file s020_sys_k11.tex, Kirk McDonald, Aug. 30, 2006
Comments in sans serif
Modifications in slanted type
Original text in Roman

1. I recommend that we switch to the Standard European convention of putting a space between a citation and the preceding word. Thus, CHOOZ experiment [8] rather than CHOOZ experiment[8]. This change requires tinkering with some LaTeX setup file, so I have not been able to enforce it myself. I have put spaces in front of citations, but they don't appear in the output, in general.

2. Looking at[8],
http://puhep1.princeton.edu/~mcdonald/examples/neutrinos/apollonio_epj_c27_331_03.pdf
we see the convention referred to in comment 1, and we see that they spell it CHOOZ and not Chooz.

3. I notice that the typography of the references does not quite follow the conventions recommended in db-latex.tex. I have changed the references to do so. While these changes are mostly invisible, experts can detect them. Also, a few bad references have been fixed....

4. I have put the hyphen in compound adjectives, as beloved by Phys. Rev. editors.

5. We should never write "errors" in a formal document, only "uncertainties"!!!! (We should also speak this way, but I know that won't happen.)

6. Ref 6dchooz has been updated to point to a very recent document. I added Vogel's paper to ref 7illbeta.

7. The big issue is that there seems to me to be a large gap in the structure of chaps 1-3. Namely, we don't introduce the concept/principle of our measurement anywhere. Chap 1 talks about physics – that we can an should measure $\sin^2 2\theta_{13}$. The old Chap 2 jumps in to talk about uncertainties on a measurement that has never been defined. The old Chap 3 talks about the equipment needed to make the measurement – without quite saying what the measurement is. So, I'm making an attempt at writing what seems to me to be the missing section. I will place it as sec. 2.1. However, it could be that we should swap chaps. 2 and 3 (and use the new section as sec. 2.1 of the chapter on the experimental overview). It could that the new section should be used to enlarge sec. 1.4.

7A. It is now agreed that the old chap 2 will become the new chap 3. So I have renumbered the new sections as 3.x.

8. We need to quote a numerical value for ΔM_{31}^2. Several variants are used in different places in the CDR. I believe that we should quote the present best value, AND reference the source. The SuperK PRD paper from 2005, ref 7superk, may be the best source. Even so, some interpretation is required. I conclude from one of their plots that the best thing to say is that $\Delta M_{31}^2 = 2.2 \pm 0.5 \times 10^{-3}$.

9. The old sec. 2.3.1 has been shortened and moved to the new sec. 3.1.5.

10. I have added a new sec. 3.1.6 as a transition from the new sec. 3.1 on the principle of the measurement to the more detailed discussion of limitations to its sensitivity. If the new sec. 3.1 is separated from the rest of chap. 3, this transition subsection should still provide a transition across such a break. The new section 3.1.6 subsumes the original introductory paragraph to chap. 2. I was very uncomfortable with that paragraph as it started out with a discussion of CHOOZ rather than Daya Bay – and that discussion did not make sense unless the reader understood that the analyzing power of CHOOZ was 1/2 due to poor choice of their far site.

11. The old sec. 2.1 is the new sec. 3.2. Various suggested changes are embedded in the new text.

12. The new sec. 3.2.1 is considerably revised from the original. I was extremely uncomfortable with the lack of motivation of the old eq. (14), and the appearance of a parameter α whose value is never specified. This led to the new sec. 3.1 as an attempt to present an understandable procedure

for the measurement, and hence and understandable characterization of the effect of various uncertainties on that measurement.

It is clear, however, that the assumption that a given detector is either "near" or "far" is poor in practice. Therefore, the actual analysis must be more sophisticated than that presented in the new sec. 3.1 – or that represented by the mysterious eq. (14) of the original version.

(Aug 30, 2006). At length I have concocted an argument that justifies the result of the old eq. (14). The text now relates the essence of that equation to a well-defined procedure to deduce $\sin^2 2\theta_{13}$ from the data. The detector weights are explicitly noted, and the resulting small increase in the statistical uncertainty on $\sin^2 2\theta_{13}$ is also explicitly noted.

I also include more clearcut results for the case of 4 reactor cores than were previously given. The values in the new Table 3.3 are similar to those in the old Table 2.2.

13. The new section 3.2.2 on location uncertainties is somewhat briefer than the old sec. 2.1.2. However, missing from this section – or from chap. 3 are TABLES of the elevations of all detectors and reactors, the overburden in meter, ands meters of water equivalent for all detectors. I have added a new Table 3.2 that gives the distances from all detectors to all reactors. This is taken from chap. 7 of the V3.3 proposal. Some of these numbers are in figures and text – with different values in different places! Note that the distance from the "Day Bay near detector" to the Ling Ao II reactor is over one km, $\Rightarrow$ the approximation of "far" and "near" detectors is not very good.

Also, we need to discuss the issue of the effect of the elevation difference between detectors and reactors. Since our detectors are cylindrical, not spherical, we have been criticized on this. However, verbal arguments have been made that there is not really much of a problem here. We must now put those arguments in writing. Has anyone already done this? (Bob McKeown...)

14. I have written some brief text for sec. 3.2.3, which was the previously blank sec. 2.1.3.

15. Sec. 3.3 (old sec. 2.2) begins with a new paragraph to remind the reader that a relative uncertainty in various detector parameters can lead to an absolute uncertainty in $\sin^2 2\theta_{13}$ or the same numerical value.

16. The discussion of the uncertainty of detector mass in the new sec. 3.3.1 (old sec. 2.2.1) has been considerably altered. It seems to me that the previous discussion was quite wide of the mark. I believe we can do much better than stated!

17. I have split the old sec. 2.2.1 into the new sections 3.3.1 and 3.3.2. The old section 2.2.1 seemed to present two quite different views on the H/C problem, without reconciling those views. In an attempt to do so, I have largely rewritten this section. But the question remains as to whether we have an agreed baseline about how we will fill the detectors????

18. The old sec. 2.2.2 is the new sec. 3.3.3, on the need to know the gadolinium concentration. This section was too brief, and indeed it seems to me that it contained a small numerical error, perhaps because the full argument had never been written out.

However, this topic would be rendered moot by filling all detectors with the same scintillator. I consider this to be the "goal", and I leave the baseline as having to struggle to make measurements that are not strictly necessary.

To me, this is a poor philosophy. I believe that the experiment would be sounder if we adopt a strategy that intrinsically eliminates sources of uncertainty where possible – and implements checks (such as measurement of the neutron-capture time) to verify that the strategy has worked to a high degree of accuracy.

19. The old sec. 2.2.3 is the new sec. 3.3.4. My general comment on this section, as on many others, is that we should put the Daya Bay experiment first, and refer to other experiments only as a sidelight. Therefore, I have reordered the text quite a bit.

Also, since chap 2 will appear early in the CDR, somewhat greater detail is needed to explain what we are doing. I seem to be putting back some of the facts and figures that appeared in the V3.3 proposal, but which vanished in the first draft of the CDR.

This section seems very incomplete in that it leads us to realize how important is the detec-

tor energy scale calibration, but gives little indication of what we can expect. So, the energy cut uncertainties seem just like guesses.

20. The old sec. 2.2.4 is the new sec. 3.3.5. The first two sentences were deleted as being repetitious. Otherwise only minor stylistic changes, such as nsec $\rightarrow$ ns.

21. The old sec. 2.2.5 is the new sec. 3.3.6. This section appears to be about a BACK-GROUND issue, rather than a systematic uncertainty. Shouldn't it be moved into the background section of chap 2?

In any case, this section should begin with a statement of the problem, and end with the comparison to CHOOZ. As it was, this section contained no numbers, so the corresponding entries in Table 3.4 seemed somewhat mysterious.

22. The old sec. 2.3 has been eliminated. All of the material that was there has been moved into new secs. 3.1 and 3.2.

3 Principle of the Measurement of $\sin^2 2\theta_{13}$, **Sensitive & Systematic** Uncertainties

3.1 Principle of the Measurement of $\sin^2 2\theta_{13}$

The Daya Bay Reactor Neutrino Experiment will measure the disappearance of electron antineutrinos ($\bar\nu_e$) as a function of distance from their production in the Daya Bay reactor complex. As discussed in sec. 1.3.1, the probability that an antineutrino that is created as a $\bar\nu_e$ of energy E remains a $\bar\nu_e$ after traveling a distance L can be written as

$$P_{\text{sur}} = 1 - P_{\text{dis}} \approx 1 - A(E, L)\sin^2 2\theta_{13}, \tag{1}$$

where the "analyzing power" A for $E \approx$ 1-10 MeV and $L < 2$ km has the form

$$A(E, L) = \sin^2 \Delta_{31} = \sin^2\left[1,267\Delta m_{31}^2(\text{eV}/c^2)^2\frac{L(\text{km})}{E(\text{MeV})}\right] \approx \sin^2\left[2.8\frac{L(\text{km})}{E(\text{MeV})}\right], \tag{2}$$

using the current best estimate[30] that the neutrino mass splitting parameter Δm_{31}^2 is 2.2 ± 0.5 (eV/$c^2)^2$.

3.1.1 One detector, one reactor, one distance

If a single neutrino detector is placed at a distance L from a single nuclear reactor, the number $N(E)$ of detected neutrino interactions in an interval dE about energy E during time t can be written as the product

$$N(E) = \frac{\phi_r(E, dE, t)}{L_{rd}^2}p_{\bar\nu}M_d\epsilon_d(1 - A\sin^2 2\theta_{13}) \equiv \frac{\phi_r K}{L_{rd}^2}(1 - A\sin^2 2\theta_{13}) \tag{3}$$

where $\phi_r(E, dE, t)$ is the total flux at unit distance of antineutrinos from the reactor during time t in interval dE about E, L_{rd} is the distance from the reactor to the detector, $p_{\bar\nu_e}$ is the probability of a neutrino interaction $\bar\nu_e + p \rightarrow n + e^+$ per unit detector mass, M_d is the detector mass, ϵ_d is the detection efficiency, and $K = p_{\bar\nu_e}M_d\epsilon_d$.

The spectrum of reactor antineutrinos falls with energy, while the cross section for rises with energy. As shown in Fig. 3.1 the most probable energy for observation of inverse β decay is for an antineutrino energy of 4 MeV.
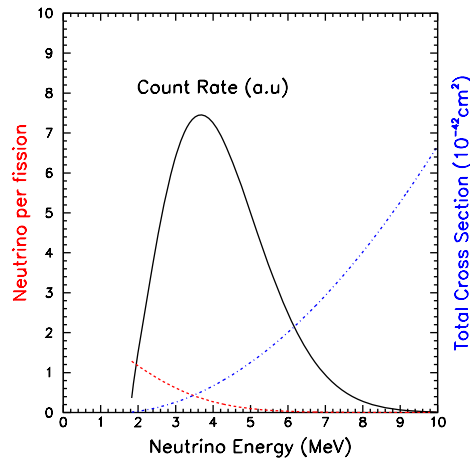

Fig. 3.1. The $\bar\nu_e$ production rate in a nuclear reactor, the cross section for inverse β decay, and the probability of observation of the inverse *beta* decay process in a reactor neutrino experiment, as a function of the energy of the antineutrino.

Clearly, the distance L_{rd} should be chosen such that the analyzing power A is maximal. Using $\Delta m^2_{31} = 2.2\ (\text{eV}/c^2)^2$ in eq. (2), the analyzing power would be 1 for $L = 2.25$ km and $E = 4$ MeV.

In principle, a determination of $\sin^2 2\theta_{13}$ can be made using eq.(3) using a single detector at a single distance from a single reactor. The distance L can be well measured, the neutrino flux ϕ can be calculated reasonably well from measurement of the reactor power[28], but the factor K is not well known in practice. Hence, extensions of the measurement technique are desirable that reduce the dependence of the result for $\sin^2 2\theta_{13}$ on the product ϕK.

3.1.2   One detector, one reactor, two distances

If a single detector is operated at different times at two distances $L^{(1)}$ and $L^{(2)}$ from a single reactor, two sets of neutrino interactions $N^{(1)}$ and $N^{(2)}$ can be observed. The ratio of these observations is

$$\frac{N^{(2)}}{N^{(1)}} = \left(\frac{L^{(1)}}{L^{(2)}}\right)^2 \frac{1 - A(L^{(2)})\sin^2 2\theta_{13}}{1 - A(L^{(1)})\sin^2 2\theta_{13}}, \tag{4}$$

assuming that the factors ϕ_r and K are independent of time.

To minimize the time of the experiment, distance $L^{(1)}$ should be much less than $L^{(2)}$. We call distance $L^{(2)}$ the Far distance and write $N^{(2)} = N_{\text{Far}}$. Similarly, we say that $L^{(1)}$ the Near distance and write $N^{(1)} = N_{\text{Near}}$.

