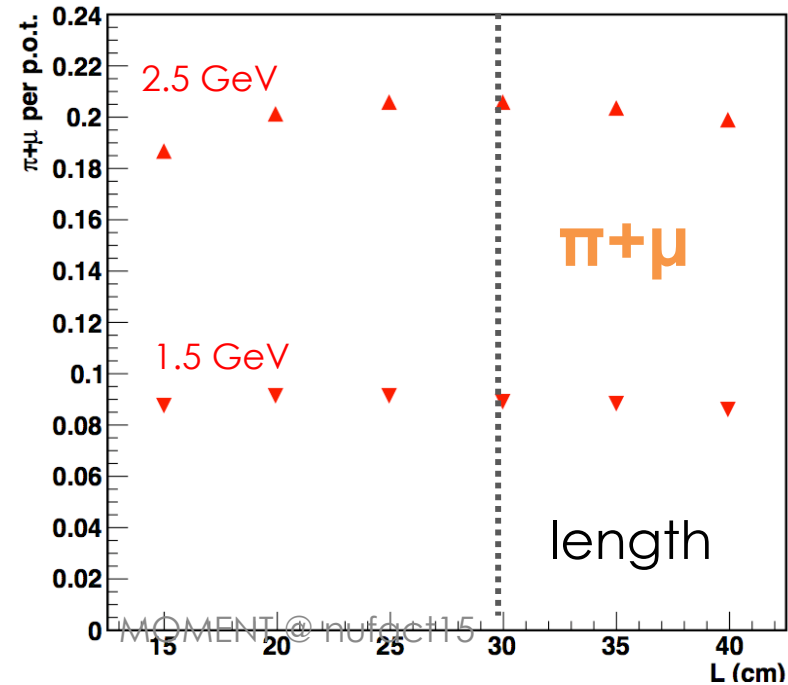
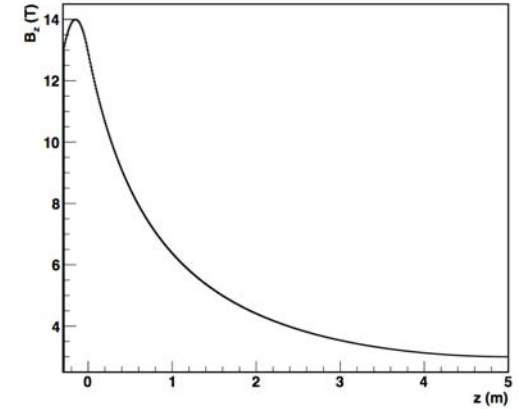
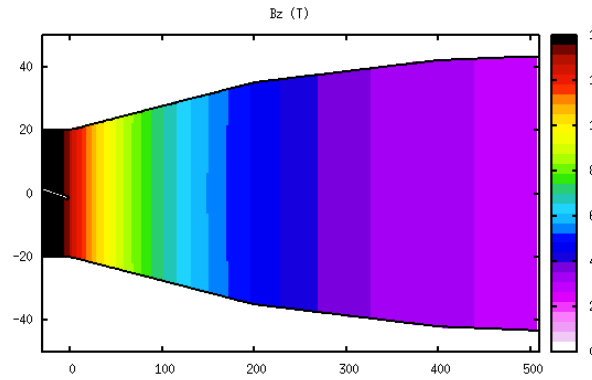
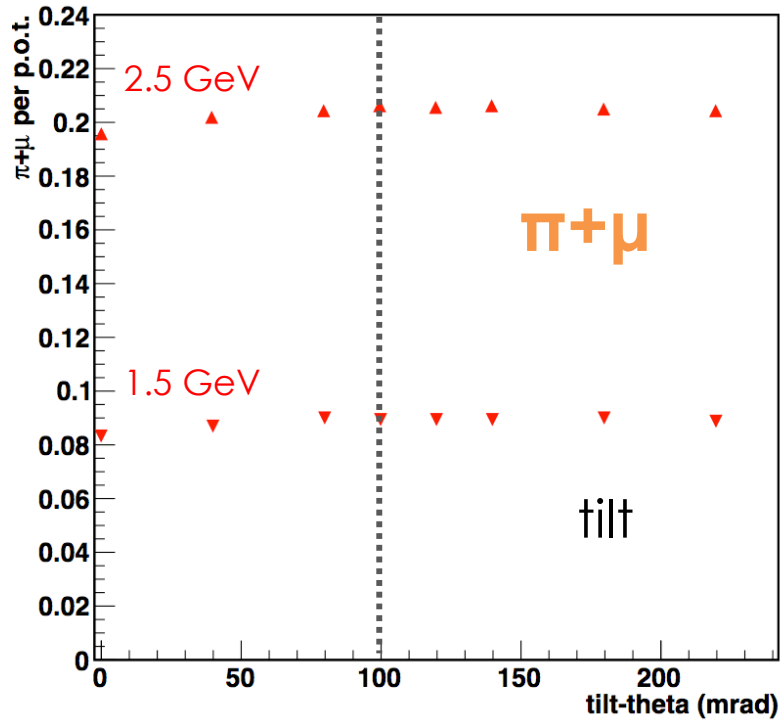
- tilt: plateau after 100 mrad
- radii: could do more

statistical error < 1 %

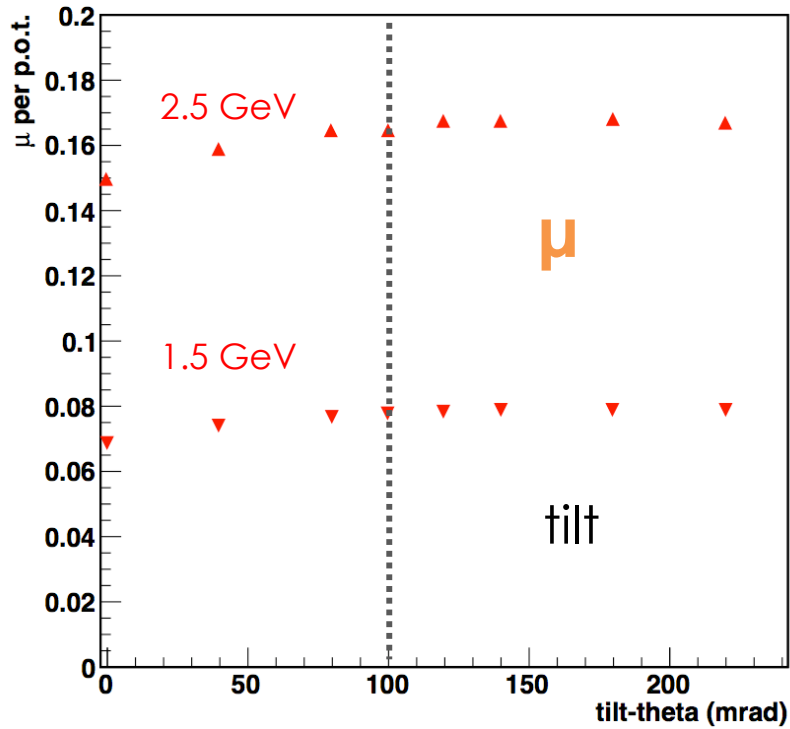
particle yields for $L_{\text{taper}}=5\text{ m}$, $E_k = 1.5, 2.5\text{ GeV}$