Then if $A(L^{(2)}) \approx 1$ we have $A(L^{(1)}) \approx 0$ and

$$\frac{N_{\text{Far}}}{N_{\text{Near}}} \approx \frac{L^2_{\text{Near}}}{L^2_{\text{Far}}}(1 - \sin^2 2\theta_{13}), \qquad \sin^2 2\theta_{13} \approx 1 - \frac{L^2_{\text{Far}}}{L^2_{\text{Near}}}\frac{N_{\text{Far}}}{N_{\text{Near}}}. \tag{5}$$

Thus, the use of two distances largely eliminates the dependence of the measurement of $\sin^2 2\theta_{13}$ on the imperfectly known quantities ϕ_r and K.

The one-standard-deviation statistical uncertainty on the observation of N events is $\delta_N = \sqrt{N}$. Hence, the statistical uncertainty on the measurement of $\sin^2 2\theta_{13}$ according to eq. (5) would be

$$\delta_{\sin^2 2\theta_{13}} \approx \frac{L^2_{\text{far}}}{L^2_{\text{Near}}}\frac{N_{\text{Far}}}{N_{\text{Near}}}\sqrt{\frac{1}{N_{\text{Far}}} + \frac{1}{N_{\text{Near}}}}. \tag{6}$$

If the number N_{Far} of events observed at the Far distance is small compared to the number N_{Near} observed at the Near distance, then

$$\delta_{\sin^2 2\theta_{13}} \approx \frac{L^2_{\text{Far}}}{L^2_{\text{Near}}}\frac{\sqrt{N_{\text{Far}}}}{N_{\text{Near}}} \qquad (N_{\text{Far}} \ll N_{\text{Near}}). \tag{7}$$

For small values of $\sin^2 2\theta_{13}$ the product $L^2 N$ is essentially independent of distance, so that we can make the further approximation,

$$\delta_{\sin^2 2\theta_{13}} \approx \frac{1}{\sqrt{N_{\text{Far}}}} \qquad (N_{\text{Far}} \ll N_{\text{Near}},\ \sin^2 2\theta_{13} \ll 1). \tag{8}$$

If we wish to determine $\sin^2 2\theta_{13}$ with a statistical uncertainty of, say, 0.001, then the number of antineutrino events observed at the far location should be $N_{\text{far}} \approx 10^6$.

Note that from the two measurements, N_{Near} and N_{Far}, the unknown product $\phi_r K$ is determined as well as $\sin^2 2\theta_{13}$. Indeed, in the approximation that the analyzing power is zero for the Near distance, we have from eq. (3) that

$$\phi_r K = L^2_{\text{Near}} N_{\text{Near}}, \qquad \text{and} \qquad \frac{\delta_{\phi_r K}}{\phi_r K} \approx \frac{1}{\sqrt{N_{\text{Near}}}}. \tag{9}$$

While the factors ϕ_r and K are not measured separately, their product is very well measured.

5

3.1.3 Two detectors, one reactor, two distances

One way to improve the statistical accuracy of the measurement of $\sin^2 2\theta_{13}$ in a fixed time is by use of multiple detectors.

For example, if $N_i^{(k)}$ is the number of antineutrino interactions observed in detector i when in configuration (k), for which its distance to the reactor is $L_i^{(k)}$, then

$$N_i^{(k)} = \frac{\phi_r K_i}{(L_i^{(k)})^2}(1 - A(L_i^{(k)}) \sin^2 2\theta_{13}).$$

(10)

The value of the constants K_i could well be different for different detectors. To minimize the effect of the possible variation of the constant K_i between detectors, they should not be operated at a single distance. A simple procedure is to operate each detector at both distances $L_1^{(1)} = L_{\text{Near}}$ and $L_1^{(2)} = L_{\text{Far}}$, which requires "swapping" the two detectors at the midpoint of the duration of the experiment. That is, $L_2^{(1)} = L_1^{(2)} = L_{\text{Far}}$ and $L_2^{(2)} = L_1^{(1)} = L_{\text{Near}}$. Then, if $A(L_{\text{Near}}) \approx 0$ and $A(L_{\text{Far}}) \approx 1$, we measure

$$\sin^2 2\theta_{13} = 1 - \frac{L_{\text{Far}}^2}{L_{\text{Near}}^2}\frac{N_1^{(2)}}{N_1^{(1)}} = 1 - \frac{L_{\text{Far}}^2}{L_{\text{Near}}^2}\frac{N_2^{(1)}}{N_2^{(2)}}.$$

(11)

If the two detectors are nearly identical, i.e., $K_1 \approx K_2$, the accuracy of each of the two measurements of $\sin^2 2\theta_{13}$ with be the same, and the best estimate is the average of the two measurements,

$$\sin^2 2\theta_{13} = 1 - \frac{1}{2}\frac{L_{\text{Far}}^2}{L_{\text{Near}}^2}\left(\frac{N_1^{(2)}}{N_1^{(1)}} + \frac{N_2^{(1)}}{N_2^{(2)}}\right) \qquad (K_1 \approx K_2).$$

(12)

Further, if the duration of operation in the two configurations is nearly identical we can write $N_1^{(2)} \approx N_2^{(1)} \approx N_{\text{Far}}/2$ and $N_1^{(1)} \approx N_2^{(2)} \approx N_{\text{Near}}/2$, so that eq. (12) reduces to eq. (5),

$$\sin^2 2\theta_{13} \approx 1 - \frac{L_{\text{Far}}^2}{L_{\text{Near}}^2}\frac{N_{\text{Far}}}{N_{\text{Near}}} \qquad (K_1 \approx K_2, \text{ equal times}).$$

(5)

The statistical uncertainty on the measurement (5) of $\sin^2 2\theta_{13}$ is again given by eqs. (7)-(8).

In principle, the four measurements $N_i^{(k)}$ suffice to determine the four unknown quantities $\sin^2 2\theta_{13}$, ϕ_r, K_1 and K_2. However, only $\sin^2 2\theta_{13}$ and the products $\phi_r K_1 = N_1^{(1)} L_{\text{Near}}^2$ and $\phi_r K_2 = N_2^{(2)} L_{\text{Near}}^2$ are determined in a simple manner. Extraction of ϕ_r, K_1 and K_2 requires use of a χ^2-minimization procedure with

$$\chi^2 = \sum_{i=1}^{2}\sum_{k=1}^{2}\frac{\left[N_i^{(k)} - \frac{\phi K_i}{(L_i^{(k)})^2}(1 - A(L_i^{(k)})\sin^2 2\theta_{13})\right]^2}{N_i^{(k)}},$$

(13)

taking the uncertainty on the number $N_i^{(k)}$ of observed events to be $\delta_{N_i^{(k)}} = \sqrt{N_i^{(k)}}$.

3.1.4 8 detectors, 6 reactors (the Daya Bay Reactor Neutrino Experiment)

Nuclear reactor complexes typically have more than one reactor. If we observe antineutrino interactions from m reactors with a set of n detectors, there are $m + n + 1$ unknowns, $\sin^2 2\theta_{13}$, the reactor fluxes ϕ_j for $j = 1$ to m, and the detector constants K_i for $i = 1$ to n.

A single configuration of the detectors around the reactors leads to the observation of n numbers of events in the n detectors. If k different configurations are the detectors are used over the course of the

experiment, a total of kn measurements are made. If $\sin^2 2\theta_{13}$ is to be determined with no dependence on the $m + n$ fluxes and detector constants, then kn must be greater than or equal to $m + n + 1$.

The Daya Bay reactor complex will have $m = 6$ reactors operational by the completion of the experiment. To determine $\sin^2 2\theta_{13}$ independent of the K_i and the ϕ_j with only two detector configurations requires a minimum of $n = 7$ detectors.

The proposal is to use 8 detectors, arrayed in two "near" groups of two detectors, and one "far" group of 4 detectors, as shown in Fig. 3.2.

Fig. 3.2. Layout of the Daya Bay *reactor neutrino* experiment.

To a first approximation, the analyzing powers (2) are unity for detectors and the far site, and zero for detectors at the near sites.

We consider two configurations, indicated by superscripts $^{(1)}$ and $^{(2)}$, such that in configuration 1 detectors 1-4 are at near sites while detectors 5-8 are at the far site. Then, in configuration 2 detectors 1-4 are at the far site and detectors 5-8 are at near far sites.

The observed rates $N_i^{(k)}$ of antineutrino events in the 8 detectors can be written as

$$N_i^{(1)} = K_i \sum_{j=1}^{6} \frac{\phi_j}{(L_{i,j}^{(1)})^2}, \qquad\qquad i = 1\text{-}4, \tag{14}$$

$$N_i^{(1)} = K_i \sum_{j=1}^{6} \frac{\phi_j}{(L_{i,j}^{(1)})^2}(1 - \sin^2 2\theta_{13}), \qquad i = 5\text{-}8, \tag{15}$$

$$N_i^{(2)} = K_i \sum_{j=1}^{6} \frac{\phi_j}{(L_{i,j}^{(2)})^2}(1 - \sin^2 2\theta_{13}), \qquad i = 1\text{-}4, \tag{16}$$

$$N_i^{(2)} = K_i \sum_{j=1}^{6} \frac{\phi_j}{(L_{i,j}^{(2)})^2}, \qquad\qquad i = 5\text{-}8, \tag{17}$$

We form the 8 ratios,

$$\frac{N_i^{(2)}}{N_i^{(1)}} = \frac{\sum_{j=1}^{6} \frac{\phi_j}{(L_{i,j}^{(2)})^2}}{\sum_{j=1}^{6} \frac{\phi_j}{(L_{i,j}^{(1)})^2}}(1 - \sin^2 2\theta_{13}) = \rho_i(1 - \sin^2 2\theta_{13}), \qquad i = 1\text{-}4, \tag{18}$$

$$\frac{N_i^{(1)}}{N_i^{(2)}} = \frac{\sum_{j=1}^6 \frac{\phi_j}{(L_{i,j}^{(1)})^2}}{\sum_{j=1}^6 \frac{\phi_j}{(L_{i,j}^{(2)})^2}}(1 - \sin^2 2\theta_{13}) = \rho_i(1 - \sin^2 2\theta_{13}), \qquad i = 5\text{-}8, \tag{19}$$

where

$$\rho_i = \frac{\sum_{j=1}^6 \frac{\phi_j}{(L_{i,j}^{(2)})^2}}{\sum_{j=1}^6 \frac{\phi_j}{(L_{i,j}^{(1)})^2}}, \qquad i = 1\text{-}4, \qquad \text{and} \qquad \rho_i = \frac{\sum_{j=1}^6 \frac{\phi_j}{(L_{i,j}^{(1)})^2}}{\sum_{j=1}^6 \frac{\phi_j}{(L_{i,j}^{(2)})^2}}, \qquad i = 5\text{-}8, \tag{20}$$

are ratios of sums of the reactor fluxes weighted by distances in the two configurations of the experiment. Using the notation that $L_{i,j,\mathrm{Far}}$ and $L_{i,j,\mathrm{Near}}$ represent the distances from detector i to reactor j when the detector is in its Far and Near location, respectively, the ratios ρ_i can be written as

$$\rho_i = \frac{\sum_{j=1}^6 \frac{\phi_j}{L_{i,j,\mathrm{Far}}^2}}{\sum_{j=1}^6 \frac{\phi_j}{L_{i,j,\mathrm{Near}}^2}}, \quad i = i\text{-}8. \tag{21}$$

We now have 8 measurements of $\sin^2 2\theta_{13}$,

$$\sin^2 2\theta_{13} = 1 - \rho_i \frac{N_i^{\mathrm{Far}}}{N_i^{\mathrm{Near}}}, \tag{22}$$

where $N_i^{\mathrm{Far}} = N_i^{(2)}$ for $i = 1\text{-}4$ and $N_i^{\mathrm{Far}} = N_i^{(1)}$ for $i = 5\text{-}8$, and similarly $N_i^{\mathrm{Near}} = N_i^{(1)}$ for $i = 1\text{-}4$ and $N_i^{\mathrm{Near}} = N_i^{(2)}$ for $i = 5\text{-}8$. All 8 detectors will be nearly identical, so if we operate for equal times in the two configurations, the numbers of events in the numerator of eq. (22) are all approximately equal to $N_{\mathrm{Far}}/8$, where N_{Far} is the total number of events observed at the Far site.

From the 8 measurements (21) of $\sin^2 2\theta_{13}$ we can report a single result based on the weighted average

$$\sin^2 2\theta_{13} = 1 - \sum_{i=1}^4 w_i \rho_i \frac{N_i^{(2)}}{N_i^{(1)}} - \sum_{i=5}^8 w_i \rho_i \frac{N_i^{(1)}}{N_i^{(2)}} = 1 - \sum_{i=1}^8 w_i \rho_i \frac{N_i^{\mathrm{Far}}}{N_i^{\mathrm{Near}}}, \qquad \text{where} \qquad \sum_{i=1}^8 w_i = 1, \tag{23}$$

where to a first approximation the weights w_i are all equal to 1/8. Equation (23) is a generalization of eqs. (5) and (12), and likewise involves ratios of rates in Far detectors to those in Near detectors. The detector factors K_i do not appear in eq. (23), but ratios of the reactor fluxes ϕ_j do appear via the ρ_i.

In the approximation that the statistical uncertainty in the measurement of $\sin^2 2\theta_{13}$ is due only to the numbers of events in Far detectors, that uncertainty is, recalling eq. (7),

$$\delta_{\sin^2 2\theta_{13}} \approx \sqrt{\sum_{i=1}^8 \left(w_i \rho_i \frac{\sqrt{N_i^{\mathrm{Far}}}}{N_i^{\mathrm{Near}}} \right)^2}. \tag{24}$$

It is a good approximation that all the numbers of events in the numerators of eq. (24) are $N_i^{\mathrm{Far}} \approx N_{\mathrm{Far}}/8$. For small $\sin^2 2\theta_{13}$ it is also a reasonable approximation that the numbers of events in the denominators can be written as $N_i^{\mathrm{Near}} \approx N_{\mathrm{Far}}/(8\rho_i)$. Then, we obtain the form

$$\delta_{\sin^2 2\theta_{13}} \approx \frac{\sqrt{8\sum_{i=1}^8 w_i^2}}{\sqrt{N_{\mathrm{Far}}}} \approx \frac{1}{\sqrt{N_{\mathrm{Far}}}}, \tag{8}$$

where the second approximation follows if the weights w_i are all 1/8.

The measurement (23) of $\sin^2 2\theta_{13}$ depends on our knowledge of the reactor fluxes ϕ_j through the factors ρ_i of eq. (20). In principle these fluxes can be determined from the 16 measurements $N_i^{(k)}$, but this determination requires use of a χ^2-minimization procedure, with

$$\chi^2 = \sum_{i=1}^{8}\sum_{j=1}^{6}\sum_{k=1}^{2} \frac{\left[N_i^{(k)} - \frac{\phi_j K_i}{(L_{i,j}^{(k)})^2}(1 - A(L_{i,j}^{(k)}, \Delta m_{31}^2)\sin^2 2\theta_{13}) \right]^2}{N_i^{(k)}} , \qquad (25)$$

as discussed further sec. 3.5.1. This procedure can fit for 16 parameters, which can include the mass-splitting parameter Δm_{31}^2 via its role in the analyzing power (2) along with the 15 parameters $\sin^2 2\theta_{13}$, K_i and ϕ_j.

3.1.5 Detector "Swapping"

As discussed in sec. 3.1.4, the 8 detector constants K_i can in principle be determined along with $\sin^2 2\theta_{13}$ if each detector is operated at one of two Near sites and at the Far site for equal amounts of time. In practice it will not be convenient to "swap" all 8 detectors halfway through the experiment. Rather, we propose to make 3 "swaps" of 4 detectors each at the end of each quarter of the experiment, as indicated in Table 3.1.

Run Period	Near(DB)	Near(LA)	Far
I	1,3	5,7	2,4,6,8
II	2,3	6,7	1,4,5,8
III	2,4	6,8	1,3,5,7
IV	1,4	5,8	2,3,6,7

Table 3.1. Swapping scheme with 4 running periods. The detectors (labeled 1-8) are deployed at the Near(DB), Near(LA), and Far sites during each period as indicated in this table. *Each detector is operated for 50% of the experiment at the Far site.*

Careful calibration of the detectors before and after each "swap" will be necessary to insure that each detector's performance does not change significantly due to relocation.

3.1.6 Statistical Uncertainty on $\sin^2 2\theta_{13}$

As discussed in secs. 3.1.2-3.1.4, the statistical uncertainty on our measurement of $\sin^2 2\theta_{13}$ is approximately $1/\sqrt{N_{\text{Far}}}$, where N_{Far} is the total number of antineutrino events observed in all detectors at the Far site.

Each detector with have a fiducial mass of about 20 tons of liquid scintillator (see chap. **??**), as constrained by requirements of operation in the underground site. The far site is approximately 2 km from the Daya Bay reactors, so that the analyzing power (2) is close to unity. Then, each of the 4 detectors at the far site at any moment will observe about 90 antineutrino events per day. In 1000 days of operation, a total of $N_{\text{far}} \approx 3.6 \times 10^5$ events will be observed, and the corresponding statistical uncertainty on the measurement will be

$$\delta_{\sin^2 2\theta_{13}} \approx 0.0017 \qquad (\text{statistical}). \qquad (26)$$

The statistical uncertainty (26) is well below the goal of an overall sensitivity of $\sin^2 2\theta_{13} \approx 0.01$. The contribution to the uncertainty on the measurement of $\sin^2 2\theta_{13}$ from other sources than the number of observed antineutrino events will be discussed in the remainder of this chapter. These systematic uncertainties are of 3 types: reactor, detector and background.

For a historical perspective, the best existing limit of $\sin^2 2\theta_{13} < 0.17$ at 90% confidence level was obtained by the CHOOZ experiment[8] (with an analyzing power of 1/2 at their far site) which quotes a statistical uncertainty of 2.8% and a systematic uncertainty of 2.7%.

3.2 Reactor-related uncertainties

For a *single* reactor *(with only one core), the reactor flux* ϕ_r *is well determined by use of* one far detector and one near detector (assuming the average distances are precisely known), as discussed in sec. 3.1.2. *At present*, the Daya Bay Power Plant has four cores in two groups, the Daya Bay Plant and the Ling Ao Plant. Another two cores will be installed adjacent to Ling Ao, called Ling Ao II, which will start to generate electricity in 2010. Fig. 3.2 shows the locations of the Daya Bay cores, Ling Ao cores, and the future Ling Ao II cores. Superimposed on the figure are the tunneling scheme and the proposed detector sites. The distance between the two cores at each reactor site, called a pair here, is about 88 m. The Daya Bay pair is 1100 m from the Ling Ao pair, and the maximum span of cores will reach 1600 m when Ling Ao II starts operation.

Uncertainties in the reactor fluxes are associated with the power levels of the different cores and the effective locations of the cores relative to the detectors.

3.2.1 Reactor-power uncertainties

Knowledge of the reactor power is needed to calculate the ratios ρ_i of sum of distance-weighted antineutrino fluxes given by eq. (21). To assess the effect on the uncertainties δ_{ϕ_j} on the reactor fluxes, we recall eq. (23) and take the derivative

$$\frac{\partial \rho_i}{\partial \phi_j} = \rho_i \left(\frac{\frac{1}{L^2_{i,j,\mathrm{Far}}}}{\sum_{j'=1}^{6} \frac{\phi_{j'}}{L^2_{i,j',\mathrm{Far}}}} - \frac{\frac{1}{L^2_{i,j,\mathrm{Near}}}}{\sum_{j'=1}^{6} \frac{\phi_{j'}}{L^2_{i,j',\mathrm{Near}}}} \right) \approx \frac{\rho_i}{\phi} \left(\frac{\frac{1}{L^2_{i,j,\mathrm{Far}}}}{\sum_{j'=1}^{6} \frac{1}{L^2_{i,j',\mathrm{Far}}}} - \frac{\frac{1}{L^2_{i,j,\mathrm{Near}}}}{\sum_{j'=1}^{6} \frac{1}{L^2_{i,j',\mathrm{Near}}}} \right) \equiv \frac{\rho_i}{\phi} A_{ij}, \tag{27}$$

where we suppose that all 6 reactor fluxes ϕ_j are close to a common value ϕ.

The dependence of the measurement (23) of $\sin^2 2\theta_{13}$ on the ratios ρ_i is such that the contribution to its uncertainty due to the uncertainty in the reactor fluxes is

$$\delta_{\sin^2 2\theta_{13}} = \sum_{i=1}^{8} w_i \sum_{j=1}^{6} \frac{\partial \rho_i}{\partial \phi_j} \delta_{\phi_j} \frac{N_i^{\mathrm{Far}}}{N_i^{\mathrm{Near}}} \approx \sum_{j=1}^{6} \frac{\delta_{\phi_j}}{\phi} \sum_{i=1}^{8} w_i A_{ij} \rho_i \frac{N_i^{\mathrm{Far}}}{N_i^{\mathrm{Near}}} \approx \sum_{j=1}^{6} \frac{\delta_{\phi_j}}{\phi} \sum_{i=1}^{8} w_i A_{ij} \tag{28}$$

The coefficients A_{ij} that appear in eq. (27) can be evaluated from Table 3.2 of the distance between detector sites and reactors. We adopt the convention that detectors $i = 1$-4 use the Daya Bay near site, detectors $i = 5$-8 use the Ling Ao near site, reactors $j = 1$-2 are the Daya Bay cores, reactors $j = 3$-4 are the Ling Ao cores, and reactors $j = 5$-6 are the Ling Ao II cores, then there are only 6 distinct coefficients, $A_{ij} = -0.547$, 0.230 and 0.316 for $j = 1$-2, 3-4 and 4-5, respectively, when $i = 1$-4, and 0.192, -0.158 and -0.034 for $j = 1$-2, 3-4 and 4-5, respectively, when $i = 5$-8. There are only 3 distinct averages, $\sum_{i=1}^{8} A_{ij}/8 = -0.178$, 0.036 and 0.141 for $j = 1$-2, 3-4 and 4-5, respectively. We combine the 6 terms of eq. (28) in quadrature, assuming that all reactors have a similar uncertainty δ_ϕ in their flux and that all weights w_i are equal to 1/8, to find

$$\delta_{\sin^2 2\theta_{13}} \approx \frac{\delta_\phi}{\phi} \sqrt{\sum_{j=1}^{6} \left(\sum_{i=1}^{8} w_i A_{ij} \right)^2} \approx 0.23 \frac{\delta_\phi}{\phi} \qquad (w_i = 1/8). \tag{29}$$

This result is only slightly better than that of the approximation that all of the coefficients A_{ij} are 1/6. The coefficients A_{ij} associated with the Daya Bay near site have opposite sign to those associated with the Ling Ao near site, so combining the data from these sites yield a lower uncertainty than that associated with either site alone.*

If the Ling Ao II cores are not operational, the effect of the uncertainty in the other 4 reactor fluxes would be $\delta_{\sin^2 2\theta_{13}} \approx 0.10 \delta_\phi/\phi$, assuming that all the weights w_i are 1/8.

---

*The analysis up to this point closely parallels that by Suekane[1]. See also[32].

Table 3.2. Average distances of the detector sites to the two cores of each reactor pair, for the configuration shown in Fig. 3.2.

	Daya Bay cores	Ling Ao cores	Ling Ao II cores
Daya Bay near site (m)	360	850	1300
Ling Ao near site (m)	1330	440	500
Far site (m)	1980	1620	1610

The uncertainty (29) is small, but not negligible. It can be reduced by use of an appropriate set of weights w_i for the various detectors. A simple choice is that $w_i = w_{\mathrm{DB}}$ for detectors $1 = 1\text{-}4$ whose near location is the Daya Bay near site, and that $w_i = w_{\mathrm{LA}}$ for detectors $1 = 5\text{-}8$ whose near location is the Ling Ao site. The weights that yield the minimum uncertainty in $\sin^2 2\theta_{13}$ due to the uncertainty in the reactor fluxes when 6 cores are operational are $w_{\mathrm{DB}} = 0.066$ and $w_{\mathrm{LA}} = 0.183$,

$$\delta_{\sin^2 2\theta_{13}} \approx \frac{\delta_\phi}{\phi} \sqrt{\sum_{j=1}^{6} \left(\sum_{i=1}^{8} w_i A_{ij} \right)^2} \approx 0.08 \frac{\delta_\phi}{\phi} \qquad (w_{\mathrm{DB}} = 0.066,\ w_{\mathrm{LA}} = 0.183). \qquad (30)$$

The use of weights other than 1/8 increasing the statistical uncertainty in the measurement of $\sin^2 2\theta_{13}$ according to eq. (7). Using the weights that minimize the effect of uncertainty in the reactor flux, the statistical uncertainty increases by 10% to

$$\delta_{\sin^2 2\theta_{13}} \approx 0.0019 \qquad (\text{statistical},\ w_{\mathrm{DB}} = 0.066,\ w_{\mathrm{LA}} = 0.183). \qquad (31)$$

If the Ling Ao II cores are not operational, the use of weights $w_{\mathrm{DB}} = 0.101$ and $w_{\mathrm{LA}} = 0.149$ reduces the effect of the uncertainty in the reactor fluxes essentially to zero, with an accompanying increase in the statistical uncertainty in the measurement of $\sin^2 2\theta_{13}$ of only 2%

Studies of the measured neutrino spectra in the different near detectors during different parts of the reactor fuel cycle can help provide additional constraints on the fuel cycle effects on the spectrum.