$$B_z(0,z) = B_0 e^{-(z-z_0)^2/2\sigma^2} + B_z(0,z) = \frac{B_1}{1 + a_1 * (z-z_1) + a_2 * (z-z_1)^2 + a_3 * (z-z_1)^3}$$

$$B_0 = 14\text{T}, z_0 = -15\text{cm}$$

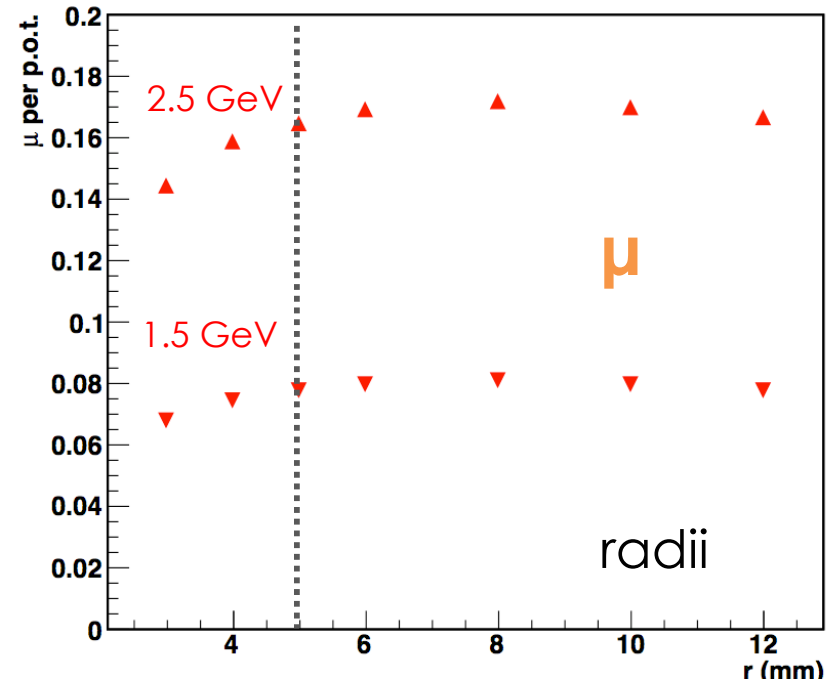
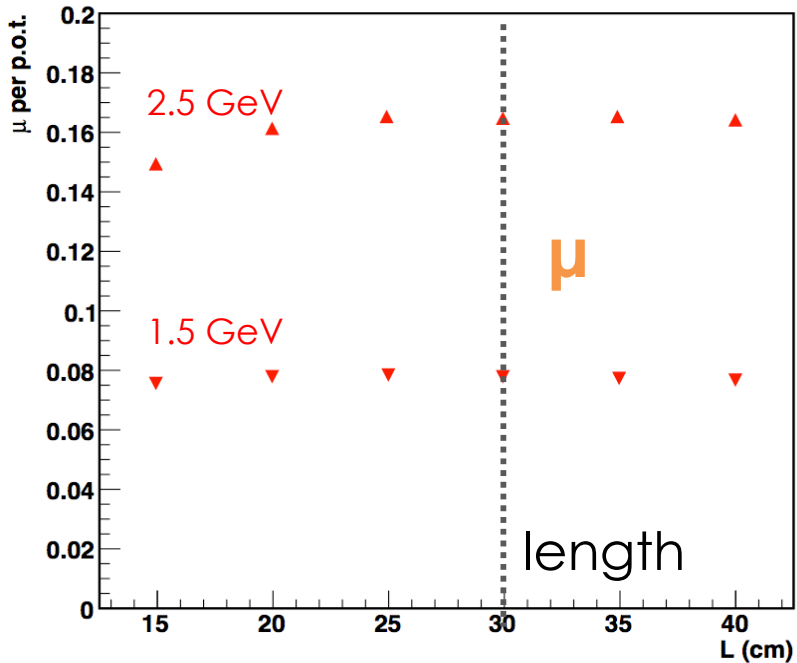
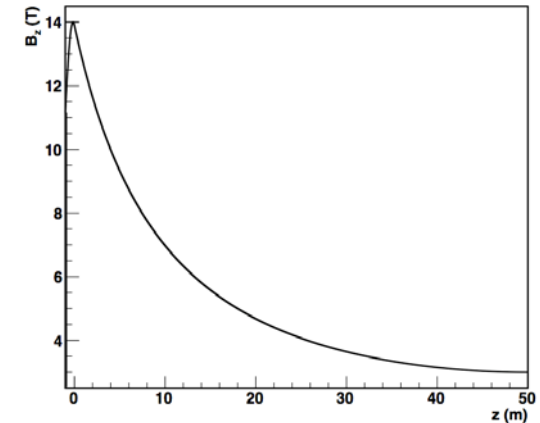
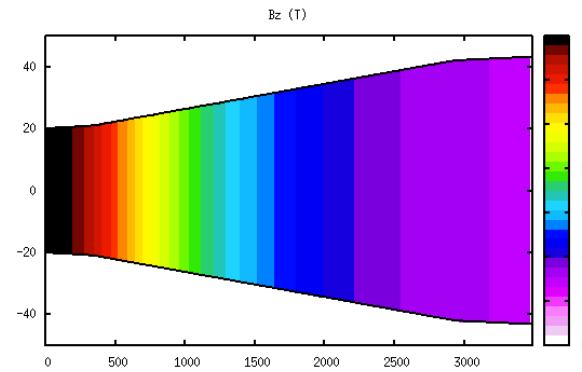


particle yields for $L_{\text{taper}} = 50 \text{ m}$, $E_k = 1.5, 2.5 \text{ GeV}$