The Bugey experiment[26] claimed an uncertainty of $\delta_\phi/\phi = 1.4\%$ in their knowledge of the reactor flux, and the CHOOZ experiment[8] claimed an uncertainty of only 0.6%. Here we suppose that the typical uncertainty in the Daya Bay reactor flux will be 2%.

Table 3.3. The effect of reactor-related *uncertainties* on the measurement of $\sin^2 2\theta_{13}$ for different reactor configurations. The uncorrelated *uncertainty in the antineutrino flux from* a single core is assumed to be $\delta_\phi/\phi = 2\%$. *The locations of the reactor cores are assumed to be known to 0.3 m.*

Number of cores	w_{DB}	w_{LA}	$\delta_{\sin^2 2\theta_{13}}$(power)	$\delta_{\sin^2 2\theta_{13}}$(location)	$\delta_{\sin^2 2\theta_{13}}$(total)
4	0.101	0.149	0.0%	0.14%	0.14%
6	0.066	0.183	0.16%	0.11%	0.18%

3.2.2 Location uncertainties

To assess the effect on the uncertainties $\delta_{L_{i,j}}$ on the reactor fluxes, we recall eq. (23) and take the derivative

$$\frac{\partial \rho_i}{\partial L_{i,j,\mathrm{Far}}} = -\frac{2\rho_i \phi_j}{L_{i,j,\mathrm{Far}}^3 \sum_{j'=1}^{6} \frac{\phi_{j'}}{L_{i,j',\mathrm{Far}}^2}} \approx -\frac{2\rho_i}{L_{i,j,\mathrm{Far}}^3 \sum_{j'=1}^{6} \frac{1}{L_{i,j',\mathrm{Far}}^2}} \equiv \rho_i B_{ij,\mathrm{Far}}, \qquad (32)$$

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and similarly,

$$\frac{\partial \rho_i}{\partial L_{i,j,\text{Near}}} = \frac{2\rho_i \phi_j}{L_{i,j,\text{Near}}^3 \sum_{j'=1}^{6} \frac{\phi_{j'}}{L_{i,j',\text{Near}}^2}} \approx \frac{2\rho_i}{L_{i,j,\text{Near}}^3 \sum_{j'=1}^{6} \frac{1}{L_{i,j',\text{Near}}^2}} \equiv \rho_i B_{ij,\text{Near}}, \tag{33}$$

where we suppose that all 6 reactor fluxes ϕ_j are close to a common value ϕ.

The dependence of the measurement (23) of $\sin^2 2\theta_{13}$ on the ratios ρ_i is such that the contribution to its uncertainty due to the uncertainty in the distances $L_{i,j}$ is

$$
\begin{aligned}
\delta_{\sin^2 2\theta_{13}} &= \sqrt{\sum_{i=1}^{8}\sum_{j=1}^{6}\left(w_i \frac{\partial \rho_i}{\partial L_{i,j,\text{Far}}}\delta_{L_{i,j,\text{Far}}}\frac{N_i^{\text{Far}}}{N_i^{\text{Near}}}\right)^2 + \left(w_i \frac{\partial \rho_i}{\partial L_{i,j,\text{Near}}}\delta_{L_{i,j,\text{Near}}}\frac{N_i^{\text{Far}}}{N_i^{\text{Near}}}\right)^2} \\
&\approx \sqrt{\sum_{i=1}^{8}\sum_{j=1}^{6}\left(w_i B_{ij,\text{Far}}\delta_{L_{i,j,\text{Far}}}\rho_i \frac{N_i^{\text{Far}}}{N_i^{\text{Near}}}\right)^2 + \left(w_i B_{ij,\text{Near}}\delta_{L_{i,j,\text{Near}}}\rho_i \frac{N_i^{\text{Far}}}{N_i^{\text{Near}}}\right)^2} \\
&\approx \sqrt{\sum_{i=1}^{8}\sum_{j=1}^{6}\left(w_i B_{ij,\text{Far}}\delta_{L_{i,j,\text{Far}}}\right)^2 + \left(w_i B_{ij,\text{Near}}\delta_{L_{i,j,\text{Near}}}\right)^2} \\
&\approx \delta_L \sqrt{\sum_{i=1}^{8}\sum_{j=1}^{6}\left(w_i B_{ij,\text{Far}}\right)^2 + \left(w_i B_{ij,\text{Near}}\right)^2}, \tag{34}
\end{aligned}
$$

assuming that the uncertainty in all distances is that same, namely δ_L.

The location of the reactor cores will be determined to a precision of about 30 cm. We assume that the location *uncertainties* $\delta_{L_{i,j}}$ are uncorrelated. The resulting *uncertainty* in *the measurement of* $\sin^2 2\theta_{13}$ is shown in Table 3.3.

3.2.3 *Spent-fuel uncertainties*

There is a small contribution to the antineutrino flux at the Day Bay site due to radioactive decays in the spent fuel of the reactors. This contribution is not expected to exceed 0.1% of the total flux, and is neglected in the present considerations.

3.3 *Detector-related uncertainties*

The various properties of the detectors relevant to the measurement of $\sin^2 2\theta_{13}$ *have been combined into the detector factors* K_i *in the formalism of sec. 3.1. If the K factors are independent of time (and are unchanged during detector "swaps") no knowledge of these factors is needed in the measurement. However, if there is an unknown relative variation δ_K/K in the detector factor for the two locations of each detector, then there is a contribution to the uncertainty $\delta_{\sin^2 2\theta_{13}}$ of this amount when all 8 detectors have the same (correlated) variation. If the variation is uncorrelated in the different detectors then the effect on the measurement is reduced to $\delta_{\sin^2 2\theta_{13}} = \delta_K/\sqrt{8}K$.*

For the detector-related *uncertainties*, we consider the CHOOZ results as a reference, and then compute *two* values for the Daya Bay case: baseline and goal. The baseline value is *what* we expect to be achievable through essentially proven methods with perhaps straightforward improvement in technique. The goal value is *what* we consider reachable through improved methods and extra care beyond the level of previous experiments of this type. The results are summarized in Table 3.4 and discussed in the rest of this section.

3.3.1 **Target mass**

The antineutrino targets are the free protons in the detector, so the event rate in the detector is proportional to the total mass of free protons. The systematic *uncertainty* in this quantity is *minimized* by precise

Source of *uncertainty*		CHOOZ	Daya Bay	
			Baseline	Goal
# protons	Mass (20 tons)	–	0.005	0.001
	H/C ratio (Gd)	0.8	0.2	0
	H/C ratio (γ)	0.8	0.03	0
Detector Efficiency	H/Gd ratio	1.0	0.1	0
	e^+ energy cut	0.8	0.2	0.05
	n energy cut	?	0.013	0.013
	Position cuts	0.32	0	0
	Time cuts	0.4	0.1	0.03
	n multiplicity	0.5	0.05	0.01
	Trigger	0	0.01	0.01
	Live time	0	< 0.01	< 0.01
Total detector-related uncertainty		1.7%	0.38%	0.15%

Table 3.4. Comparison of detector-related systematic uncertainties (all in percent, per detector module) of CHOOZ experiment and projections for *the Daya Bay experiment*. Baseline values for *the Daya Bay experiment* are achievable through essentially proven methods, whereas the goals should be attainable through additional efforts described in the text.

measurement of the relative total mass of the central volumes of the detector modules, as well as by filling the modules from a common batch of scintillator liquid so that the H/C ratio is the same to high precision.

Knowledge of the absolute volume of the detectors modules is not essential. The detector modules will be built to specified tolerance so that the volume is known to $\sim 0.1\%$ (typically <1 mm dimension out of several meters). We will make measurements of these volumes after construction to characterize them to higher precision than 0.1%. The thermal expansion coefficient of acrylic plastic is about $10^{-4}/^\circ C$, so temperature-induced volume changes can be known to 0.1% if the temperature is know to $3^\circ C$.

The mass of the central detector *will be* accurately determined in several ways. *The initial mass will be deduced from measurements, using precision flowmeters with a repeatability specification of 0.02%, of the fluid flow during filling from a common stainless steel tank at a controlled constant temperature. We will Several flowmeters will be run in series for redundancy.*

The thermal expansion coefficient of the mineral-oil-based liquid scintillator is about $7 \times 10^{-4}/^\circ C$, so the mass of a fixed volume of liquid scintillator would not be constant to 0.1% unless its temperature were constant to $0.3^\circ C$, which is unlikely to be the case. It will also be difficult to know the temperature throughout the detector volume to this accuracy. Rather, the detector volume will be connected to a buffer tank, and the resulting temperature-dependent flow between the two monitored via precision flowmeters. Then the difference in the volume/mass of the liquid in the detector between the initial fill and any later time can be deduced. If the temperature excursions are, say, $2^\circ C$, then the relative mass change is about 0.4%, corresponding to 80 kg out of 20 tons of liquid transferred to the buffer tank. If we measure this 80 kg to an accuracy of 1 kg, then we know the relative mass of the liquid in the detector to an accuracy of 0.005%.

3.3.2 *H/C ratio*

The relevant target mass for the Daya Bay experiment is not that of the liquid scintillator, but that of the free protons in the scintillator. Recent studies indicate that it should be possible to measure the number of free protons per kg of scintillator (loosely called the H/C ratio) to an absolute accuracy of 0.3% based on combustion and analysis of samples of the scintillator. The CHOOZ experiment[8] reported an accuracy of 0.8% for their use of this technique.

The difficulty in obtaining precise knowledge as to the number of free protons per kg of scintillator suggests that the experiment should avoid the need for this knowledge by insuring that the scintillator samples in all detectors (or at least in "swapped" pairs of detectors) are the same. This requires buffer storage tanks for the liquid scintillator of size 40-160 tons, and a scheme for pumping the scintillator from the buffer tanks into the detectors. We take this as the "goal", and regard the "baseline" as a scheme in which the scintillator in different detectors is not guaranteed to be identical, and so the free-proton content must be measured. The baseline accuracy of our knowledge of the free-proton content is 0.2%, which is somewhat better than has been achieved to date.

We are presently engaged in a program of R&D with the goal of measuring the *relative* H/C ratio in different samples of liquid scintillator to $\sim 0.1\%$ precision. We are exploring two different methods the achieve this goal: precision NMR and neutron capture. The *neutron-capture* method would need to be utilized before the introduction of Gd into the scintillator, but could be used to *characterize precisely* the organic liquids used in the *liquid-scintillator* cocktail. In principle, the NMR method could be used on the final Gd-loaded scintillator.

Each detector includes 30 tons of undoped liquid scintillator in the so-called γ-catcher, as well as 20 tons of Gd-loaded liquid scintillator. Antineutrino interactions in the γ-catcher can result in the detection of "spill-in" neutrons in the Gd-doped liquid scintillator after thermal diffusion, whose characteristic length is 5 cm. Need a good number here. *Since the γ-catcher is 50 cm thick, about 10% of its mass, some 3 tons, contributes to the effective target mass of the experiment. This is about 1/6 of the total target mass, so the requirement of knowledge of the free-proton content in the γ-catcher is about 6 times larger than that for the Gd-load scintillator, namely 1.2%. In practice, the same techniques of analysis can be applied to the $gamma$-catcher scintillator as to the Gd-loaded scintillator, with the same resulting accuracy as to our knowledge of the free-proton content.*

The "goal" is that γ-catcher scintillator be identical in all 8 detectors, as could be arranged by use of another buffer storage tank of 250 tons.

If the free-proton content in the γ-catcher scintillator is to be linked to that in the Gd-loaded scintillator, then the entire mass of $8 \times (20 + 30) = 400$ tons of liquid scintillator must be prepared in a single large tank before 160 tons are moved to a second tank where the Gd is added. This option may not be realizable, and the γ-catcher scintillator and the Gd-doped scintillator will likely be prepared separately. In this case, we must measure the relative free-proton content in both types of scintillators.