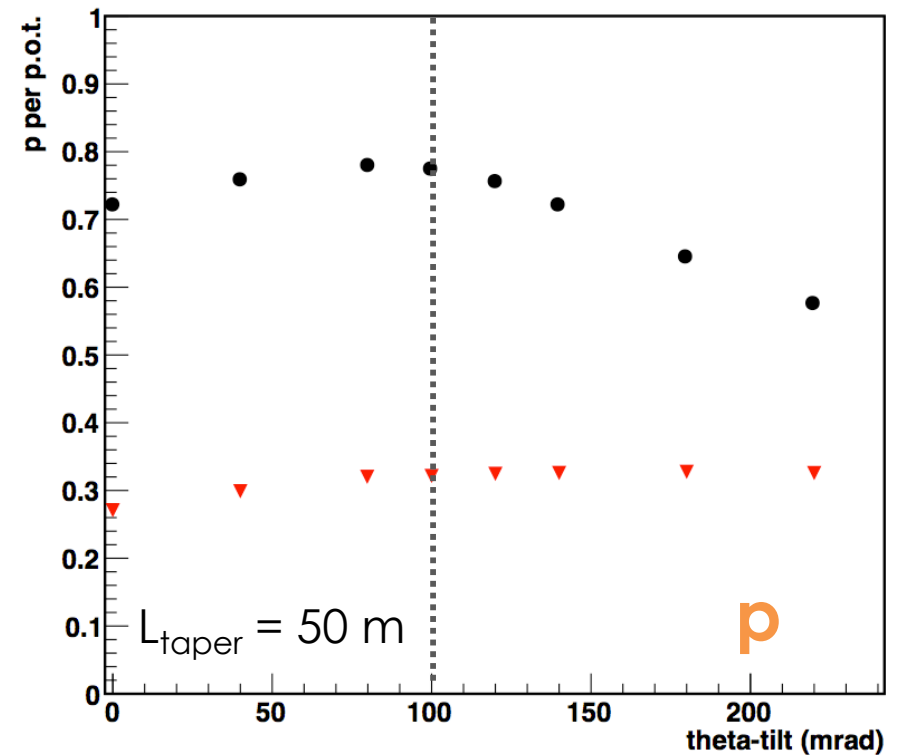
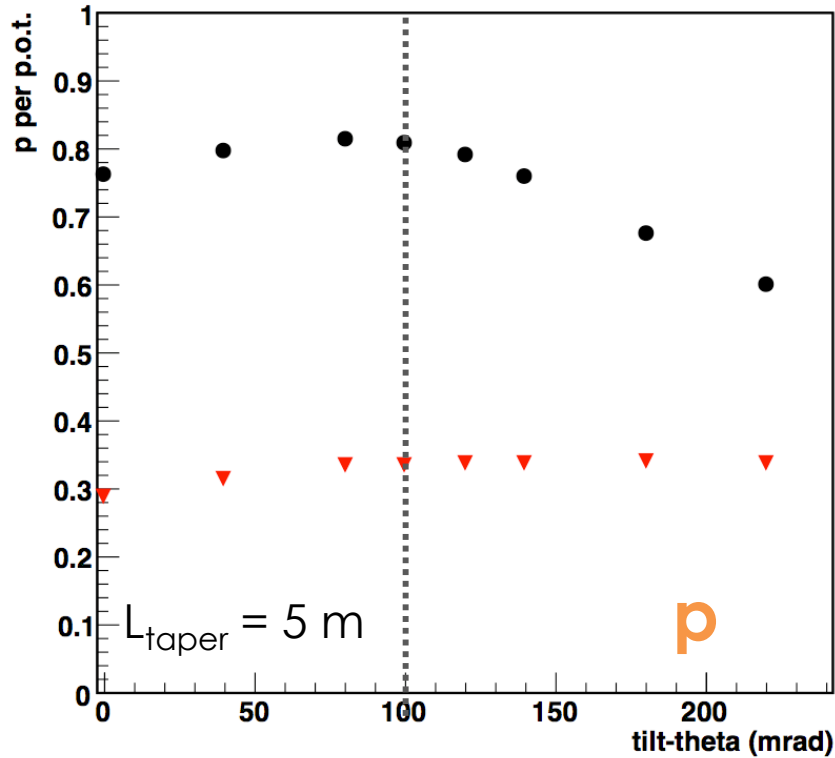


$$B_z(0, z) = B_0 e^{-(z-z_0)^2/2\sigma^2} + B_z(0, z) = \frac{B_1}{1 + a_1 * (z-z_1) + a_2 * (z-z_1)^2 + a_3 * (z-z_1)^3}$$

$$B_0 = 14T, z_0 = -15cm$$



proton yields for different target-tilts and tapers



all momenta in black

selection in red

• proton $0.222 < P \text{ (GeV/c)} < 0.776$

statistical error $< 1 \%$

there is a reduction of higher momentum protons with the tilt

conclusion/further studies

for 5, 50 m gaussian + 1st degree inverse adiabatic solenoid:

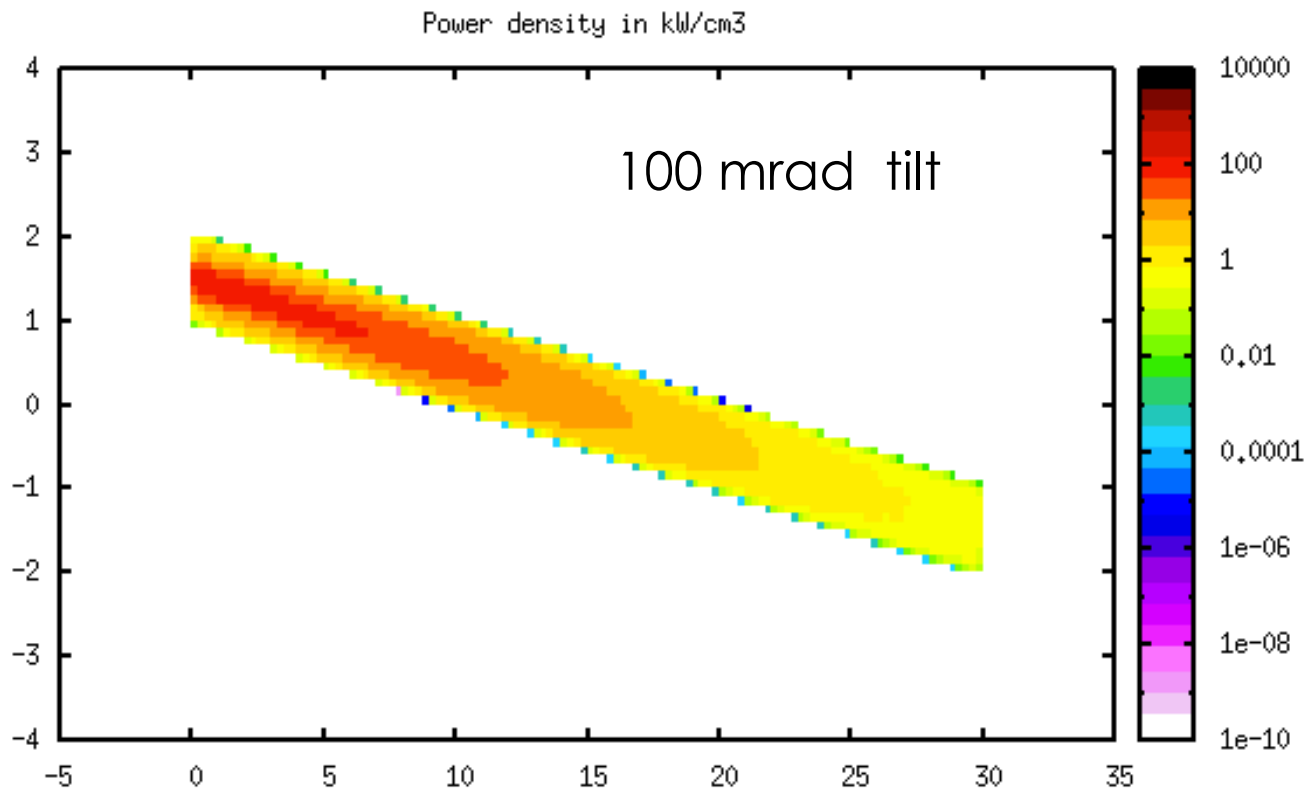
- target-tilt 100 mrad or more
- target-length 25 cm or more
- target-radius 5 mm or more
- higher momentum protons yields decreases with larger target-tilts
- proton $E_k = 2.5$ GeV doubles the yields

next:

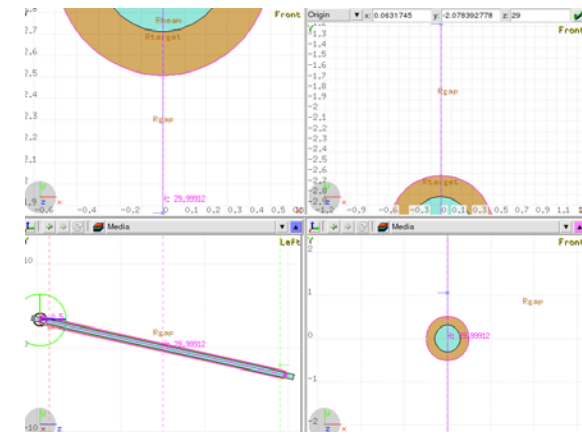
- test the cubic field “slower decrease of the field” (similar results expected)
- test with a different MC (geant4, MARS) to compare the yield patterns and their absolute values

Thanks

Power on target

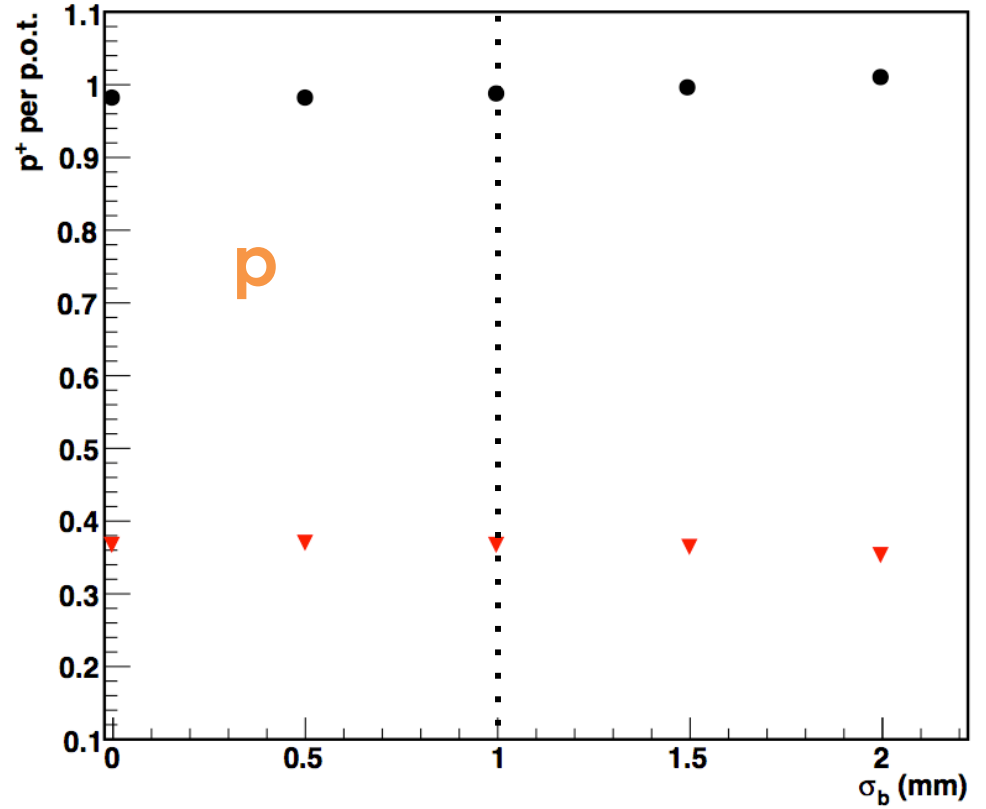
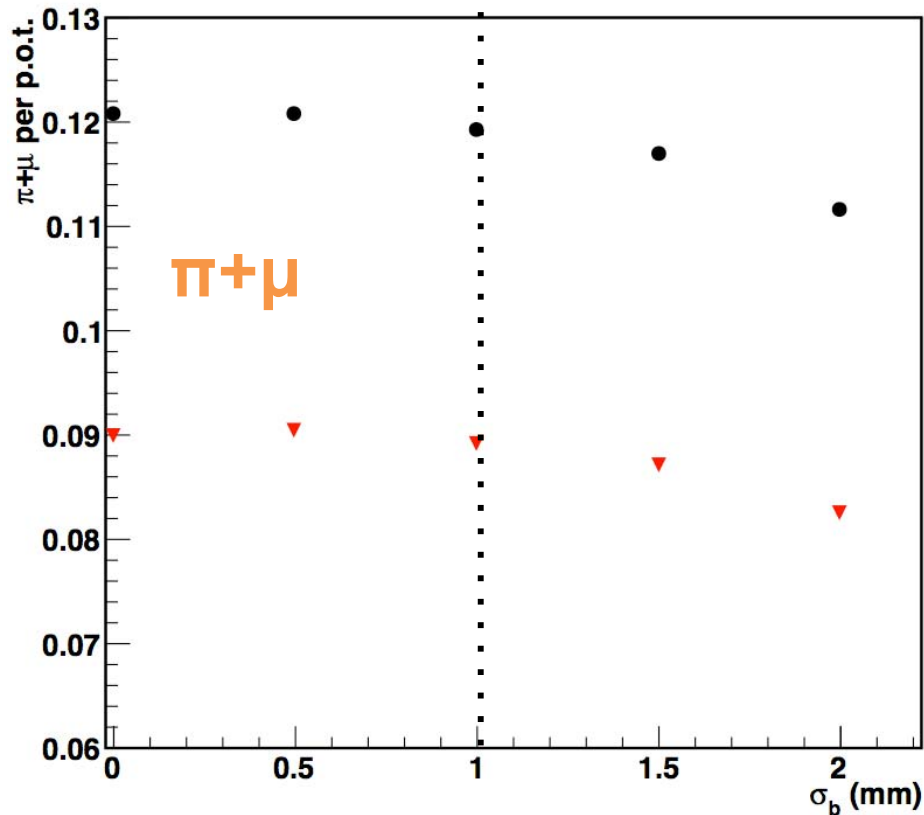