3.3.3 H/Gd ratio

Neutrons *from inverse β decay* are thermalized during their first 10 μs of existence in the detector central volume. *For* times longer than *this* the *thermal neutrons are captured by Gd nuclei producing a detectable signal of $\approx$ 8 MeV of secondary γ's, or they are captured by free protons producing a 2-MeV γ that falls below the neutron-energy cut of about 6 MeV.*

The rate Γ of *delayed* capture *of thermal neutrons* is given by: Elements in Roman, not italic.

$$\Gamma = \Gamma_{\mathrm{Gd}} + \Gamma_{\mathrm{H}} = [N_{\mathrm{Gd}}\sigma_{\mathrm{Gd}} + N_{\mathrm{H}}\sigma_{\mathrm{H}}]v_n \,, \tag{35}$$

where N_{Gd} and N_{H} are the number densities of gadolinium and free protons, respectively, σ_{Gd} and σ_{H} are the thermal-neutron capture cross sections, and v_n is the velocity of the thermal neutron. The expected values are $\tau_{\mathrm{H}} = 1/\Gamma_{\mathrm{H}} = 180 \ \mu s$, $\tau_{\mathrm{Gd}} = 1/\Gamma_{\mathrm{Gd}} = 36 \ \mu s$, and $\tau = 1/\Gamma = 30 \ \mu s$. The fraction of *thermal* neutrons that *are captured by* Gd rather than H is then

$$f_{\mathrm{Gd}} = \frac{\Gamma_{\mathrm{Gd}}}{\Gamma} = \frac{\tau_{\mathrm{H}} - \tau}{\tau_{\mathrm{H}}} \approx \frac{5}{6} \,. \tag{36}$$

If all detectors are filled with a common batch of Gd-loaded liquid scintillator, we do not need to know the fraction f_{Gd} to measure $\sin^2 2\theta_{13}$. However, if different detectors are filled with different batches of scintillator, then the uncertainty in the ratio of the fractions f_{Gd} for different detectors leads to an uncertainty

in $\sin^2 2\theta_{13}$ of the same amount. Defining $R = f_1/f_2$ to be the ratio of the fractions f_{Gd} for two detectors, whose neutron-capture times are τ_1 and τ_2, we have

$$R = \frac{f_1}{f_2} = \frac{\tau_{\mathrm{H}} - \tau_2}{\tau_{\mathrm{H}} - \tau_1}, \qquad \text{and} \qquad \frac{\delta_R}{R} = \sqrt{2}\frac{\delta_\tau}{\tau_{\mathrm{H}} - \tau} \approx \frac{\delta_\tau}{100\,\mu s}, \tag{37}$$

where $\delta_\tau = \delta_{\tau_1} = \delta_{\tau_2}$ is the uncertainty on our knowledge of the capture times τ_1 and τ_2.

We set the baseline requirement of $\delta_R/R = 0.001$, which requires that the neutron-capture times be measured to an accuracy of $\delta_\tau = 0.1\,\mu s$, or $\delta_\tau/\tau = 1/300$. Such a measurement requires measuring about *100,000* neutron captures, which can be done in a few minutes with a neutron source.

The CHOOZ experiment[8] measured the (*absolute*) capture time τ to *a precision of* $0.5\,\mu s$.

3.3.4 *Positron and neutron energy cuts*

In the analysis of inverse β decays, cuts will be placed on the observed energies of both the positron and the γ's from delayed-neutron capture.

Positrons generate a minimum energy of 1.022 MeV upon annihilation, with an energy spectrum as shown in Fig. 3.3, with the full spectrum shown in the inset. Also shown is a GEANT simulation of the observed energy in a 20-ton detector module instrumented with 200 PMTs such that the reconstructed energy resolution is ~ 15% at 1 MeV. The inefficiencies for positron detection are 0.32%, 0.37%, and 0.43% for cuts at 0.98 MeV, 1.0 MeV, and 1.02 MeV, respectively.
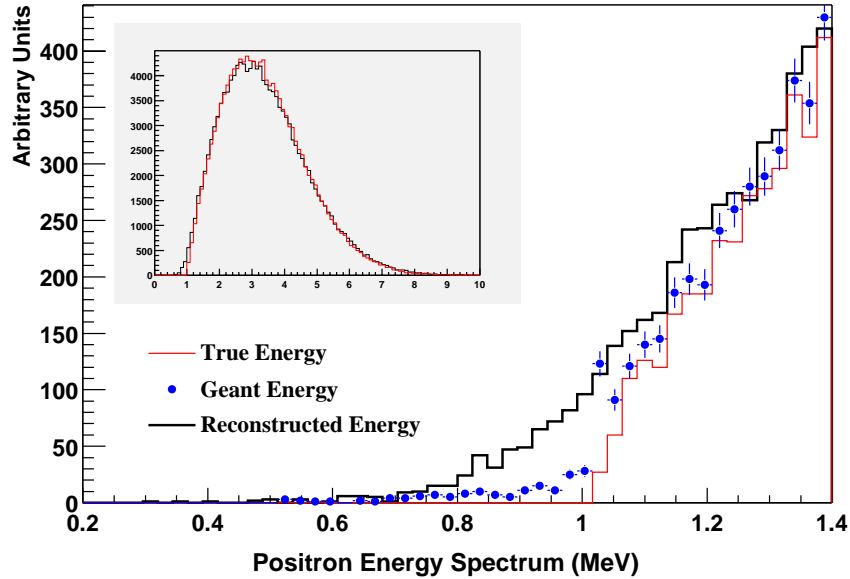

Fig. 3.3. Spectra of the energy of positrons from antineutrino interactions for true, simulated (GEANT), and reconstructed energy at around 1 MeV. The full spectrum is shown in the inset, where the red line corresponds to the true energy and the black one corresponds to the reconstructed energy.

Our goal is a positron-energy scale error is 2% at 1 MeV, in which case the uncertainty in the true position of the positron energy cut produces a 0.05% error in the detected antineutrino rate. The baseline positron-energy scale error is 8% at 1 MeV, which contributes an uncertainty of 0.2% to our sensitivity to $\sin^2 2\theta_{13}$.

There is no motivation for the stated value of the positron energy-scale uncertainty. The baseline value of 8% results in one of the largest systematic errors in the experiment. Shouldn't we at least discuss what it takes to do better on this?

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For comparison, the CHOOZ experiment[8] employed a positron energy cut of 1.3 MeV., which resulted in an estimated uncertainty of 0.8% on their sensitivity to $\sin^2 2\theta_{13}$.

The use of a positron energy cut at 1 MeV will be possible in the Daya Bay experiment because the oil-buffer around the PMTs and the large water pool surrounding each detector suppresses backgrounds of γ's above 1 MeV from radioactivity in the detector and its environment to 0.1% of the rate of positrons from antineutrinos.

The capture of a thermalized neutron from inverse β decay on a Gd nucleus leads the emission of several soft γ's whose combined energy spectrum peaks about 8 MeV, as shown in Fig. 3.4. An energy threshold of about 6 MeV will be employed to select these delayed events. The variation of efficiency of this selection will be monitored via calibration of the detector energy response using radioactive sources (see Chapter 8) and spallation-neutron captures. We intend to calibrate the detector modules with a precision comparable to that in the KamLAND experiment[12] where the detector gain is routinely monitored with sources (every 2 weeks), and a relative long-term gain drift of $\sim 1\%$ is readily monitored with a precision of 0.05%. According to our Monte Carlo simulations, an energy-scale uncertainty of 0.05% at 6 MeV results in a 0.013% uncertainty in the neutron detection efficiency.
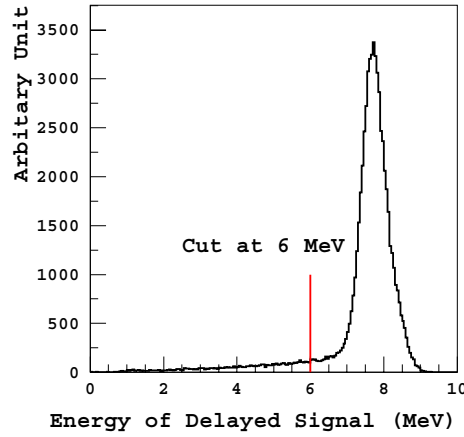

Fig. 3.4. GEANT3 simulation of the spectrum of the energy of γ's from the capture of a thermal neutron by a Gd nucleus. The simulation includes a detector module with 200 PMT's and 20 tons of Gd-loaded liquid scintillator surrounded by a 45-cm thick γ-catcher.

3.3.5 Position and time cuts

We do not anticipate employing cuts on reconstructed position to select events.

However, the time correlation of the prompt (positron) event and the delayed (neutron) event is a critical aspect of the event signature. Matching the time delays of the start and end times of this time window between detector modules is crucial to reducing systematic uncertainties associated with this aspect of the antineutrino signal. If the starting time ($\sim 0.3\ \mu s$) and ending time ($\sim 200\ \mu s$) of the delayed event window are determined to ~ 10 ns precision, the resulting uncertainty associated with the lost-event fraction is $\sim 0.03\%$. We will insure that this timing is equivalent for different detector modules by slaving all detector electronics to one master clock. We estimate that with due care, the relative neutron efficiency for different modules due to timing is known to $\sim 0.03\%$.

3.3.6 Neutron multiplicity

Cosmic-ray muons can lead to spallation reactions in which multiple neutrons are detected in Gd-loaded

scintillator. If the muon and hadronic shower associated with these neutrons is not tagged by the muon-veto system, then a cut on neutron multiplicity in the central detector can further suppress this background. We estimate the uncertainty on the measurement of $\sin^2 2\theta_{13}$ from this cut by scaling from the CHOOZ experiment[8]. For the *Daya Bay* near site at 500 m baseline, the muon rate relative to the signal rate will be more than a factor 9 lower than for the CHOOZ site. Therefore, *the uncertainty due to the cut on events with multiple neutron signals will be reduced by this factor relative to CHOOZ, as indicated in Table 3.4.*

3.3.7 Trigger

The trigger efficiency will be measured using studies with pulsed light sources in the detector. Through a series of careful measurements we should be able to measure the trigger efficiency of each detector system to high precision, 0.01%. (KamLAND has used this method to determine 99.8% absolute trigger efficiency[22].)

3.3.8 Live time

The detector live time can be measured accurately by counting a 100 MHz clock using the detector electronics, and normalizing to the number of clock ticks in a second (as defined by a GPS receiver signal). The uncertainty associated with this procedure should be extremely small, and certainly negligible relative to the other systematic *uncertainties.* For example, SNO measured the relative live times for their day/night analysis with a relative fractional uncertainty of 5×10^{-7}.

3.4 Backgrounds

In the Daya Bay experiment, the signal events (inverse beta decay reactions) have a distinct signature of two time-ordered signals: a prompt positron signal followed by a delayed neutron-capture signal. Backgrounds can be classified into two categories: correlated and uncorrelated backgrounds. If a background event is triggered by two signals that come from the same source, such as those induced by the same cosmic muon, it is a correlated background event. On the other hand, if the two signals come from different sources but satisfy the trigger requirements by chance, the event is an uncorrelated background.

There are three important sources of backgrounds in the Daya Bay experiment: fast neutrons, ^{8}He/ ^{9}Li, and natural radioactivity. A fast neutron produced by cosmic muons in the surrounding rock or the detector can produce a signal mimicking the inverse beta decay reaction in the detector: the recoil proton generates the prompt signal and the capture of the thermalized neutron provides the delayed signal. The ^{8}He/ ^{9}Li isotopes produced by cosmic muons have substantial beta-neutron decay branching fractions, 16% for ^{8}He and 49.5% for ^{9}Li. The beta energy of the beta-neutron cascade overlaps the positron signal of neutrino events, simulating the prompt signal, and the neutron emission forms the delayed signal. Fast neutrons and ^{8}He/ ^{9}Li isotopes create correlated backgrounds since both the prompt and delayed signals are from the same single parent muon. Some neutrons produced by cosmic muons are captured in the detector without proton recoil energy. A single neutron capture signal has some probability to fall accidentally within the time window of a preceding signal due to natural radioactivity in the detector, producing an accidental background. In this case, the prompt and delayed signals are from different sources, forming an uncorrelated background.

All three major backgrounds are related to cosmic muons. Locating the detectors at sites with adequate overburden is the only way to reduce the muon flux and the associated background to a tolerable level. The overburden requirements for the near and far sites are quite different because the signal rates differ by more than a factor of 10. Supplemented with a good muon identifier outside the detector, we can tag the muons going through or near the detector modules and reject backgrounds efficiently.

In this section, we describe our background studies and our strategies for background management. We conclude that the background-to-signal ratio will be around 0.5% at the near sites and around 0.2% at the far site, and that the major sources of background can be quantitatively studied *in-situ*.

3.4.1 Cosmic muons at underground laboratories

The most effective and reliable approach to minimize the backgrounds in the Daya Bay experiment is to have sufficient amount of overburden over the detectors. The Daya Bay site is particularly attractive because it is located next to a 700-m high mountain. The overburden is a major factor in determining the optimal detector sites. The location of detector sites has been optimized by using a global χ^2 analysis described in section 3.5.1.