$$P_{\text{trg}} = 2.5 \text{ MW}$$



particle yields at the edge of MCS for different beam sizes

tilt=100 mrad, $L_{\text{trg}}=30$ cm, $r_{\text{trg}}=5$ mm

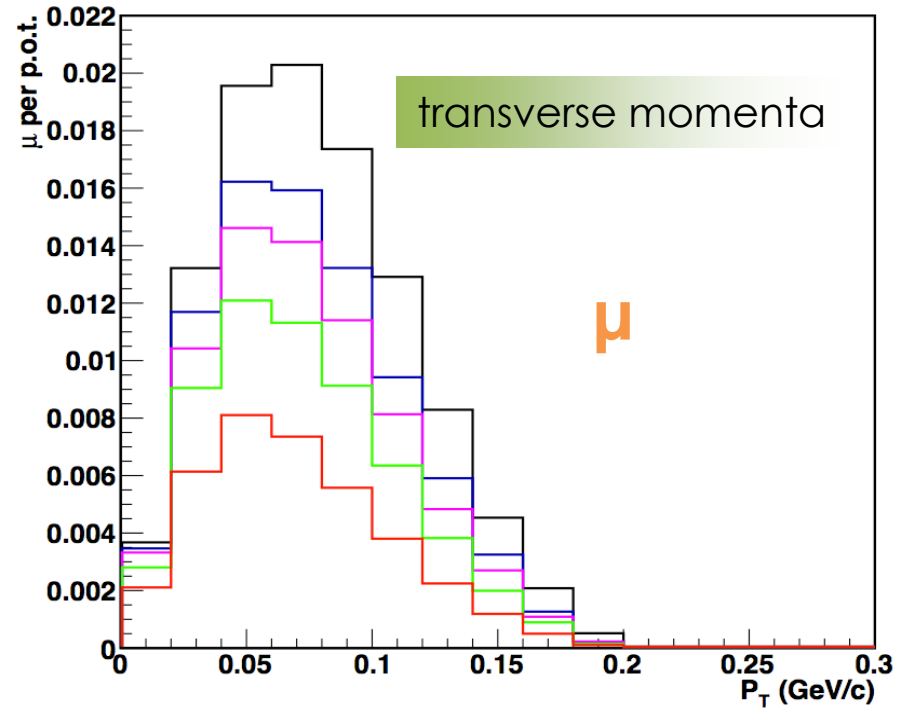
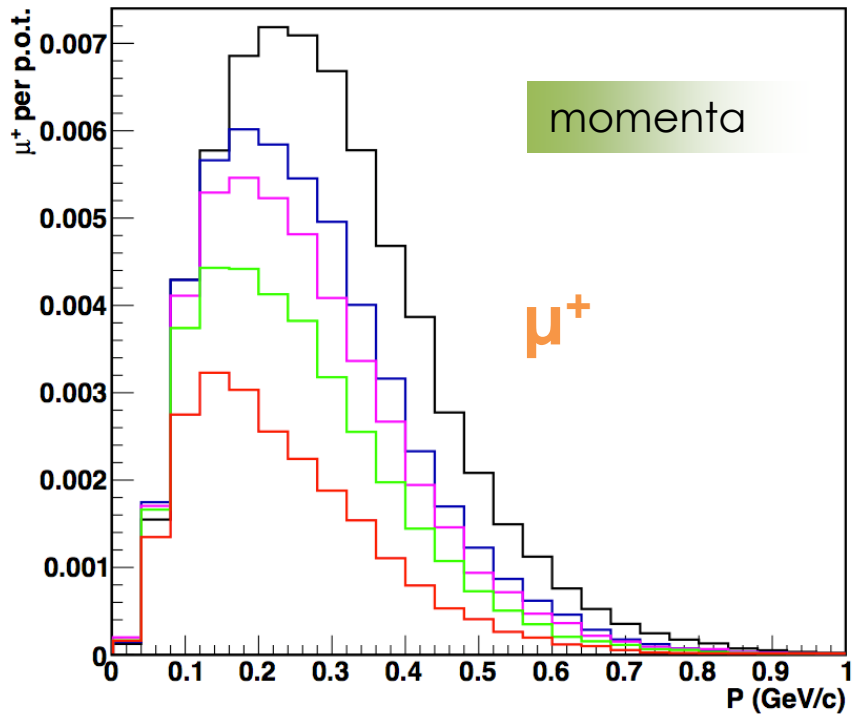
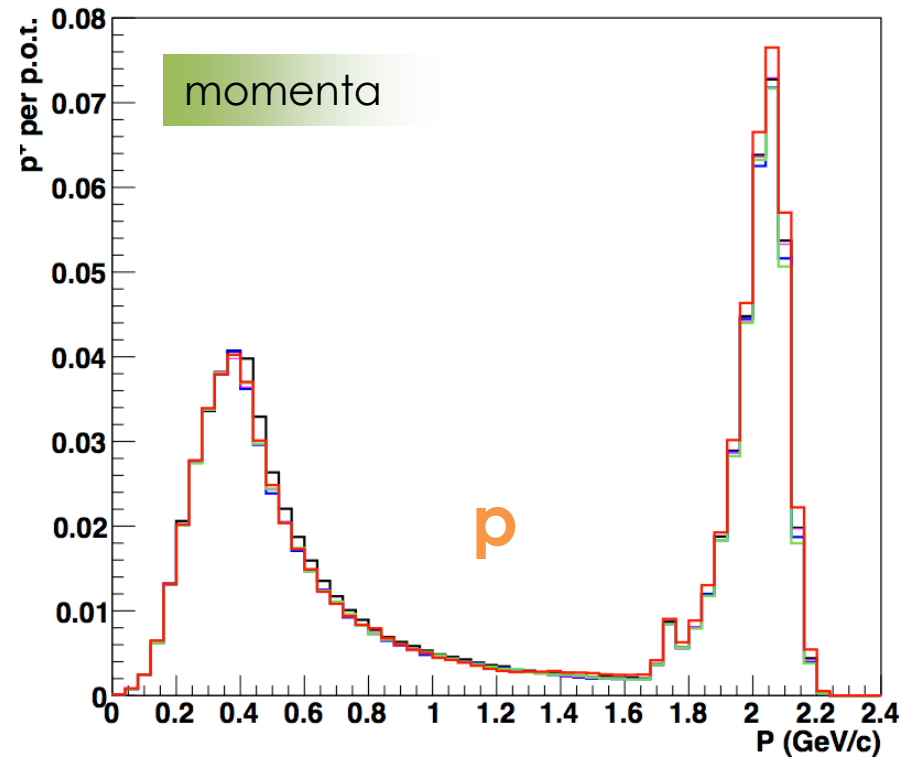


statistical error < 1 %

similar, could do less in beam size

momenta distributions (to be updated)

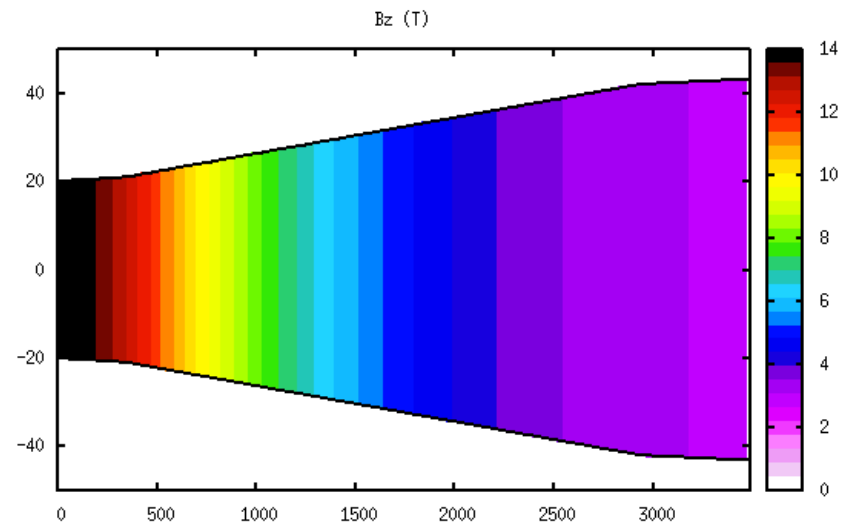
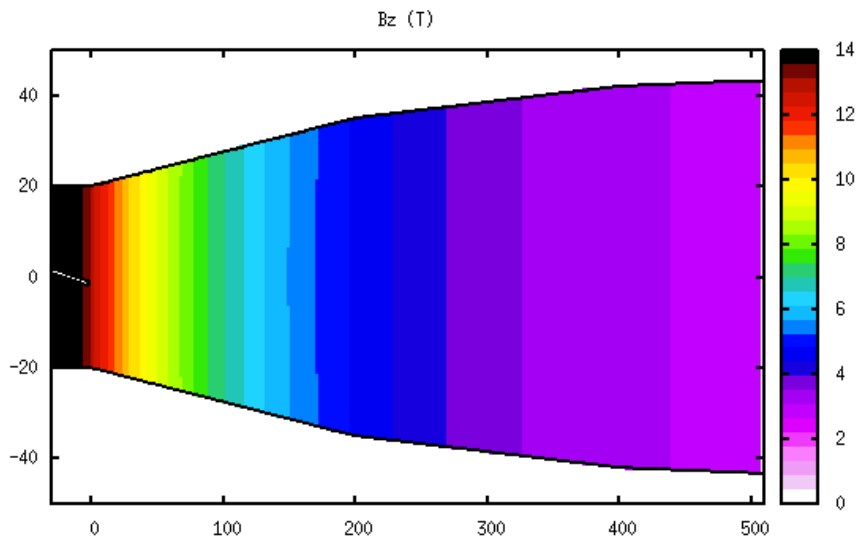
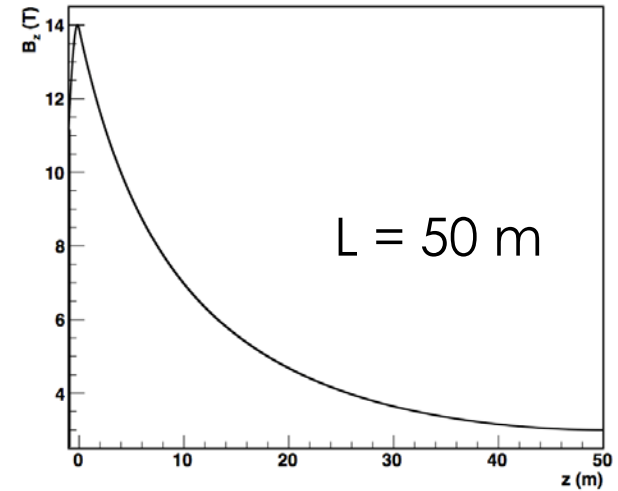
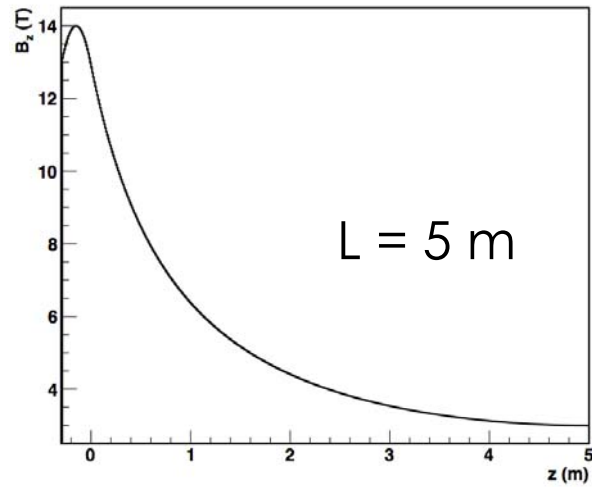
$L = 5, 10, 15, 20, 50$ m

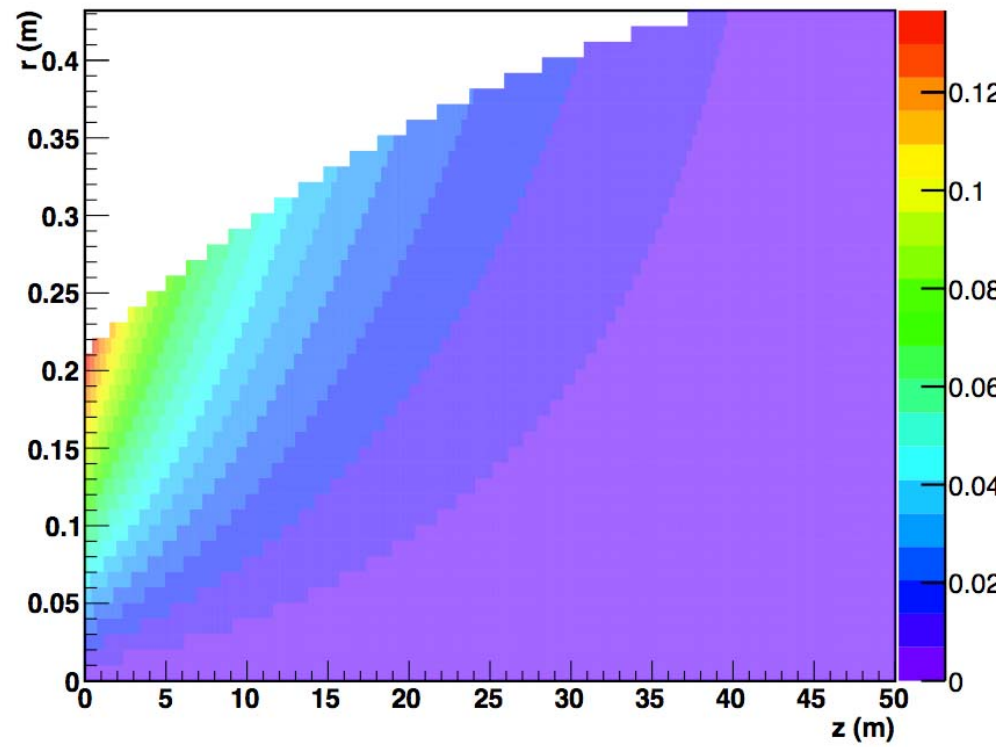
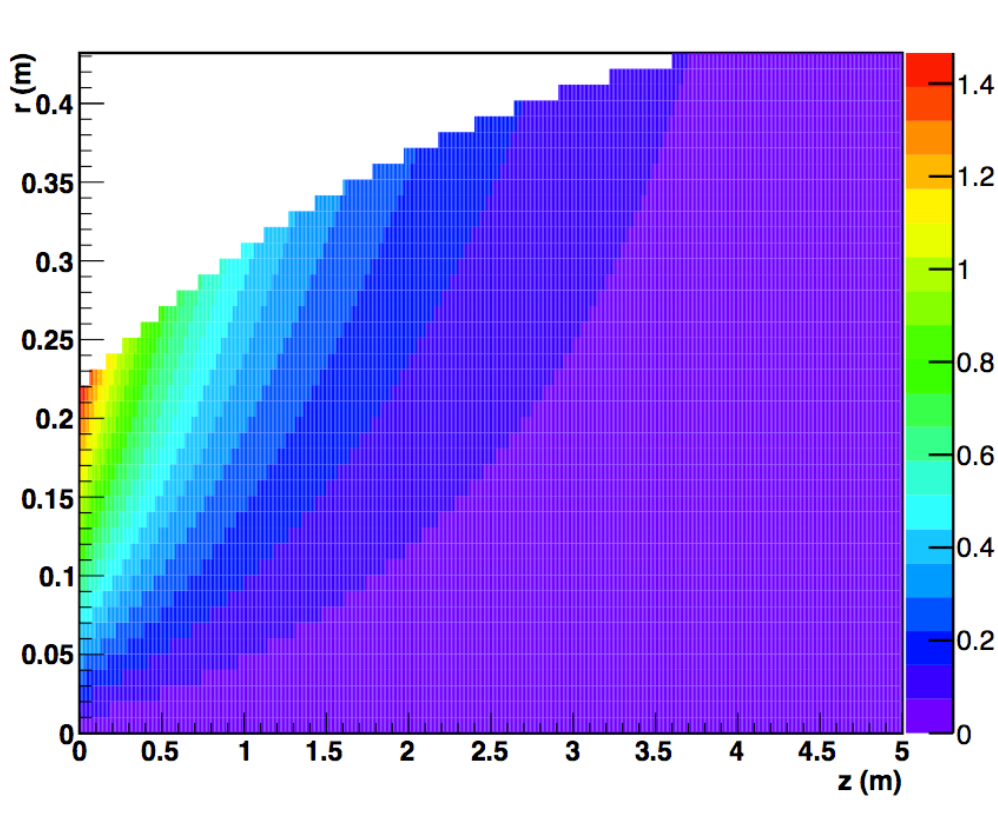