Detailed simulation of the cosmogenic background requires accurate information of the mountain profile and rock composition. Fig. 3.5 shows the mountain profile converted from a digitized 1:5000 topographic map. The horizontal tunnel and detector sites are designed to be about 10 m below sea level. Several rock samples at different locations of the Daya Bay site were analyzed by two independent groups. The measured rock density ranges from 2.58 to 2.68 g/cm^3. We assume an uniform rock density of 2.60 g/cm^3 in the present background simulation.
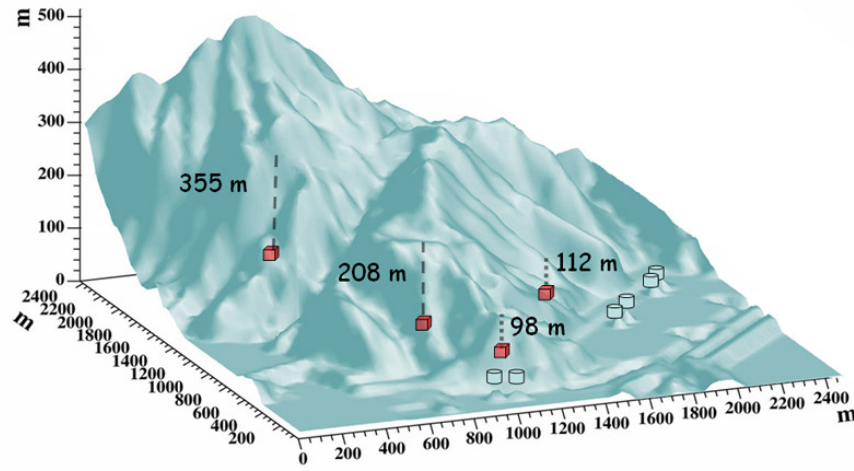

Fig. 3.5. Three dimensional profile of Pai Ya Mountain generated from a 1:5000 topographic map of the Daya Bay area.

The standard Gaisser formula is known to poorly describe the muon flux at large zenith angle and at low energies. This is relevant for the Daya Bay experiment since the overburden at the near sites is only ~ 100 m. We modified the Gaisser formula[3] to describe the muon flux at the sea level. The comparison of the modified formula with data is shown in Fig. 3.6, where the calculations with the standard Gaisser formula are also shown. At muon energies of several tens of GeV, the standard Gaisser formula has large discrepancies with data while the modified formula agrees with data in the whole energy range.

Using the mountain profile data, the cosmic muons are transported from the atmosphere to the underground detector sites using the MUSIC package[2]. Simulation results are shown in Table 3.5 for the optimal detector sites. The muon energy spectra at the detector sites are shown in Fig. 3.7. The four curves from upper to lower corresponds to the Daya Bay near site, the Ling Ao near site, the mid site and the far site, respectively.

3.4.2 Simulation of neutron backgrounds

The neutron production rates will depend upon the cosmic muon flux and average energy at the detector. However, the neutron backgrounds in the detector also depend on the local detector shielding. The neutrino detectors will be shielded by at least 2 meters of water. The veto water will be used as a Cerenkov detector to detect muons. Thus neutrons produced by muons in the detector module or the water shield will be identified by the muon signal in the water veto detector. In addition, neutrons created by muons in the surrounding rock will be effectively attenuated by the 2 m water shield. Together with another muon tracker outside the
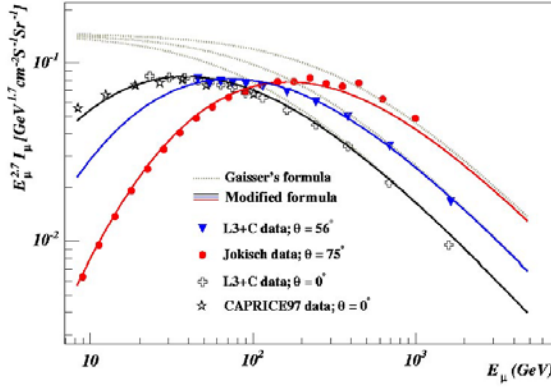
Fig. 3.6. Comparison of the modified formula (solid lines) with data. Calculations with the standard Gaisser's formula are shown in dashed lines. The data are taken from Ref.[5,6].
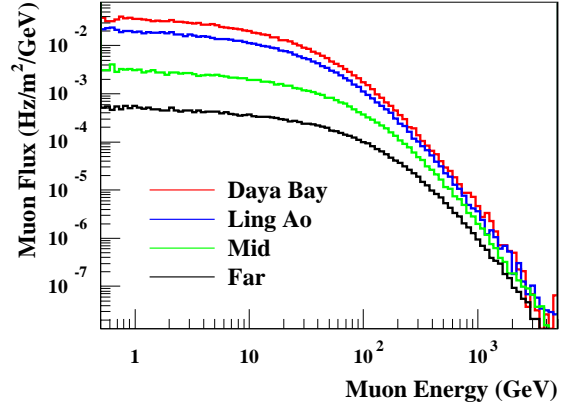

Fig. 3.7. Muon flux as a function of the energy of the surviving muons. The four curves from upper to lower corresponds to the Daya Bay near site, the Ling Ao near site, the mid site and the far site, respectively.

	DYB site	LA site	Mid site	Far site
Vertical overburden (m)	98	112	208	355
Muon Flux (Hz/m^2)	1.16	0.73	0.17	0.041
Muon Mean Energy (GeV)	55	60	97	138

Table 3.5. Vertical overburden of the detector sites and the corresponding muon flux and mean energy.

veto water, the combined muon tag efficiency is designed to be 99.5%, with an uncertainty smaller than 0.25%.

With the detailed muon flux and mean energy at each detector site, the neutron yield, energy spectrum, and angular distribution can be estimated with an empirical formula[7] which has been tested against experimental data whenever available. A full Monte Carlo simulation has been carried out to propagate the primary neutrons produced by muons in the surrounding rocks and the water buffer to the detector. The primary neutrons are associated with their parent muons in the simulation so that we know if they can be tagged by the veto detector. All neutrons produced in the water buffer will be tagged with an efficiency of 99.5%, since their parent muons must pass through the muon systems. About 30% of the neutrons produced in the surrounding rocks cannot be tagged. The neutrons produced in the rocks, however, have to survive at least 2 meters of water. The neutron background after veto rejection is the sum of the untagged events and 0.5% of the tagged events.

Some energetic neutrons will produce tertiary particles, including neutrons. For those events that have energy deposited in the liquid scintillator, quite a lot of them have a complex time structure due to multiple neutron scattering and captures. These events are split into sub-events in 50 ns time bins. We are interested in two kinds of events. The first kind has two sub-events. The first sub-event has deposited energy in the range of 1 to 8 MeV, followed by a sub-event with deposited energy in the range of 6 to 12 MeV in a time window of 1 to 200μs. These events, called fast neutron events, can mimic the antineutrino signal as correlated backgrounds. The energy spectrum of the prompt signal of the fast neutron events, e.g. at the far site, is shown in Fig. 3.8 up to 50 MeV. The other kind of events has only one sub-event with deposited

energy in range of 6 to 12 MeV. These events, when combined with the natural radioactivity events, can provide the delayed signal to form the uncorrelated backgrounds. We call them single neutron events. The neutron simulation results are listed in Table 3.6.

		DYB site	LA site	far site
fast neutron	vetoed	57.8	45.6	3.8
(/day/module)	not vetoed	0.83	0.64	0.08
single neutron	vetoed	1365	1070	94.7
(/day/module)	not vetoed	27.2	21.0	2.1

Table 3.6. Neutron rates in a 20-ton module at the Daya Bay sites. The rows labeled "vetoed" refer to the case where the parent muon track traversed the veto detectors, and thus it could be tagged. Rows labeled "not vetoed" refer to the case where the muon track did not traverse the veto detectors. (numbers to be updated.)
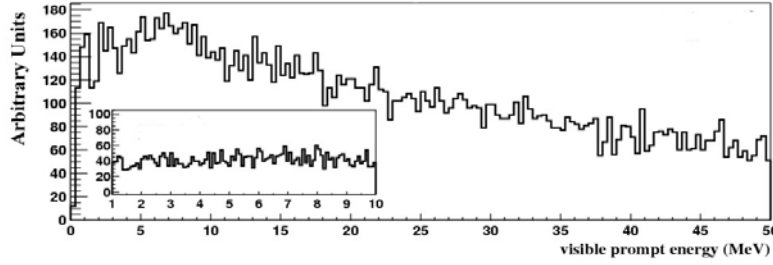

Fig. 3.8. The prompt energy spectrum of fast neutron backgrounds at the Daya Bay far detector. The inset is an expanded view of the spectrum from 1 to 10 MeV.

The rate and energy spectrum of the fast neutron backgrounds can be studied with the tagged sample, which is 200 times larger than the untagged one.

3.4.3 Cosmogenic isotopes

Cosmic muons, even if they are tagged by the muon identifier, can produce radioactive isotopes in the detector scintillator which decay by emitting both a beta and a neutron (β-neutron emission isotopes). Some of these so-called cosmogenic radioactive isotopes live long enough such that their decay cannot be reliably associated with the last vetoed muon. Among them, ^{8}He and ^{9}Li with half-lives of 0.12 s and 0.18 s, respectively, constitute the most serious correlated background sources. The production cross section of these two isotopes has been measured with muons at an energy of 190 GeV at CERN[11]. Their combined cross section is $\sigma(^9\text{Li} +^8 \text{He}) = (2.12 \pm 0.35)\mu\text{barn}$. Since their lifetimes are so close, it is hard to get their individual cross sections. About 16% of ^{8}He and 49.5% of ^{9}Li will decay by β-neutron emission. Using the muon flux and mean energy given in last section at the detector sites and an energy dependence of the cross section, $\sigma_{\text{tot}}(E_\mu) \propto E_\mu^\alpha$, with $\alpha = 0.74$, the ^{8}He+^{9}Li backgrounds are estimated to be

	DYB site	LA site	Far site
(^{8}He+^{9}Li)/day/module	3.7	2.5	0.26

The KamLAND experiment measures this ^{9}Li/ ^{8}He background very well by fitting the time since last muon. The muon rate is 0.3 Hz in the active volume of KamLAND detector. The mean time interval of successive muons is 5 seconds, much longer than the lifetimes of ^{9}Li/ ^{8}He. For the Daya Bay experiment,

the target volume of a 20 ton detector module has a cross section around 10 m^2, thus the muon rate is around 10 Hz at the near sites, resulting in a mean time interval of successive muons shorter than the lifetimes of ^{9}Li/^{8}He. With a modified fitting algorithm, we find that it is still feasible to measure the isotope background *in-situ*.

From the decay time and β-energy spectra fit, the contribution of ^{8}He relative to that of ^{9}Li was determined by KamLAND to be less than 15% at 90% confidence level[12]. Furthermore, the ^{8}He contribution can be identified by tagging the double cascade ^{8}He $\rightarrow^8$Li $\rightarrow^8$Be. So we assume that all isotope backgrounds are ^{9}Li. They can be determined with a maximum likelihood fitting even at 10 Hz muon rate, by taking all contributions from the preceding muons into account. The resolution of the background-to-signal ratio can be determined to be[13]

$$\sigma_b = \frac{1}{\sqrt{N}} \cdot \sqrt{(1 + \tau R_\mu)^2 - 1}, \tag{38}$$

where N is the total number of neutrino candidates, τ is the lifetime of ^{9}Li, and R_μ is the muon rate in the target volume of detector. The resolution is insensitive to the ^{9}Li level since the statistical fluctuation of neutrino events dominates the uncertainty. The background-to-signal ratio of ^{9}Li background can be measured to $\sim 0.3\%$ with two 20-ton modules at the near sites of the Daya Bay experiment and $\sim 0.1\%$ at the far site with four 20-ton modules, with the data sample of three years of running. The fitting uses time information only. Inclusion of energy and vertex information could further improve the precision.

A Monte Carlo has been carried out to check the fitting algorithm. The background-to-signal ratio is fixed at 1%. The total number of neutrino candidates is 2.5×10^5, corresponding to the far site statistical error, 0.2%. Fig. 3.9 shows the fitting results as a function of muon rate. The data sample generation and fitting were performed 400 times for each point to get the fitting precision. In Fig. 3.10 the fitting precision is compared to the analytic formula Eq. 38 with the same Monte Carlo samples. The Monte Carlo results for minimizing χ^2, the maximum likelihood fit, and the simple analytical estimation are in excellent agreement.
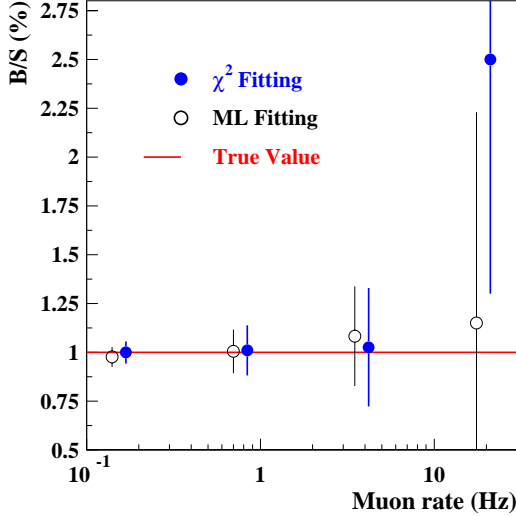

Fig. 3.9. Fitting results as a function of the muon rate. The error bars show the precision of the fitting. The χ^2 fitting uses the same muon rate as ML fitting but shown on the right of it.
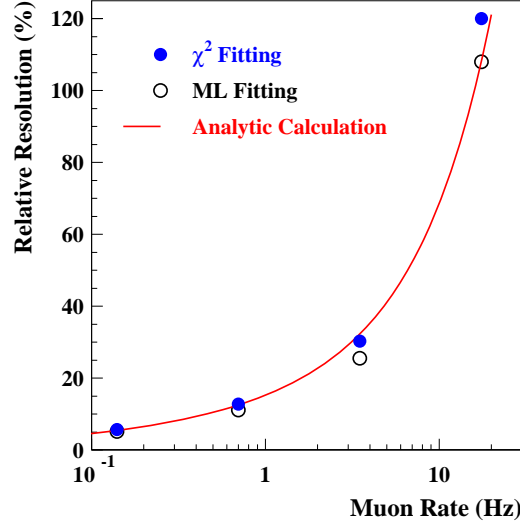
Fig. 3.10. The fitting precision as a function of the muon rate, comparing with the analytic estimation of Eq. 38. The y-axis shows the relative resolution of the background-to-signal ratio.