$$B_z(0, z) = B_0 e^{-(z-z_0)^2/2\sigma^2}$$

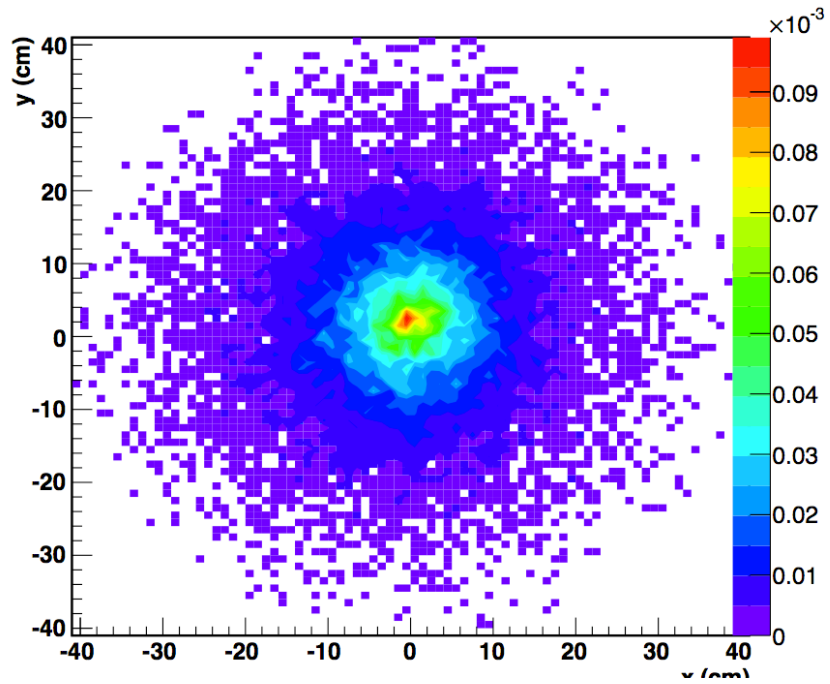
$$B_0 = 14T, z_0 = -15cm$$

$$+ B_z(0, z) = \frac{B_1}{1 + a_1 * (z-z_1) + a_2 * (z-z_1)^2 + a_3 * (z-z_1)^3}$$

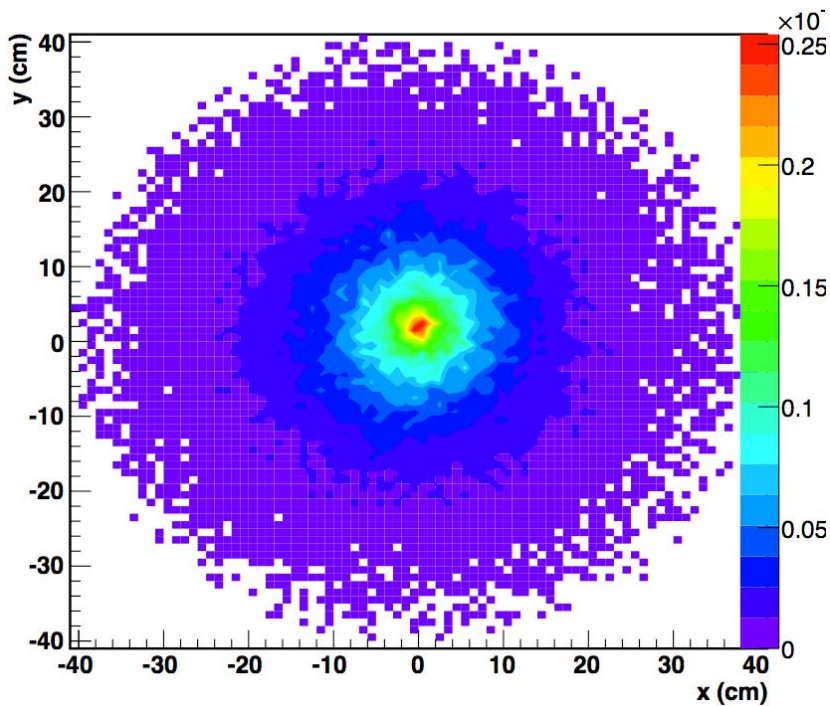
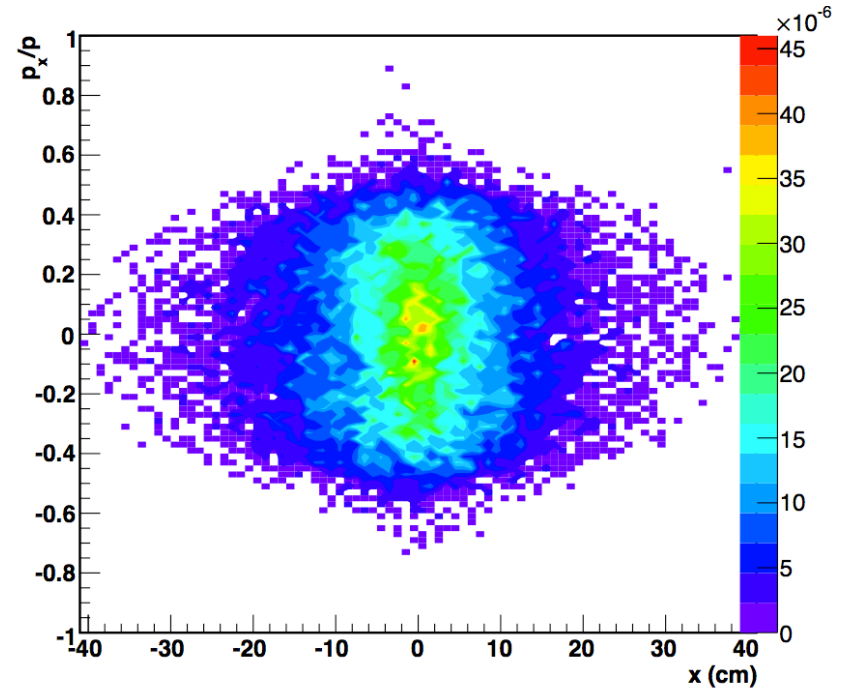