KamLAND also found that most (perhaps all) ^{8}He/^{9}Li background are produced by showering muons[12]. A 2-second veto of the whole detector is applied at KamLAND to reject these backgrounds. Roughly 3% of cosmic muons shower in the detector. It is not feasible for Daya Bay to apply a 2-second veto since the dead time of the near detector would be more than 50%. However, if the Daya Bay detector is vetoed for 0.5 s after a showering muon, about 85% isotope backgrounds caused by shower muons can be rejected. Approximately 30% of the ^{8}He/^{9}Li background will remain: $\sim 15\%$ from non-showering muons and $\sim 15\%$ from showering muons. Although additional *uncertainties* may be introduced due to the uncertainties in the relative contributions from showering and non-showering muons and the uncertainties arising from the additional cuts (e.g., increased dead time), this rejection method can cross check the fitting method and firmly determine the background-to-signal ratio to 0.3% at the near sites and to 0.1% at the far site.

3.4.4 Radioactivity

Natural radioactivity and the single neutron events induced by cosmic muons may occur within a given time window accidentally to form an uncorrelated background. The coincidence rate is given by $R_\gamma R_n \tau$, where R_γ is the rate of natural radioactivity events, R_n is the rate of spallation neutron, and τ is the length of the time window. With the single neutron event rate given in previous section, the radioactivity should be controlled to 50 Hz to limit the accidental backgrounds $< 0.1\%$. The accidental backgrounds can be well determined *in-situ* by measurement of the individual single rates from radioactivity and the single neutrons. The energy spectrum can be also well determined.

Past experiments suppressed uncorrelated backgrounds with a combination of using carefully selected construction materials, self-shielding, and using absorbers that have large neutron capture cross section. However, additional care is necessary to lower the detector energy threshold much below 1 MeV. A higher threshold will introduce a systematic error in the efficiency of detecting the positron. In the following, the singles rate is the radioactivity of > 1 MeV visible energy in detector.

Radioactive background can come from a variety of sources:

○ U/Th/K in the rocks around the detector hall.

○ U/Th/K in the veto water.

○ ^{60}Co in the detector vessel and other supporting structures.

○ U/Th/K in the PMT glass.

○ U/Th/K in the scintillator.

○ U/Th/K in materials used in the detector.

○ Radon in air.

○ Cosmic rays.

The radioactivity of the rock samples from the Daya Bay site have been measured by several independent groups. The concentration is ~ 10 ppm for ^{238}U, ~ 30 ppm for ^{232}Th, and ~ 5 ppm for ^{40}K. The rock radioactivity has been studied with Monte Carlo. With the shielding of 2-meter veto water and 45 cm oil buffer, there are 5 Hz, 20 Hz, and 2 Hz singles rate of visible energy greater than 1 MeV at each center detector module, for U/Th/K respectively. The total rate is ~ 27 Hz.

The geological environment and rock composition are very similar for Hong Kong and Daya Bay. The spectrum of the natural radioactivity of the rocks in the Aberdeen Tunnel in Hong Kong is shown in Fig. 3.11.

The veto water will be circulated and purified to achieve enough attenuation length for water Cerenkov light as well as low radioactivity. KamLAND veto water has 1 ppb ^{238}U, 1 ppb ^{232}Th, and also 1 ppb ^{40}K. Assuming the same concentration, the veto water will contribute 1.8 Hz, 0.4 Hz, and 6.3 Hz single rates from U/Th/K, respectively.
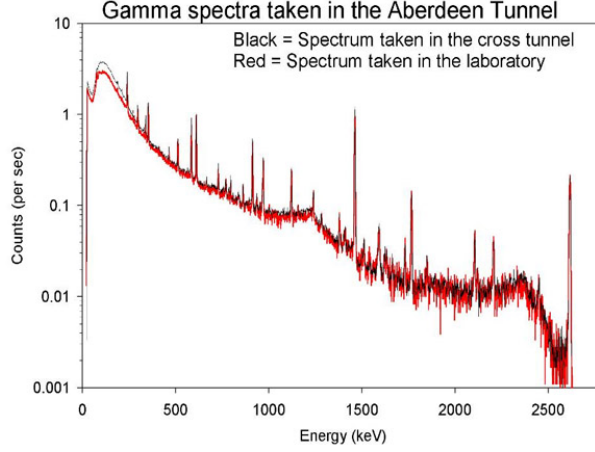
Fig. 3.11. Spectrum of natural radioactivity measured with a Ge crystal in the Hong Kong Aberdeen Tunnel.

The ^{60}Co in stainless steel varies from batch to batch and should be measured before use as detector material, such as the outer vessel. Conservatively, assuming 1 pCi/kg ^{60}Co in the outer vessel, the single rates will be $\sim$ 6 Hz.

A potential PMT candidate is the Hamamatsu R5912 with low radioactivity glass. The concentrations of ^{238}U and ^{232}Th are both less than 40 ppb in the glass, and that of ^{40}K is 25 ppb. The Monte Carlo study shows that the single rate is 2.2 Hz, 1 Hz, 4.5 Hz for U/Th/K, respectively, with 20 cm oil buffer from the PMT surface to the liquid scintillator. The total rate from the PMT glass is 7.7 Hz.

Following the design experience of Borexino and Chooz, backgrounds from impurities in the detector materials can be reduced to the required levels. The U/Th/K concentration of $10^{-12}g/g$ in liquid scintillator will contribute only 0.8 Hz of background in a 20 ton module.

Radon is one of the radioactive daughters of ^{238}U, which can increase the background rate of the experiment. The Radon concentration in the experimental halls can be kept to an acceptable level by ventilation with fresh air from outside. Since the neutrino detector modules are immersed in 2-meter thick water buffer, it is expected that the radon contribution can be safely ignored for the water pool design.

The β decay of long lived radioactive isotopes produced by cosmic muons in the scintillator will contribute a couple of Hz at the near detector, and less than 0.1 Hz at the far detector. The rate of accidental coincidence induced by muon decay or muon capture is less than the muon rate. So they can be ignored too.

3.4.5 Background subtraction error

There are other sources of backgrounds, such as cosmogenic nuclei, stopped-muon decay, and muon capture. While they are important for a shallow site, our study shows that they can be safely ignored at Daya Bay.

Assuming 99.5% muon veto efficiency, the three major backgrounds are summarized below while the other sources are negligible. In our sensitivity study, the *uncertainties* were taken to be 100% for the accidental and fast neutron backgrounds. The ^{8}He/ ^{9}Li background can be measured to an uncertainty of 0.3% and 0.1% at the near and far sites, respectively.

The rates and energy spectra of all three major backgrounds can be measured *in-situ*. Thus the backgrounds at the Daya Bay experiment are well controlled. The simulated energy spectra of backgrounds are shown in Fig. 3.4.5. The background-to-signal ratios are taken at the far site. The oscillation signal is the difference of the expected neutrino signal without oscillation and the "observed" signal with oscillation if $\sin^2 2\theta_{13} = 0.01$.

	DYB site	LA site	far site
Neutrino rate (/day/module)	930	760	90
Natural radiation (Hz)	<50	<50	<50
Single neutron (/day/module)	34	26	2.6
Accidental/Signal	<0.05%	<0.05%	<0.05%
Fast neutron/Signal	0.14%	0.1%	0.1%
^{8}He^{9}Li/Signal	0.3%	0.2%	0.2%

Table 3.7. Summary of backgrounds. The neutrino rate and single neutron rates has been applied an neutron detection efficiency of 78%.
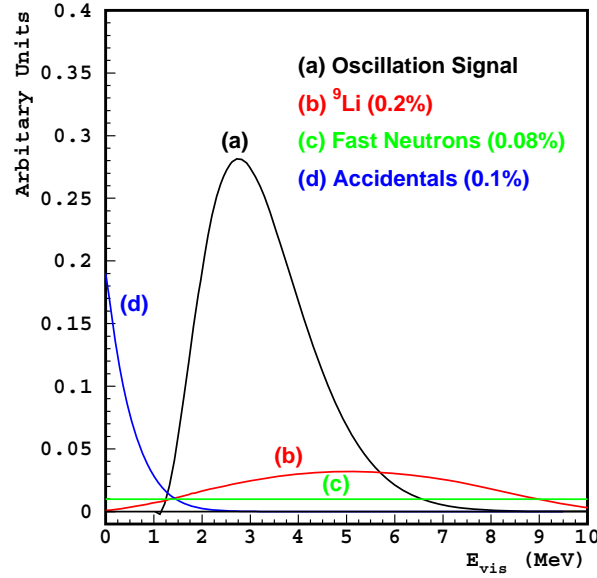

Fig. 3.12. Spectra of three major backgrounds for the Daya Bay experiment and their size relative to the oscillation signal.

3.5   Sensitivity

3.5.1   Global χ^2 analysis

If θ_{13} is non-zero, a rate deficit will be present at the far detector due to oscillation. At the same time, the energy spectra of neutrino events at the near and far detectors will be different because neutrinos of different energies oscillate at different frequencies. Both rate deficit and spectral distortion of neutrino signal will be explored in the final analysis to obtain maximum sensitivity. When the neutrino event statistics is low, say < 400 ton·GW·y, the sensitivity is dominated by the rate deficit. For luminosities higher than 8000 ton·GW·y, the sensitivity is dominated by the spectral distortion[31]. The Daya Bay experiment will have $\sim$ 3000 ton·GW·y exposure in three years, where both rate deficit and shape distortion will be important to the analysis.

Many systematic *uncertainties* will contribute to the final sensitivity of the Daya Bay experiment, and many of the *uncertainties* are correlated, which must be taken into account. A rigorous analysis of systematic *uncertainties* can be done by constructing a χ^2 function with pull terms, where the error correlations can be

introduced naturally[29–32]:

$$
\begin{aligned}
\chi^2 &= \min_{\gamma} \sum_{A=1}^{3} \sum_{i=1}^{N_{bins}} \frac{\left[M_i^A - T_i^A \left(1 + \alpha_c + \sum_r \omega_r^A \alpha_r + \beta_i + \varepsilon_D + \varepsilon_d^A \right) - \eta_f^A F_i^A - \eta_n^A N_i^A - \eta_s^A S_i^A \right]^2}{T_i^A + \sigma_{b2b}^2} \\
&+ \frac{\alpha_c^2}{\sigma_c^2} + \sum_r \frac{\alpha_r^2}{\sigma_r^2} + \sum_{i=1}^{N_{bins}} \frac{\beta_i^2}{\sigma_{\mathrm{shp}}^2} + \frac{\varepsilon_D^2}{\sigma_D^2} + \sum_{A=1}^{3} \left[\left(\frac{\varepsilon_d^A}{\sigma_d} \right)^2 + \left(\frac{\eta_f^A}{\sigma_f^A} \right)^2 + \left(\frac{\eta_n^A}{\sigma_n^A} \right)^2 + \left(\frac{\eta_s^A}{\sigma_s^A} \right)^2 \right],
\end{aligned}
\tag{39}
$$

where A sums over detectors, i sums over energy bins, and γ denotes the set of minimization parameters, $\gamma = \{\alpha_c, \alpha_r, \beta_i, \varepsilon_D, \varepsilon_d^A, \eta_f^A, \eta_n^A, \eta_s^A\}$. The γ_s are used to introduce different sources of systematic *uncertainties*. The standard deviations of the corresponding parameters are $\{\sigma_c, \sigma_r, \sigma_{\mathrm{shp}}, \sigma_D, \sigma_d, \sigma_f^A, \sigma_n^A, \sigma_s^A\}$. For each energy bin, there is a statistical error T_i^A and a bin-to-bin systematic error σ_{b2b}. For each point in the oscillation space, the χ^2 function has to be minimized with respect to the parameter γ_s.

Assuming each error can be approximated by a Gaussian, this form of χ^2 can be proven to be strictly equivalent to the more familiar covariance matrix form $\chi^2 = (M-T)^T V^{-1}(M-T)$, where V is the covariance matrix of $(M - T)$ with systematic *uncertainties* included properly[29]. The systematic *uncertainties* are described one by one in the following.

○ Reactor-related correlated error $\sigma_c \approx 2\%$. This fully correlated error will be canceled by the near-far relative measurement and has almost no impact on the sensitivity.

○ Reactor-related uncorrelated error $\sigma_r \approx 2\%$. After minimization, it contributes $\sim 0.1\%$ to the normalization of neutrino rate, as described in sec. 2.1.

○ Shape error $\sigma_{\mathrm{shp}} \approx 2\%$: Shape error is the uncertainty on neutrino energy spectra calculated from reactor information. This error is uncorrelated between different energy bins but correlated between different detectors. Since we have enough statistics at near detector to measure neutrino energy spectrum to much better than 2%, in addition to this calculation, it has little impact for Daya Bay sensitivity.

○ Detector-related correlated error $\sigma_D \approx 2\%$. Some detection *uncertainties* are common to all detectors, such as H/Gd ratio, H/C ratio, neutron capture time on Gd, and edge effect, assuming we use the same batch of liquid scintillator and identical detectors. Based on Chooz's experience, σ_D is (1 - 2)%. Like other fully correlated *uncertainties*, it has almost no impact on sensitivity.

○ Detector-related uncorrelated error $\sigma_d \approx 0.2\%$. Detector-related uncorrelated *uncertainties* include the mass of active volume, live time, etc., which do not cancel out with near-far measurement. It is estimated to be 0.36% for a single detector module. However, with detector swapping between the near and far sites, most will cancel too. Those can not cancel are mainly related with the *energy-scale* uncertainties, such as positron and neutron detection efficiency. They are estimated to be $\sim 0.2\%$.

○ Background rate error σ_f^A, σ_n^A, and σ_s^A, labeling the rate error of fast neutron, accidental backgrounds, and isotopes. They are listed in table 3.7.

○ Bin-to-bin error σ_{b2b}: Bin-to-bin error is systematic error that is uncorrelated between energy bins and uncorrelated between different detector modules. The bin-to-bin *uncertainties* normally arise from the different energy scale at different energies and uncertainties of background energy spectra during background subtraction. Up to now, the only reactor neutrino experiment that performed spectral analysis with large statistics is Bugey, which has bin-to-bin error of order of 0.5%[26,27]. With better designed detectors and much less background, we should have much smaller bin-to-bin *uncertainties* than Bugey. The bin-to-bin error can be studied by comparing the spectra of two detector modules at the same site. We will use 0.5% in the sensitivity analysis.

There are other *uncertainties* not included in the χ^2 function. 1) Due to the energy resolution, the spectra are distorted. However, the energy bins used for sensitivity analysis (~ 30 bins) is $2 \sim 6$ times larger than the energy resolution, and the distortion happens at all detectors in the same way. It has almost no impact on the final sensitivity. 2) Detector energy scale error has significant impact on detection *uncertainties* (neutron efficiency and positron efficiency). It is taken into account in σ_d. At the same time, an energy scale error will shift the whole spectrum, thus directly impacting the analysis, especially on the best fit values. However, this shift is not a distortion, and cannot mimic oscillation. It has very little impact on sensitivity computations. 3) Current knowledge on θ_{12} and Δm_{21} has around 10% *uncertainties*. Although the net oscillation effect at Daya Bay baseline is related to θ_{13} only, the subtraction of θ_{12} oscillation effects might bring *uncertainties*.

We have studied the above three sources *of uncertainty* and found none of them having a significant impact on the sensitivity of the Daya Bay experiment. For simplicity, they are ignored in our χ^2 analysis of sensitivity.

3.5.2 θ_{13} sensitivity

Fig. 3.13 shows the sensitivity contours in the $\sin^2 2\theta_{13}$ versus Δm^2_{31} plane for three years of data, using the global χ^2 analysis. The green area covers the 90% confidence region of Δm^2_{31} determined by solar neutrino experiments. Taking a design with four 20-ton modules at the far site and two 20-ton modules at each near site, the statistical *uncertainty* is around 0.2%. The sensitivity of the Daya Bay experiment with this design can achieve the challenging goal of 0.01 with 90% confidence level in almost the whole range of Δm^2_{31}.
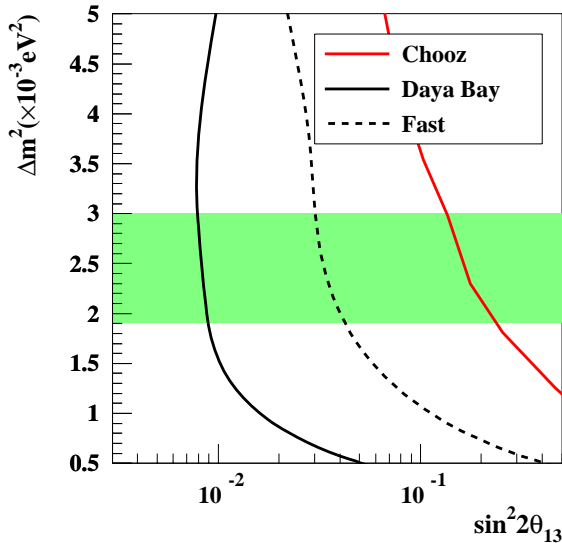

Fig. 3.13. Expected $\sin^2 2\theta_{13}$ sensitivity at 90% C.L. with 3 years of data, as shown in solid black line. The dashed line shows the sensitivity of the fast measurement with the DYB near site and the mid site only. The red line shows current upper limit measured by Chooz.
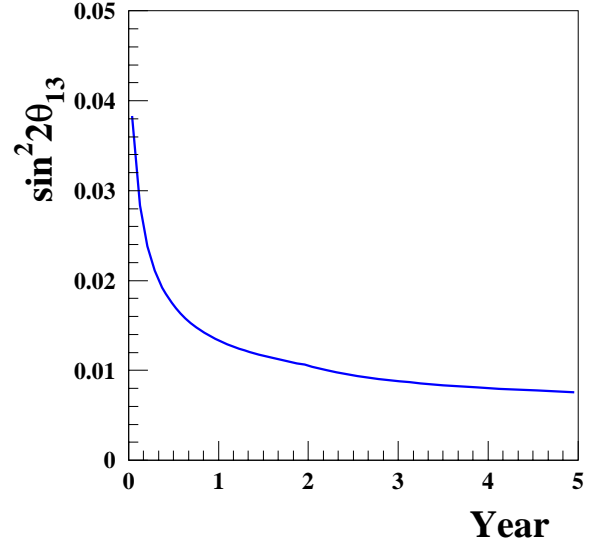
Fig. 3.14. Expected $\sin^2 2\theta_{13}$ sensitivity at 90% C.L. versus year of data taking of the full measurement, with two near sites and one far site. The Δm^2 is taken to be 2.5×10^{-3} eV^2.

Fig. 3.14 shows the sensitivity versus time of data taking. After one year of data taking, $\sin^2 2\theta_{13}$ sensitivity will reach 0.014 (1.4%) at 90% confidence level.

The tunnel of the Daya Bay experiment will have a total length around 3 km. The tunneling will take 1 $\sim$ 2 years. To accelerate the experiment, the first completed experimental hall, the Daya Bay near hall, can be used for detector commissioning. Furthermore, it is possible to conduct a fast experiment with only two detector sites, the Daya Bay near site and the mid site. For this fast experiment, the "far detector", which is located at the mid hall, is not at the optimal baseline. At the same time, the reactor-related *uncertainty* would be 0.7%, very large compared with that of the full experiment. However, the sensitivity is still much better than the current best limit of $\sin^2 2\theta_{13}$. It is noteworthy that the improvement comes from better background shielding and improved experiment design. The sensitivity of the fast experiment for one year data taking is shown in Fig. 3.13 in dashed line. With one year's data, the sensitivity is around 0.03 for $\Delta m^2 = 2.5 \times 10^{-3}$ eV^2, compared with the current best limit of 0.17 from the Chooz experiment.

3.5.3 Direct measurement of Δm_{31}^2

1. F. Suekane, *The Systematic Error Induced from the baseline differences in Kashiwazaki-Kariwa* $\sin^2 2\theta_{13}$ *experiment: A Conceptual Description* (Sept. 1, 2003).
2. P. Antonioli *et al.,* Astro. Phys. **7**, 357 (1997).
3. T. Gaisser, *Cosmic Rays and Particle Physics* (Cambridge University Press, 1991).
4. Y. Muraki *et al.,* Phys. Rev. D **28**, 40 (1983).
5. J. Kremer *et al.,* Phys. Rev. Lett. **83**, 4241 (1999)
6. H. Jokisch *et al.,* Phys. Rev. D **19**, 1368 (1979).
7. Y. F. Wang *et al.,* Phys. Rev. D **64**, 013012 (2001).
8. M. Apollonio *et al.,* Phys. Lett. **420B**, 397 (1998); Phys. Lett. **466B**, 415 (1999); Euro. Phys. J. C **27**, 331 (2003).
9. M. Ambrosio *et al.* (The MACRO Collaboration), Phys. Rev. D **52**, 3793 (1995); M. Aglietta *et al.* (LVD Collaboration), Phys. Rev. D **60**, 112001 (1999); Ch. Berger *et al.* (Frejus Collaboration), Phys. Rev. D **40**, 2163 (1989).
10. *Atomic Data and Nuclear Data Tables*, Vol. **78**, No. 2 (July, 2001).
11. T. Hagner *et al.,* Astro. Phys. **14**, 33 (2000).
12. T. Araki *et al.* (KamLAND Collaboration), Phys. Rev. Lett. **94**, 081801 (2005).
13. L. Wen *et al.*, Nucl. Instr. and Meth. A **564**, 471 (2006).
14. K. S. McKinny, *A Search for Astrophysical Electron Anti-neutrinos at KamLAND*, Ph. D thesis, University of Alabama.
15. F. Ardellier *et al.*, *Double-CHOOZ: a Search for the Mixing Angle* θ_{13} (June 20, 2006), hep-ex/0606025.
16. J. A. Rice, *Mathematical Statistics and Data Analysis*, 2nd ed. (Wadsworth Publishing Co., Inc., 1993).
17. F. Ashton, H. J. Edwards, and G. N. Kelly, J. Phys. A **4**, 352 (1971).
18. K. Anderson, *et al.*, *A New Nuclear Reactor Neutrino Experiment to Measure* θ_{13} (Feb. 26, 2004), hep-ex/0402041.
19. Y. F. Wang *et al.,* Phys. Rev. D **62**, 013012 (2000).
20. A. Piepke *et al.*, Nucl. Instr. and Meth. A **432**, 392 (1999); F. Boehm *et al.*, Phys. Rev. D **62**, 072002 (2000).
21. F. Boehm *et al.,* Phys. Rev. D **64**, 112001 (2001); Phys. Rev. D **62**, 072002 (2000); Phys. Rev. D **62**, 092005 (2000).
22. K. Eguchi *et al.,* Phys. Rev. Lett. **90**, 021802 (2003).
23. L. A. Mikaelyan and V. V. Sinev, Phys. Atom. Nucl. **63**, 1002 (2000); L. A. Mikaelyan, Nucl. Phys. Proc. Suppl. **91**, 120 (2001); L. A. Mikaelyan, Phys. Atom. Nucl. **65**, 1173 (2002).
24. F. Suekane, *The systematic error induced from the baseline differences in Kashiwazaki-Kariwa* $\sin^2 2\theta_{13}$ *experiment: A conceptual description* (unpublished).
25. H. Kwon *et al.,*, Phys. Rev. D **24**, 1097 (1981).
26. Y. Declais *et al.,* Phys. Lett. **B338**, 383 (1994); B. Ackar *et al.,* Nucl. Phys. **B434**, 503 (1995); B. Ackar *et al.,* Phys. Lett. **B374**, 243 (1996).
27. H. Sugiyama and O. Yasuda, *A formula for the sensitivity to* $\sin^2 2\theta_{13}$ *in reactor experiments with a spectral analysis* (Aug. 8, 2005), hep-ph/0508090.
28. P. Vogel *et al.*, Phys. Rev. C **24**, 1543 (1981); K. Schreckenbach *et al.*, Phys. Lett. **B160**, 325 (1985); A. A. Hahn *et al.*, Phys. Lett. **B218**, 365 (1989).

29. D. Stump *et al.*, Phys. Rev. D **65**, 014012 (2001).
30. Y. Fukuda *et al.,* Phys. Rev. Lett. **81**, 1562 (1998); Y. Ashie *et al.,* Phys. Rev. D **71**, 112005 (2005).
31. P. Huber, M. Lindner, T. Schwetz, and W. Winter, Nucl. Phys. **B665**, 487 (2003); Nucl. Phys. **B645**, 3 (2002).
32. H. Minakata *et al.,* Phys. Rev. D **68**, 033017 (2003); H. Minakata and H. Sugiyama, Phys. Lett. **B580**, 216 (2004).