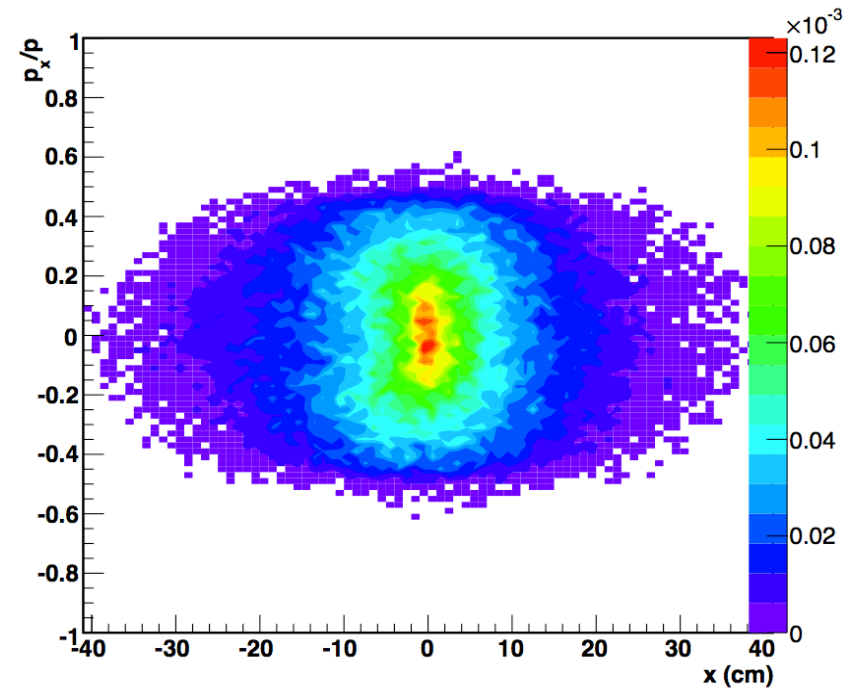
spatial distribution and transverse emittance



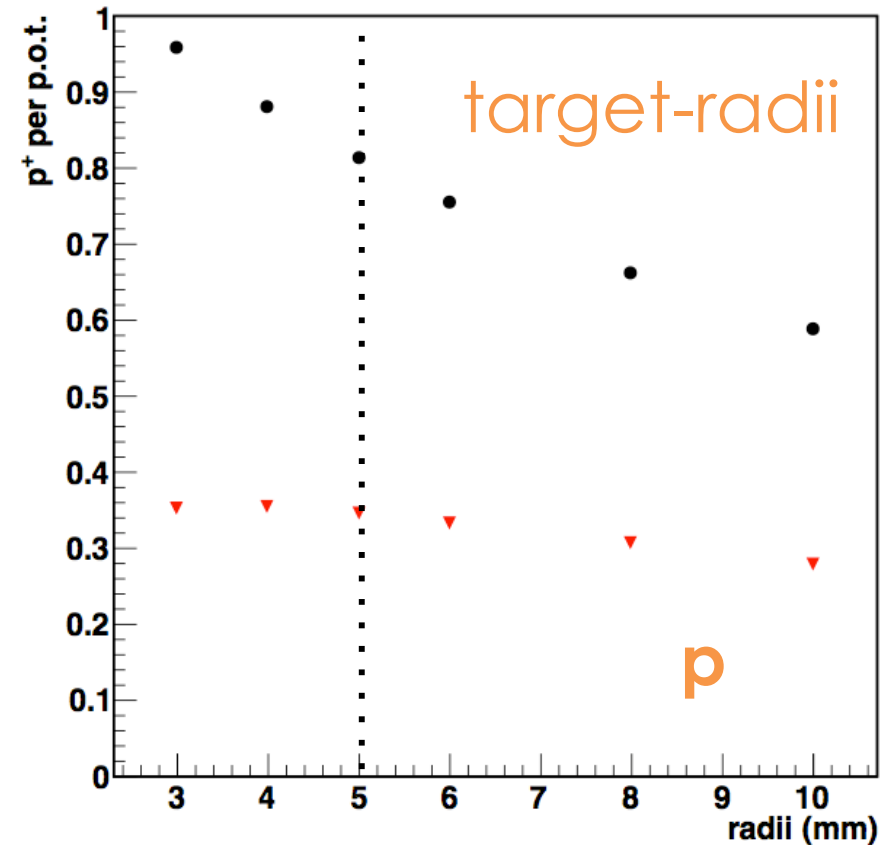
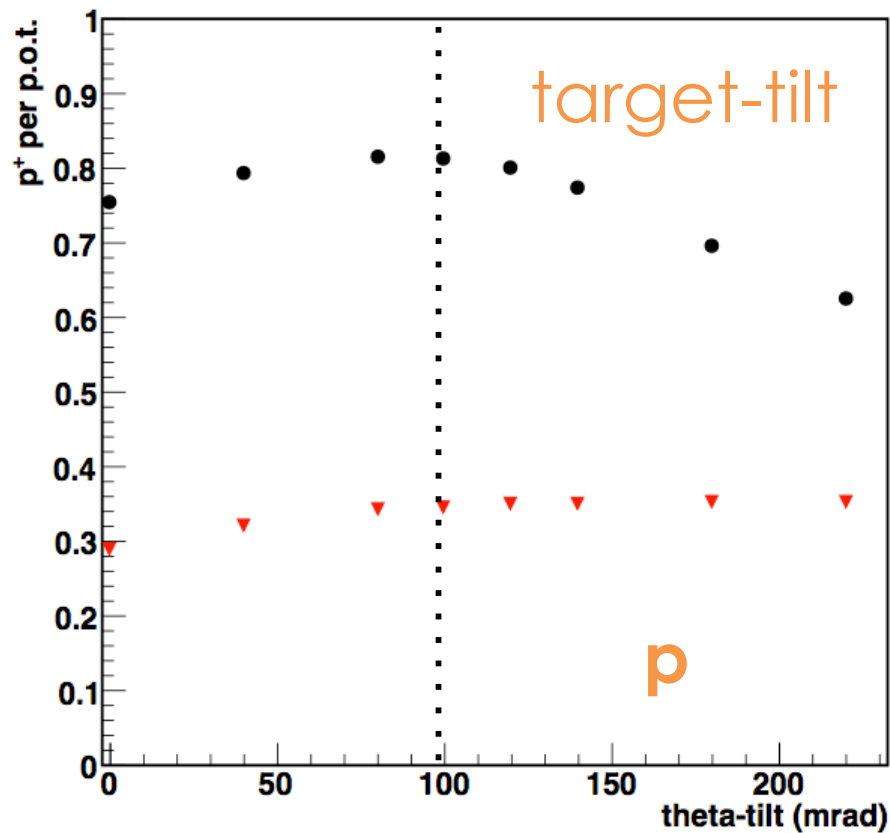
$L = 5$ m



$L = 50$ m



proton yields for inverse taper $L = 50$ m vs different target-tilts, radii



statistical error < 1 %